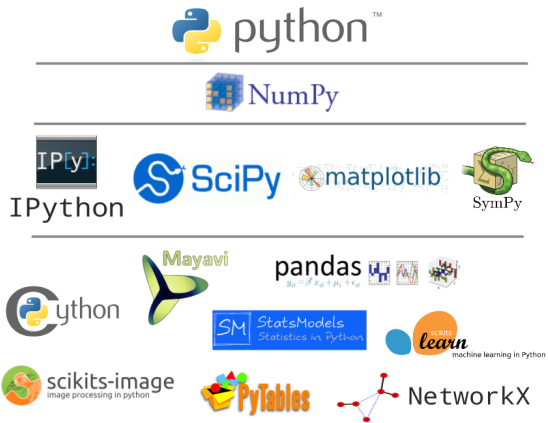
Scientific programming: data structures – NumPy, Pandas & beyond

Scientific programming with Python

Federica Lionetto

Based partially on a talk by Stéfan van der Walt

The ecosystem of Homo Python Scientificus



[Ondřej Čertík/LANL]

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NumPy – the fundamental container for scientific computing

`import numpy as np`

https://www.numpy.org

NumPy offers memory-efficient data containers for fast numerical operations, e.g. in data manipulation and typical linear algebra calculations

Standard Python

```
>>> L = list(range(1000))
>>> [i**2 for i in L]
```

NumPy

```
>>> import numpy as np
>>> a = np.arange(1000)
>>> a**2
```

$\Rightarrow$ Speed up by a factor of $\sim$ 100

Details about NumPy

`np.__version__` indicates version, `np.show_config()` reveals information about libraries

NumPy's C API

```
ndarray typedef struct PyArrayObject {
    PyObject_HEAD
    char *data;
    int nd;
    npy_intp *dimensions;
    npy_intp *strides;
    PyObject *base;
    PyArray_Descr *descr;
    int flags;
    PyObject *weakreflist;
} PyArrayObject ;
```

Creating NumPy arrays

There are several ways to do so

Creating arrays

```
>>> a = np.array([1,2,4])                  # [1,2,4]
>>> b = np.arange(1,15,2)                  # [1,3,5,7,9,11,13]
>>> c = np.linspace(0,1,6)                 # [0.0,0.2,0.4,0.6,0.8,1.0]
>>> d = np.empty((1,3))                    # empty 1x3 array
>>> e = np.zeros((2,5,3))                  # 2x5x3 array of zeros
>>> f = np.ones((3,3))                     # 3x3 array of ones
>>> g = np.eye(4)                          # 4x4 unit matrix
>>> h = np.identity(4)                     # 4x4 unit matrix
>>> i = np.diag(np.array([1,2,3,4]))       # diagonal matrix
>>> l = np.diag(np.array([1,2,3,4]),k=-1) # values just below the main diagonal
>>> m = np.diag(np.array([1,2,3,4]),k=2)  # values 2 rows above the main diagonal
```

NumPy arrays of random numbers

Again, several possibilities

Creating arrays

```
>>> a = np.random.rand(4)              # 4-elements array from [0,1)
>>> b = np.random.rand(4,3)            # 4x3 array from [0,1)
>>> c = np.random.randint(1,3,(2,3))   # 2x3 array from [1,3)
>>> d = np.random.randn(4,5)           # 4x5 array (norm. dist)
>>> e = np.random.poisson(3,5)         # 5-element array (Poisson dist of mean 3)
```

Random seed can be set with `np.random.seed(<integer>)`, useful for reproducibility of results

Basic operations

Many basic functions/operators can be applied on NumPy arrays

Examples

```
>>> a = np.random.rand(3,4)
>>> b = np.random.rand(3,4)

>>> a+b
>>> a-b
>>> a*b # Which product? See exercise in this lecture
>>> a/b
>>> a+3.0

>>> a>b
```

Basic operations - more

Many basic functions/operators can be applied on NumPy arrays

Examples

```
>>> a = np.random.rand(3,4)
>>> b = np.random.rand(3,4)

>>> a.min()
>>> a.min(axis=0)
>>> a.min(axis=1)

>>> np.exp(b)
>>> np.cos(b)
```

All element-wise operations including dedicated functions, called universal functions (ufunc)

`math.exp(b)` $\Rightarrow$ failure as it expects scalar

Data representation

Data type accessible via `dtype` variable

Datatype

```
>>> a = np.array([1,0,-2],dtype=np.int64)   #[1,0,-2]
>>> b = np.array([1,0,-2],dtype=np.float64) #[1.0,0.0,-2.0]
>>> c = np.array([1,0,-2],dtype=np.bool)    #[True,False,True]
>>> c.dtype # dtype('bool')
```

Data structure

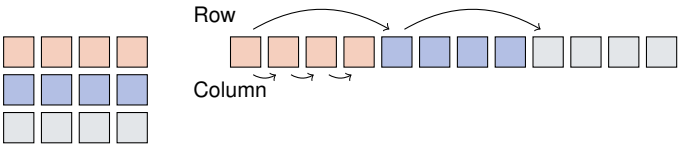
Information via attributes accessible:

`ndim`	number of dimensions (axes)
`shape`	size of the different dimensions (as a tuple, `ndim` elements)
`size`	total number of elements
`itemsize`	size of one element
`nbytes`	data size
`data`	memoryview of the data (`tobytes()` returns the byte representation)
`flags`	among other things if the memory “belongs” to this array
`strides`	number of bytes to jump to in-/decrement index by one (as a tuple)

Data structure

Strides

Problem of one-dimensional memory to store multi-dimensional arrays:

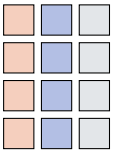


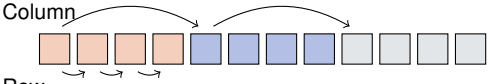
Strides describe the logical alignment of the data within the memory

Data structure

Strides

Problem of one-dimensional memory to store multi-dimensional arrays:





Transposing the array means to interchange the strides of the different dimensions

Strides describe the logical alignment of the data within the memory

Data structure

Information via attributes accessible:

`ndim`	number of dimensions (axes)
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`flags`	among other things if the memory “belongs” to this array
`strides`	number of bytes to jump to in-/decrement index by one (as a tuple)

Transpose of arrays can be called by `<array name>.T` $\Rightarrow$ inverts shape and strides (*i.e.* C-contiguous $\leftrightarrow$ F-contiguous)

Be aware that many manipulations do not lead to memory duplications. You can force it by the `copy` method.

Shape manipulation

Possible to manipulate the shape of existing arrays

Examples

```
>>> a = np.random.randn(3,4)
>>> b = np.random.randn(4)
>>> c = np.random.randn(4,1)

>>> a.reshape(1,12)
>>> a.resize(1,12) # Modify existing array
>>> a.ravel()
>>> a.T
>>> b.shape #(4,) wrong way
>>> b.T # no changes
>>> c.shape #(4,1) right way
>>> c.T # expected behaviour
```

Get the data

Reading data from txt/csv/etc. files can be sometimes very painful, especially with complicated/mixed data structure

NumPy offers an easy way to read in data from text files

- function `loadtxt(fname,dtype,comments,delimiter,skiprows,usecols,...)`
  - `delimiter` for columns separation, `comments` for the string indicating comments in the text file
- function `genfromtxt(...,missing_values,filling_values)`
  - more advanced options for missing data

Binary files as well as text files are also readable via the function `fromfile`

Get the data

Complicated data structure are manageable by defining the data type, e.g.

Solar.txt (Solar system on June 21, 2014)

```
Sun     332946 2.13E-03 -1.60E-03 -1.20E-04  5.01E-06 ...
Mercury 0.0552 1.62E-01  2.64E-01  6.94E-03 -2.97E-02 ...
Venus   0.8149 3.02E-01  6.54E-01 -8.44E-03 -1.85E-02 ...
Earth   1.00   5.66E-01 -8.46E-01 -9.12E-05  1.40E-02 ...
```

Datatype

```
>>> dt = np.dtype([('name','|S7'),('mass',np.float),
 ('position',[('x',np.float),('y',np.float),('z',np.float)]),
 ('velocity',[('x',np.float),('y',np.float),('z',np.float)])])

>>> data = np.loadtxt('Solar.txt',dtype=dt)
```

Strings in arrays

Strings in arrays are in principle not a problem (as seen before), but two things to keep in mind

1. Speed reduction due to a different common base type of the objects stored in the array (*i.e.* PyObject)
2. Memory spoiling since the entry size is defined by the maximal length of the stored strings

$\Rightarrow$ if possible, better work with e.g. lookup tables

In general you can mix different data types in an array

Mixed datatype

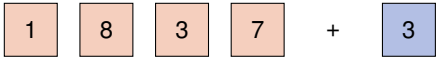
```
>>> na = np.array([2,True,"Hello"],dtype=object)
```

without `dtype=object` the elements would be treated as strings

Broadcasting – leveraging vectorisation

Memory-friendly way of combining arrays with different shapes in mathematical operations

Example:



Arrays are alignable if the number of elements in the dimensions match
(*i.e.* they are equal or there is only one element)

Details can be found in docstrings `np.doc.broadcasting`

Broadcasting – leveraging vectorisation

Memory-friendly way of combining arrays with different shapes in mathematical operations

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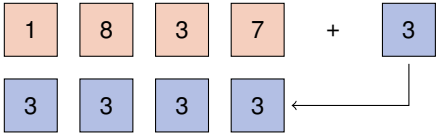

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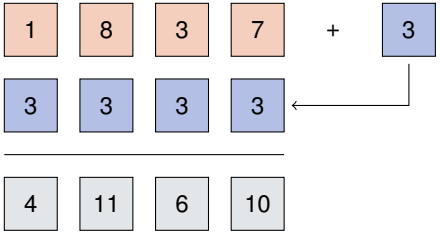
Details can be found in docstrings `np.doc.broadcasting`

Broadcasting – leveraging vectorisation

Memory-friendly way of combining arrays with different shapes in mathematical operations

Example:

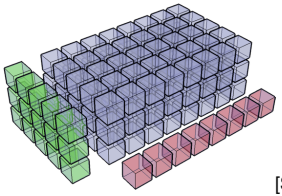


Arrays are alignable if the number of elements in the dimensions match
(*i.e.* they are equal or there is only one element)

Details can be found in docstrings `np.doc.broadcasting`

Broadcasting – more complex

Multiplication of a 3×5-array and a 8-elements array



[S. v. d. Walt]

Broadcasting

```
>>> a = np.random.rand(3,5)
>>> b = np.random.rand(8)
>>> c = a[...,np.newaxis]*b
>>> c.shape # (3,5,8)
```

`np.newaxis` allows to align the dimensions of arrays so that they can be broadcasted, but be careful and make sure the arrays are aligned as you want them.

Broadcasting – matching rules

This principle can be expanded to multi-dimensional arrays,
e.g. a 3×4-array and a 4-elements array
⇒ adding/multiplying/etc. the 1D array to each of the three rows of the 2D array

Rule: Compare dimensions, starting from the last one. Match when either dimension is one or None, or if dimensions are equal.

`(3,4)`	`(4,1,6)`	`(3,4,1)`	`(3,2,5)`	`(4,2,3)`	`(4,1,3)`
`(4)`	`(1,3,6)`	`(8)`	`(6)`	`(4,3)`	`(4,3)`
`(3,4)`	`(4,3,6)`	`(3,4,8)`	`not OK`	`not OK`	`(4,4,3)`

Arrays can be extended to further dimensions by
`<array name>[...,np.newaxis]`, e.g.

`a.shape` → `(3,2)`
⇒ `a[...,np.newaxis,np.newaxis].shape` → `(3,2,1,1)`

Explicit broadcasting

NumPy has the method `broadcast_arrays` to align two or more arrays

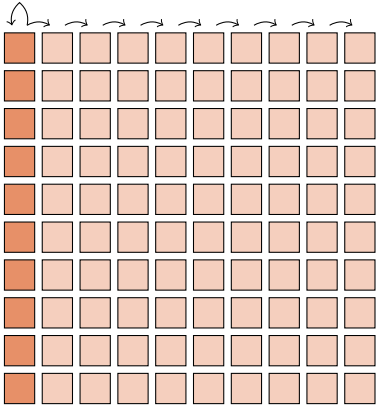
Explicit Broadcasting

```
>>> d = np.random.rand(1,10)
>>> e = np.random.rand(10,1)
>>> dd,ee = np.broadcast_arrays(d,e)
```

`dd` and `ee` are now 10 $\times$ 10-arrays, but without own data

Broadcasted arrays have a stride of zero $\Rightarrow$ pointer stays while index moves

This concept is a generalisation of the `meshgrid` function in MATLAB



Simple indexing

NumPy allows to easily select subsets in the array, e.g.

Simple indexing

```
>>> a = np.arange(100).reshape(10,10)
>>> a[4:9]           # rows 4 to 8
>>> a[:,3:8]         # columns 3 to 7
>>> a[:,-1]          # the last column
>>> a[-2::-3,1:6:2] # 2nd-to-last row every 3rd and every odd column from 1 to 5
```

Also repetition of rows or columns are possible, e.g.

Simple indexing (continued)

```
>>> a[:,[1,3,1]]
```

All these operations do not create additional memory entries!

Fancy indexing

NumPy also allows to select subsets via arrays of indices, e.g.

Fancy indexing

```
>>> a = np.arange(100).reshape(10,10)
>>> i0 = np.random.randint(0,10,(8,1,8))
>>> i1 = np.random.randint(0,10,(2,8))
>>> a[i0,i1] # creates a 8×2×8 array
```

- First broadcasting of the two index arrays `i0` and `i1`
- Then selecting the elements in `a` according to the broadcasted arrays

Caution: Mixing of indexing types (e.g. `b[5:10,i0,:,i1]`) can lead to unpredictable output shapes (and to barely readable code)

Pandas

`import pandas as pd` – and never use Excel again!

https://pandas.pydata.org

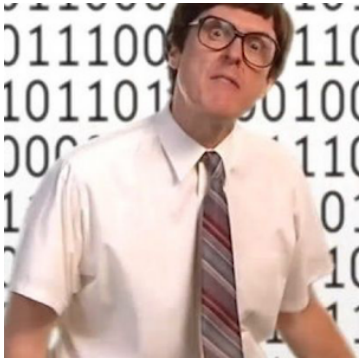
- Python data analysis library
- Tools for reading and writing data and interface to a large variety of file formats (nobody has heard about all of them!)
- Offering data containers plus corresponding functionality
  - DataFrame object for data manipulation
  - time series `pd.Series` and their notorious functions (*i.e.* rolling-"whatever"-you-want function)
  - many SQL-like data operations (group, merge, join)
- Data interface/API to many data repositories (Yahoo Finance, FRED)

Excel on steroids!

. . . but particularly helpful tool to transform data (clean-up, aggregation, . . .)

numpy *vs.* pandas

NumPy



fast and good with numbers

Pandas

a bit slow and cool with everything

Some functionalities and pitfalls

Functionalities

- Fill missing (NA) values according to different principles
- Timeseries applications (*e.g.* `resample`)
- Data aggregation (*e.g.* `groupby`)
- Merging tools (*e.g.* `append`, `concat`, `merge`, `join`)
- Derivation of new features via `map` (from Series) or `apply` (from Dataframe)

Pitfalls

- Pandas tries to be smart!!!
- It accepts data as long as it can derive the lowest common ancestor (almost always the case although ending up with `object`)
- . . . so you should check the data types `dtypes` since your processing code (e.g. `groupby`) will work, but not as expected

NumPy and Pandas - reloaded

If you work with big data, chances are high that at some point you'll encounter a `MemoryError` when loading your data. What next?

- Dask
  https://dask.pydata.org/en/latest/
  - flexible parallel computing library for analytics
  - compatible with NumPy, Pandas, Scikit-Learn and many others

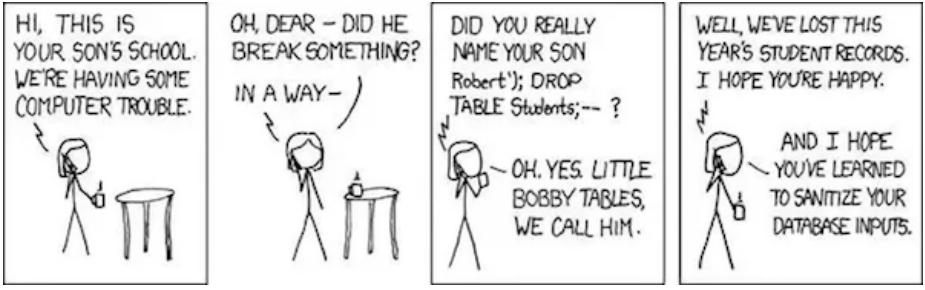
Pandas

```
>>> import pandas as pd
>>> df = pd.read_csv('2018-01-01.csv')
>>> df.groupby(df.user_id).value.mean()
```

Dask

```
>>> import dask.dataframe as dd
>>> df = dd.read_csv('2018-*-*.csv')
>>> df.groupby(df.user_id).value.mean()
    .compute()
```

Other options for storing data



- Pickle, JSON, YAML and protocol buffers
- SQL and NoSQL

Pickle and JSON – brothers from other mothers

Pickle

- Python proprietary
- . . . thus also Python objects storable
  → class instances
  → NumPy arrays
- Binary files

JSON (javascript object notation)

- Interface to other/web applications
- Similar structures
  Python: array → JSON: array
  Python: dict → JSON: object
- Some format issues need to be cleared

Pickle

```
>>> a = dict(...)
>>> with open(<filename>,'wb') as f_o:
>>>   pickle.dump(a,f_o)
>>> with open(<filename>,'rb') as f_i:
>>>   b = pickle.load(f_i)
```

JSON

```
>>> a = dict(...)
>>> with open(<filename>,'w') as f_o:
>>>   json.dump(a,f_o)
>>> with open(<filename>,'r') as f_i:
>>>   b = json.load(f_i)
```

. . . also string-wise possible (dumps/loads)

YAML

Improved version of JSON

- language-portable
- more human-readable, *e.g.* indentation instead of symbols

Examples

```
data = {
'first_data':[1,2,3,4,5],
'second_data':'Just a string.',
'third_data':  dict(a=1.1,b=1.2,c=1.3)}
with open('example.yaml','w',default_flow_style=False) as f_o :
yaml.dump(data,f_o)

with open('example.yaml','r') as f_i:
new_data = yaml.load(f_i)
```

Protocol buffers

Example: address book application that can read and write information from/to a file. How do we exchange this data?

- Pickle
- JSON
- Custom encoding
- XML
- **protobuf**: Google's mechanism for serialising structured data that uses a binary format to transfer messages
  - it works with different programming languages
  - it transfers data as fast as possible, as compact as possible
  - well-defined schema, but no need to worry if schema changes over time

How to work with protocol buffers

- Define messages (and their fields) in a .proto file
  - messages can consist of fields and other messages, nested structure
  - fields have name, type, modifier and tag
- Use the protocol buffer compiler to compile the .proto file
- Use the Python protocol buffer API to read and write messages

Connection to SQL Databases - `sqlite3`

What is SQLite? (https://www.sqlite.org)

- Lightweight disk-based (= server-less) SQL-type (= spreadsheet-based) database system
- Does not require a separate server process
- Understands most of the standard SQL language but omits some features (drop column, rename column)
- Due to the outsourced write-interlock handling write-intensive programs will suffer

Another option, `SQLAlchemy` (http://www.sqlalchemy.org)

- Python SQL toolkit that gives developers the full power and flexibility of SQL
- Probably the most suitable package for a database-type independent approach, with connections to:
  - MySQL
  - Microsoft Access
  - SQLite

A Few Typical (SQL) Commands

https://www.sqlite.org

Purpose	Command
Retrieve all data from a table	`SELECT * FROM <table>`
Retrieve columns (`c1,c2`) from table `t` based on condition	`SELECT c1,c2 FROM t WHERE <cond>`
Group entries according to values	`SELECT SUM(c1),AVG(c2) FROM t GROUP BY c3,c4`
Add new entry	`INSERT INTO t (c1,c2) values (v1,v2)`
Delete one or more entries	`DELETE FROM t WHERE c1=v1 AND c2=v2`

sqlite3

https://docs.python.org/3.6/library/sqlite3.html

- Database operations on sqlite3 databases
- `sqlite3.connect` to get a handler on the database
- Default output of (part of) a row is a list

  $\Longrightarrow$ possibility to change the behaviour via the `row_factory` variable of the database
- Use `?` as placeholder instead of concatenating the SQL command by Python string operations
- Use `executemany()` to run same SQL command with several parameter sets
- All executed commands need to be commited before closing the connection (`<dbvariable>.commit()`)

Summary

- Python offers various options to handle data suitable for different purposes
  - NumPy is a very powerful tool for numerical computations and data manipulations
  - Pandas offers functionalities of the combination of spreadsheet and database processing
  - Various other options to store data – different formats for different purposes
- Further leverage with analytics tool (`scipy`) $\Longrightarrow$ Scientific analysis lecture
- Very handy tool for data management...
- ... but, for certain particular tasks, other and more suitable options (e.g. large image databases that can be heavily compressed)
- Try it out, try it out, try it out!

References

1. Stéfan van der Walt, *Diving into NumPy*, Advanced Scientific Programming in Python, 2013 (Zurich)
2. Bartosz Teleńczuk, *Introduction to data visualization*, Advanced Scientific Programming in Python, 2013 (Zurich)
3. Stéfan van der Walt, S. Chris Colbert and Gaël Varoquaux, *The NumPy array: a structure for efficient numerical computation*, Computing in Science and Engineering (IEEE)
4. http://www.numpy.org
5. http://pandas.pydata.org

Backup

Data Structure (Advanced)

Further information via the `flags` variable accessible:

C_CONTIGUOUS	dimension ordering C-like
F_CONTIGUOUS	dimension ordering Fortran-like
OWNDATA	responsibility of memory handling
WRITEABLE	data changable
ALIGNED	appropriate hardware alignment
UPDATEIFCOPY	update of base array

C-contiguous:
$a[0,0], a[0,1], \ldots, a[0,n], a[1,0], \ldots, a[m,n]$

F-contiguous:
$a[0,0], a[1,0], \ldots, a[m,0], a[0,1], \ldots, a[m,n]$

Broadcasting (Dimensional)

This principle can be expanded to multi-dimensional arrays, e.g. a 3×4-array and a 1D 4-elements array ⇒ adding/multiplying/etc. to each of the three rows the 1D array

Rule: Compare dimensions, starting from the last one. Match when either dimension is one or None, or if dimensions are equal.

`(3,4)`	`(4,1,6)`	`(3,4,1)`	`(3,2,5)`
`(4)`	`(1,3,6)`	`(8)`	`(6)`
`(3,4)`	`(4,3,6)`	`(3,4,8)`	`not OK`

Arrays can be extended to further dimensions by `<array name>[...,np.newaxis]`, e.g.

`a.shape` → `(3,2)`
⇒ `a[...,np.newaxis,np.newaxis].shape` → `(3,2,1,1)`