



Software-based Speed-up Techniques

Scientific Programming with Python

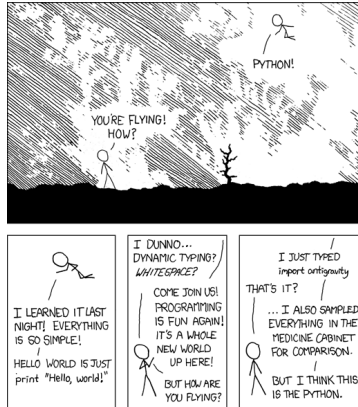
Christian Elsasser

Partially based on a talk by Stéfan van der Walt



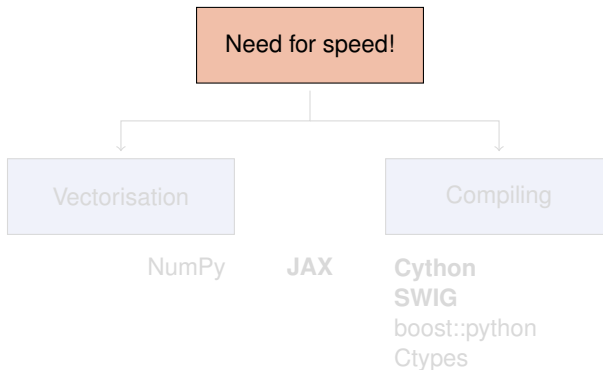
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Python is nice, but by construction not very fast ...

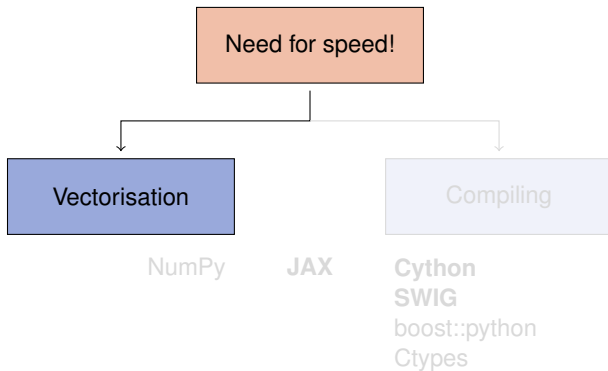


[xkcd]

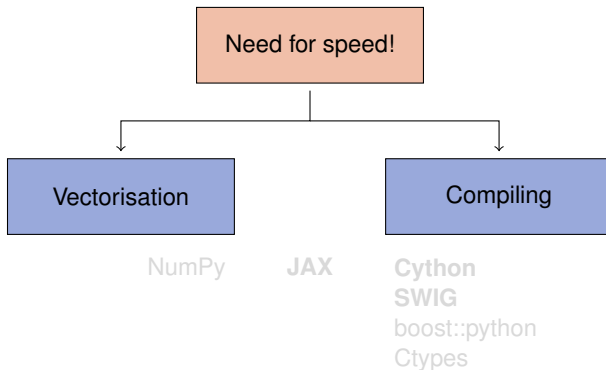
...so how can we overcome this issue?



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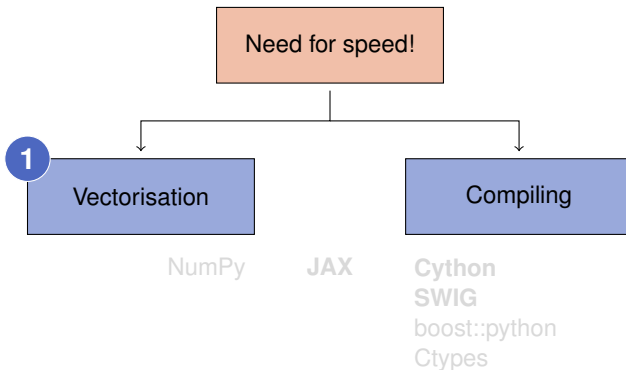


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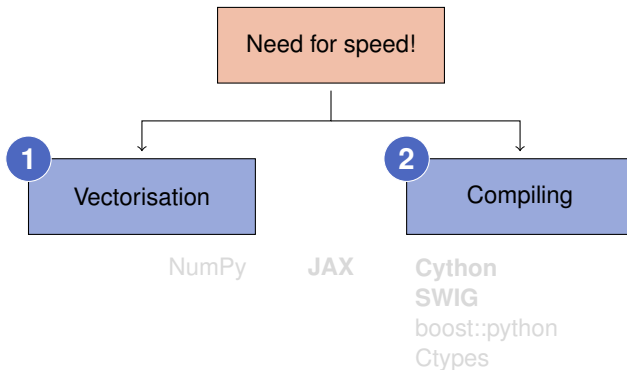


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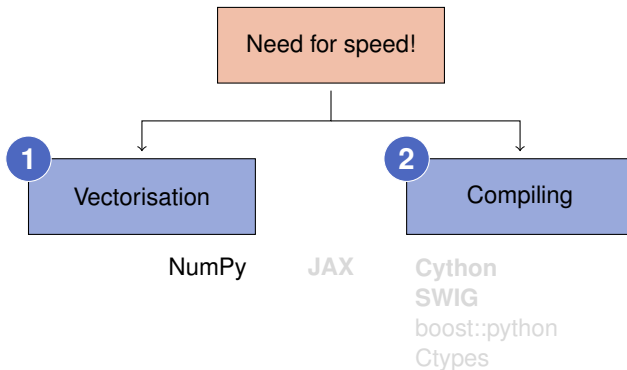


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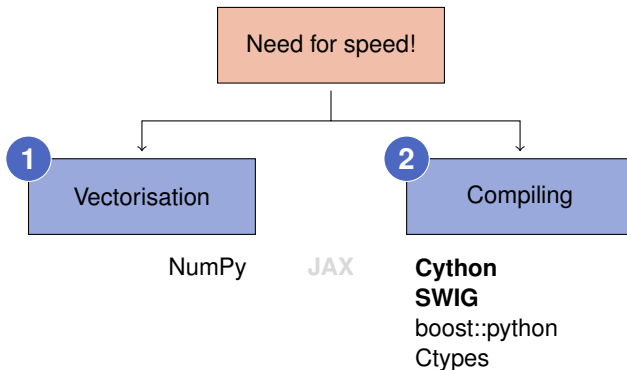




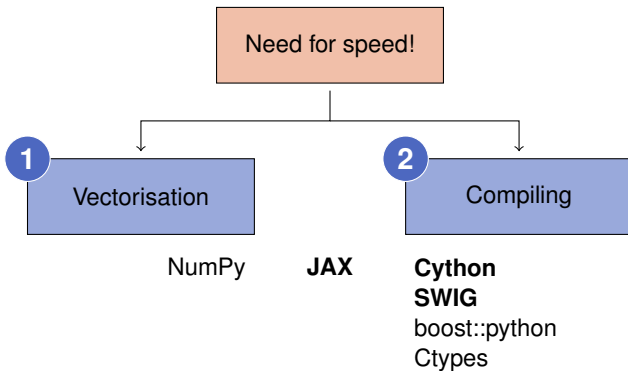
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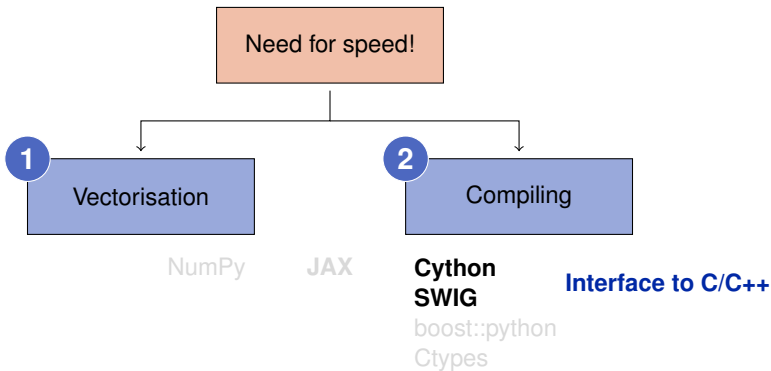
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... so how can we overcome this issue?





JAX - Accelerator-oriented Array Computation and Program Transformation

by Google

- ▶ **Auto-vectorisation:** Translating of code into an optimised version that is better leveraging vectorisation
- ▶ **Just-in-time (JIT) compilation:** Compiling of functions “on the fly” to improve their performance
- ▶ **Auto-parallelisation:** Automated conversion of code into a code running on multiple CPUs or GPUs
- ▶ **Automatic differentiation:** techniques leveraging mathematical rules to algorithmically evaluate derivatives, in particular for nested functions (*i.e.* via the chain rule)
- ▶ Same code can be run not just on CPUs, but also on GPUs and TPUs.



C keeps Python running ...

- ▶ CPython is the standard implementation of the Python interpreter written in C.
- ▶ The Python C API (application programming interface) allows to build C libraries that can be imported into Python (<https://docs.python.org/3/c-api/>)

The sum function ...

Pure Python

```
>>>>> a = [1,2,3,4,5,6,7,8]
>>>>> sum(a)
36
>>>>> b = [0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8]
>>>>> sum(b)
3.6
```

...looks in the back like this ...



...but takes a lot of the fun out of Python

C++ implementation

```
sum_list(PyObject *list) {  
    int i, n;  
    long total = 0;  
    PyObject *item;  
    n = PyList_Size(list);  
    if (n < 0)  
        return -1; /* Not a list */  
    for (i = 0; i < n; i++) {  
        item = PyList_GetItem(list, i); /* Can't fail */  
        if (!PyInt_Check(item)) continue; /* Skip non-integers */  
        total += PyInt_AsLong(item);  
    }  
    return total;  
}
```



C/C++ in Python: Not a New Thing

NumPy's C API

```
ndarray typedef struct PyArrayObject {  
    PyObject_HEAD;  
    char *data;  
    int nd;  
    npy_intp *dimensions;  
    npy_intp *strides;  
    PyObject *base;  
    PyArray_Descr *descr;  
    int flags;  
    PyObject *weakreflist;  
} PyArrayObject;
```

⇒ Several Python “standard” libraries are using C/C++ to speed things up



Example 1: Fibonacci series

Fibonacci function - Python

```
def fib(n):  
  
    a,b = 1,1  
    for i in range(n):  
        a,b = a+b,a  
    return a
```




Example 1: Fibonacci series

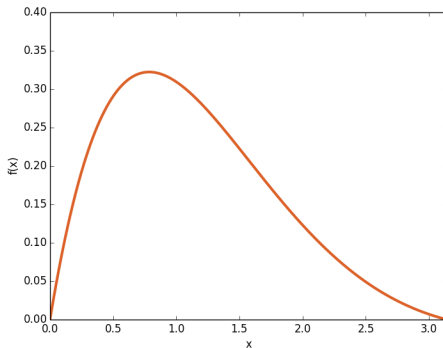
Fibonacci function - Cython

```
def fib(int n):  
    cdef int i,a,b  
    a,b= 1,1  
    for i in range(n):  
        a,b = a+b,a  
    return a
```

- ▶ Type declaration (`cdef`) \Rightarrow Python/Cython knows what to expect
- ▶ A few (simple) modifications can easily change the CPU time by a factor of $\mathcal{O}(100)$

Example 2: Numerical Integration

$$\int_0^{\pi} f(x) = \sin x \cdot e^{-x} \quad \text{Exact result: } \frac{e^{-\pi} + 1}{2} = 0.521607$$





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$$\int_0^{\pi} f(x) = \sin x \cdot e^{-x} \quad \text{Exact result: } \frac{e^{-\pi} + 1}{2} = 0.521607$$

- ▶ Return values of function can be specified via the key word `cdef`
- ▶ `cpdef` \Rightarrow function also transparent to Python itself (no performance penalty)
- ▶ C/C++ library can be imported via `from libc/libcpp.<module> cimport <name>` (see in the appendix and exercises)
- ▶ Using C++ functions can lead to a huge speed-up
- ▶ Try to do as much as you can in the C-layer
- ▶ **Already huge speed-up when leveraging NumPy and its vectorisation**



Cython can also handle and interact with other features of C/C++

- ▶ Cython comes with access to **fundamental C libraries** like `(math, stdlib)`
- ▶ There is a mapping between Python types and **STL containers** (e.g. `std::vector`) (see appendix).
- ▶ The same is also true for **exceptions/errors** in Python and C++.

You can find more details in the appendix and in the exercises.

Integration of C Functions in Cython

Starting point: .c/.h file for function definition e.g. fast_inv_sqrt

1. Expose it to **Cython** by **declaring the function signature**.
2. Integrating it into Cython either via direct usage or by defining a wrapper function.

_____ C function definition in c_func.c _____

```
#include <stdio.h>

double fast_inv_sqrt( double number )
{
    ...
}
```

Integration of C Functions in Cython

Starting point: .c/.h file for function definition e.g. fast_inv_sqrt

1. Expose it to **Cython** by declaring the function signature.
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Wrapping the function

```
cdef extern from "c_func.c":  
    double fast_inv_sqrt(double number)  
  
def py_fis(number:double) -> double:  
    return fast_inv_sqrt(number)  
  
def norm_vector(values:list) -> list:  
    length_squared = sum([x**2 for x in values])  
    return [x*fast_inv_sqrt(length_squared) for x in values]
```

Compiling Cython Code outside of a notebook

Support via `setuptools` for building and installing Python modules \Rightarrow applicable for cython

_____ Cython setup script _____

```
from setuptools import setup
from Cython.Build import cythonize

setup(ext_modules = cythonize([<name of .pyx files>],
                               language_level=3
))
```

Execute: `python setup.py build_ext --inplace`

Creates a `.c/.cpp` file for each `.pyx` file, then compiles it to an executable (in build sub-directory) and compiles a `.so` file (or a `.pxd` if you are using Windows)

Further options for `cythonize` via help explorable

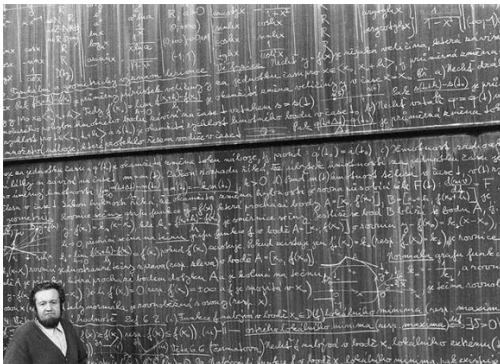


Automatic Wrappers

... since not everybody likes to write lines of error-prone code

- ▶ SWIG
- ▶ boost::python
- ▶ ctypes
- ▶ ...

Goal: creating compilable C/C++ code
based on the Python C API



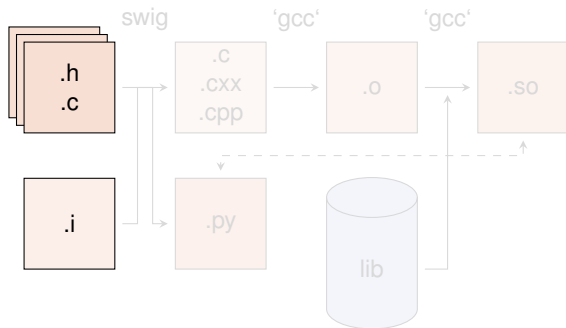


SWIG

SWIG: Simplified Wrapper and Interface Generator

- ▶ Generic Wrapper for C/C++ to script-like languages
 - ▶ R
 - ▶ Perl
 - ▶ Ruby
 - ▶ Tcl
 - ▶ PHP5
 - ▶ Java
 - ▶ ... and **Python**
- ▶ Pretty old – created in 1995 by Dave Beazley
- ▶ Current version is 4.0.2

SWIG – in a Nutshell

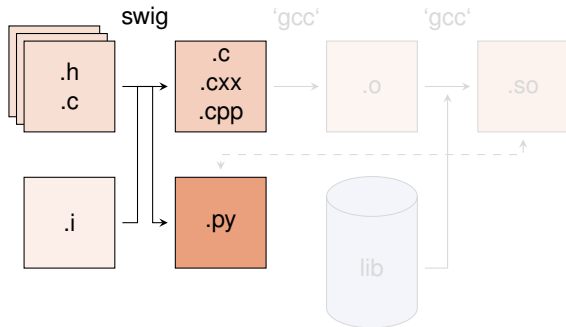


1. Create python wrapper and necessary C files
`swig -c++ -python <name>.i`
2. Compile shared object (*i.e.* library)

Step 2 best handed to setuptools
 (setup.py)
`python setup.py build_ext
 --inplace`

Module (<name>.py) can be imported into Python
 with `import name` ⇒ Shared object needs different
 name

SWIG – in a Nutshell



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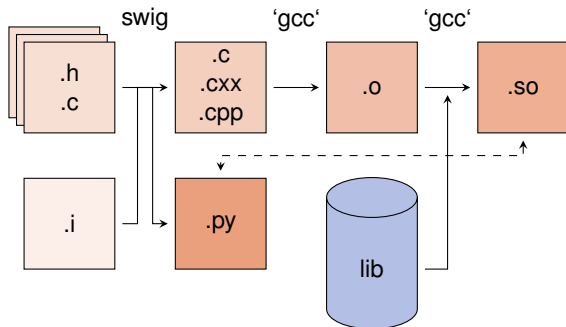
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```
python setup.py build_ext  
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SWIG – in a Nutshell



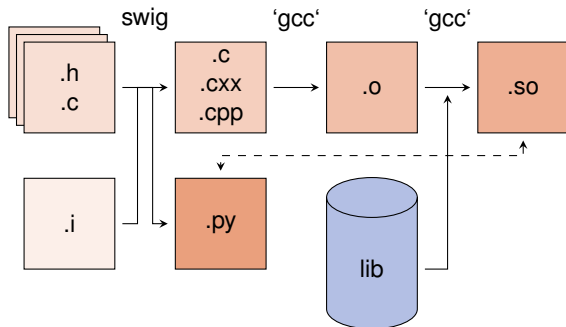
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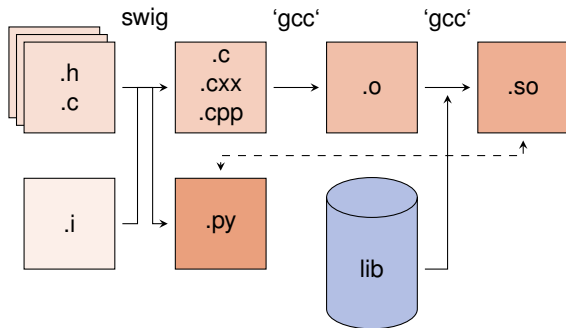
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SWIG – The `setup.py` file

```
_____ setuptools setup script (setup.py) _____  
  
from setuptools import setup, Extension  
extension_mod = Extension("_<name>", # Use _ to distinguish to final module name  
                           ["<name_wrap>.cxx",  
                           "<source1>.cpp",  
                           "<source2>.cpp", "..."],  
                           language='c++')  
setup(name = "_<name>", ext_modules=[extension_mod])
```

- ▶ To be build extension needs a different name than the module set up by SWIG (default: `_name`)
- ▶ Language option only needed for C++
- ▶ `python setup.py build_ext --inplace`



Summary

- ▶ There are several options to improve the speed of your code:
 - ▶ **Vectorisation:**
 - ▶ NumPy
 - ▶ JAX
 - ▶ **Compiling:**
 - ▶ JIT compiling
 - ▶ Cython
 - ▶ Write your code in a compiled language and wrap it for Python
 - ▶ Some further tools and considerations discussed by Roman in the afternoon
- ▶ Wrapping is particularly interesting for **existing code** allowing to integrate existing functionality in different languages.



Summary

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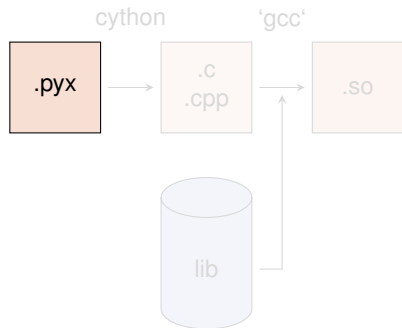
**University of
Zurich**^{UZH}

Faculty of Science



Appendix

Compiling Cython Code (The hard way)



Shared object (`<name>.so`) can be imported into Python with `import <name>`

1. Compile Cython code to C/C++ code
`cython3 -3 <name>.pyx`
2. Compile shared object file (i.e. library)

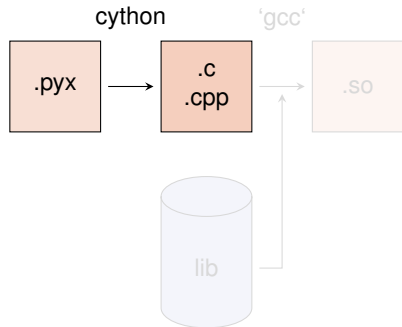
```
gcc [options] -fPIC -O2 -Wall  
-I<path_to_python_include>  
-L<path_to_python_library>  
<name>.c -o <name>.so
```

- ▶ If using C++ code, cython needs the option `-+` and `gcc` \rightarrow `g++`
- ▶ options are for MacOS X `-bundle -undefined dynamic_lookup` and for Debian `-shared`

School-Laptops:

```
gcc -shared -fPIC -O2 -Wall  
-I/usr/include/python3.9/  
<name>.c -o <name>.so
```

Compiling Cython Code (The hard way)



Shared object (`<name>.so`) can be imported into Python with `import <name>`

1. Compile Cython code to C/C++ code

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cython3 -3 <name>.pyx
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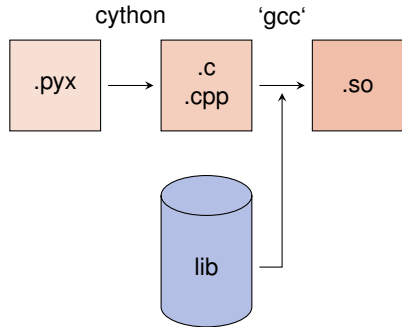
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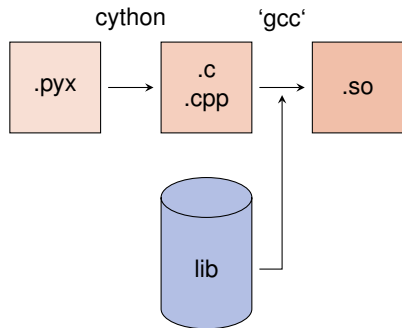
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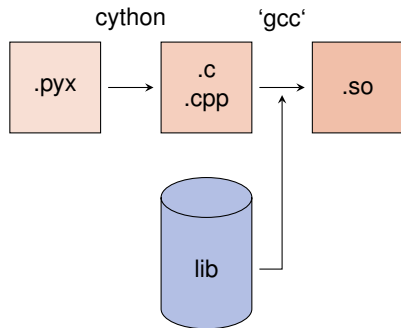
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```



STL Containers

An often used feature of C++ are the Standard Template Library containers (*e.g.* `std::vector`, `std::map`, etc.)

Object holders with specific memory access structure, *e.g.*

- ▶ `std::vector` allows to access any element
- ▶ `std::list` only allows to access elements via iteration
- ▶ `std::map` represents an associative container with a key and a mapped values

STL Containers

An often used feature of C++ are the Standard Template Library containers (e.g. `std::vector`, `std::map`, etc.)

... and Cython knows how to treat them!

Python	→	C++	→	Python
iterable	→	<code>std::vector</code>	→	list
iterable	→	<code>std::list</code>	→	list
iterable	→	<code>std::set</code>	→	set
iterable (len 2)	→	<code>std::pair</code>	→	tuple (len 2)
dict	→	<code>std::map</code>	→	dict
bytes	→	<code>std::string</code>	→	bytes





STL Containers

An often used feature of C++ are the Standard Template Library containers (e.g. `std::vector`, `std::map`, etc.)

A few remarks!

- ▶ iterators (e.g. `it`) can be used \Rightarrow dereferencing with `dereference(it)` and incrementing/decrementing with `preincrement` (i.e. `++it`), `postincrement` (i.e. `it++`), `predecrement` (i.e. `--it`) and `postdecrement` (i.e. `it--`) from `cython.operator`
- ▶ Be careful with performance! \Rightarrow performance lost due to shuffling of data
- ▶ More indepth information can be found directly in the corresponding sections of the cython code <https://github.com/cython/cython/tree/master/Cython/Includes/libcpp>
- ▶ C++11 containers (like `std::unordered_map`) are partially implemented



Exceptions/Errors

In terms of exception and error handling three different cases need to be considered:

- ▶ Raising of a **Python error** in cython code \Rightarrow return values make it impossible to raise properly Python errors (Warning message, but continuing)
- ▶ Handling of **error codes from pure C functions**
- ▶ Raising of a **C++ exception** in C++ code used in cython \Rightarrow C++ exception terminates – if not caught – program



Errors in Python

Python Error in Cython - untreated

```
cpdef int raiseError():  
    raise RuntimeError("A problem")  
    return 1
```

⇒ Just prints a warning (and worse gives an ambiguous return value)



Errors in Python

Python Error in Cython - untreated

```
cpdef int raiseError():  
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```

⇒ Just prints a warning (and worse gives an ambiguous return value)

Python Error in Cython - treated

```
cpdef int raiseError() except *:  
    raise RuntimeError("A problem")  
    return 1
```

⇒ Propagates the RuntimeError



Errors in C

C does not know exceptions like Python or C++. If errors should be caught, it is usually done via dedicated return values of functions which cannot appear in a regular function call.

Use the `except` statement to tell cython about this value

Handling a C Error

```
cpdef int raiseException() except -1:  
    return -1
```

Exceptions in C++



In cython this is also true for C++ exceptions!

Cython is not able to deal with C++ exceptions in a try-and-except clause!

⇒ But capturing in cython and translating to Python exceptions/errors is possible!

Exceptions in C++

...and how to tackle them!

- ▶ `cdef <C++ function>() except +`
⇒ translates a C++ exception into a Python error according to the right-hand scheme
- ▶ `cdef <C++ function>() except +<Python Error>` e.g. `MemoryError` ⇒ translates every thrown C++ exception into a `MemoryError`
- ▶ `cdef <C++ function>() except +<function raising Python error>` ⇒ runs the indicated function if the C++ function throws any exception. If `<function raising Python error>` does not raise an error, a `RuntimeError` will be raised.

C++	→	Python
<code>bad_alloc</code>	→	<code>MemoryError</code>
<code>bad_cast</code>	→	<code>TypeError</code>
<code>domain_error</code>	→	<code>ValueError</code>
<code>invalid_argument</code>	→	<code>ValueError</code>
<code>ios_base::failure</code>	→	<code>IOError</code>
<code>out_of_range</code>	→	<code>IndexError</code>
<code>overflow_error</code>	→	<code>OverflowError</code>
<code>range_error</code>	→	<code>ArithmeticError</code>
<code>underflow_error</code>	→	<code>ArithmeticError</code>
(all others)	→	<code>RuntimeError</code>



Classes

Classes are a common feature of Python and C++

There are two aspects when dealing with cython:

- ▶ **Defining classes containing C++ code in cython**
- ▶ C++ classes integrated into Python



Defining Classes in Cython

Let's go back to the integration examples

Defining classes in Cython

```
cdef class Integrand:
    cpdef double evaluate(self, double x) except *:
        raise NotImplementedError()

cdef class SinExpFunction(Integrand):
    cpdef double evaluate(self, double x):
        return sin(x)*exp(-x)

def integrate(Integrand f, double a, double b, int N):
    ...
    s += f.evaluate(a+(i+0.5)*dx)
```



Defining Classes in Cython

Let's go back to the integration examples

Adding classes in Python

```
class Poly(Integrand):  
    def evaluate(self, double x):  
        return x*x-3*x  
integrate(Poly(), 0.0, 2.0, 1000)
```

⇒ Speed lost with respect to definition in cython, but still faster than a pure Python implementation



Integration of C++ Classes in Cython – Possible but cumbersome

Starting point: .cpp/.h file for class Rectangle defined in a namespace shapes

1. Expose it to **Cython** by **declaring the class structure and method signatures**
2. Integrating it into Cython either via direct usage or by defining a wrapper class

Exposing C++ classes in Cython

```
# distutils: language = c++
# distutils: sources = Rectangle.cpp
cdef extern from "Rectangle.h" namespace "shapes":
    cdef cppclass Rectangle:
        Rectangle(int, int, int, int) except +
        int x0, y0, x1, y1
        int getLength()
        int getHeight()
        int getArea()
        void move(int, int)
```



Integration of C++ Classes in Cython – Possible but cumbersome

Starting point: .cpp/.h file for class Rectangle defined in a namespace shapes

1. Expose it to **Cython** by declaring the class structure and method signatures
2. Integrating it into Cython either via direct usage or by **defining a wrapper class**

Wrapping the class for Python

```
cdef class PyRectangle:
    cdef Rectangle *thisptr
    def __cinit__(self, int x0, int y0, int x1, int y1):
        self.thisptr = new Rectangle(x0, y0, x1, y1)
    def __dealloc__(self):
        del self.thisptr
    def getLength(self):
        return self.thisptr.getLength()
    def getHeight(self):
        return self.thisptr.getHeight()
    . . .
```



Arrays

Arrays in cython are usually treated via typed memoryviews (e.g. `double[:, :]` means a two-dimensional array of doubles, i.e. compatible with e.g. `np.ones((3,4))`)

Further you can specify which is the fastest changing index by `:1`, e.g.

- ▶ `double[:, :1, :]` is a F-contiguous three-dimensional array
- ▶ `double[:, :, :1]` is a C-contiguous three-dimensional array
- ▶ `double[:, :, :1, :]` is neither F- nor C-contiguous

For example a variable `double[:, :, :1]` `a` has as NumPy arrays variables like `shape` and `size` and the elements can be accessed by `a[i, j]`

But be aware: NumPy is already heavily optimised, so do not to reinvent the wheel!