Online Monitoring for the Silicon Tracker of the LHCb Experiment

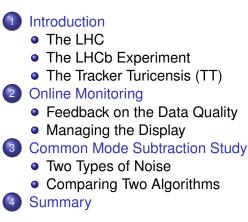
Nicola Chiapolini

Physik-Institut Universität Zürich

09. July 2009

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Outline

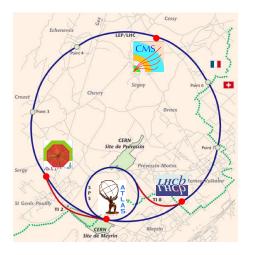




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The LHC

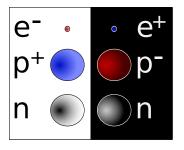
The LHC (The Large Hadron Collider)



- underground ring-tunnel
- 27 km circumference
- over 5000 proton bunches in 2 beam pipes
- protons accelerated to almost speed of light (*E_{kin}* = 7 TeV)
- collisions at 4 interaction points (every 25 ns)
- expected restart: Sept/Oct 2009

The LHCb Experiment

Physics Motivation



anti-particle twin of normal particle with opposite charge

- Big Bang produced equal amounts of particles and anti-particles
- no anti-matter in known universe
- few processes affect particles and anti-particles differently
- present model of processes can not explain the huge difference

Goal: Study these processes and look for new effects.

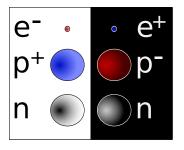
The LHCb Experiment

Physics Motivation - Details

- LHCb looks at CP violation and rare B meson decays
- CP violation observed in weak interactions
- CKM mechanism of Standard Model can explain CP violation
- current results consistent with predictions
- but too small to explain matter/anti-matter asymmetry
- new source of CP violation needed

The LHCb Experiment

Physics Motivation



anti-particle twin of normal particle with opposite charge

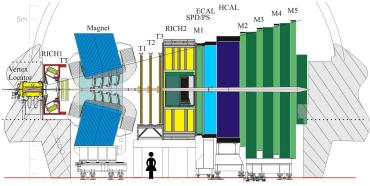
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The LHCb Experiment

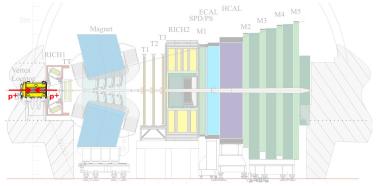
The LHCb Detector



- consists of many subdetectors
- each measuring different properties of particles (e.g. energy, momentum)
- UZH contribution is the Tracker Turicensis (TT)

The LHCb Experiment

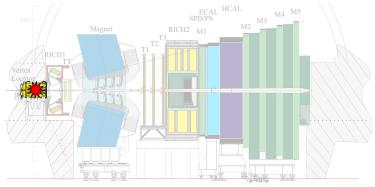
The LHCb Detector



- create new particles
- 2 new particles decay
- In properties of decay products measured (e.g. flight path)

The LHCb Experiment

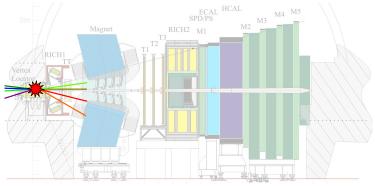
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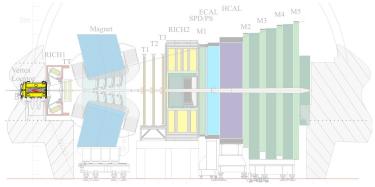
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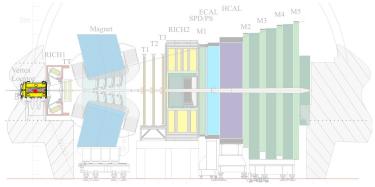
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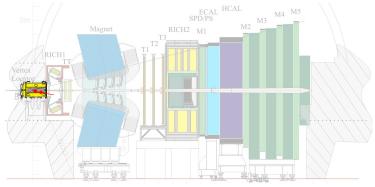
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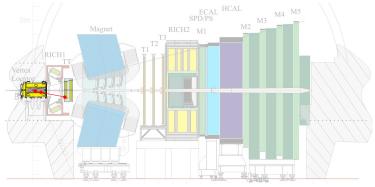
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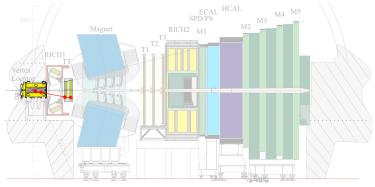
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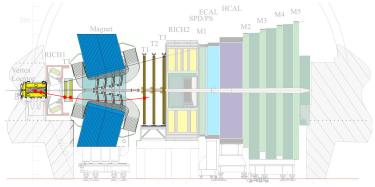
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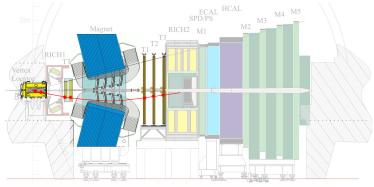
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The LHCb Experiment

The LHCb Detector

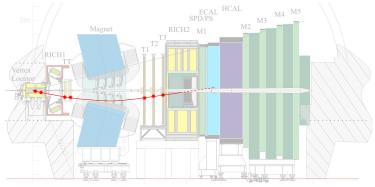


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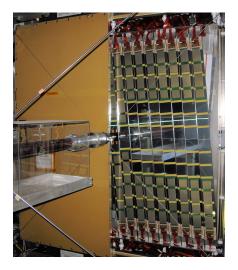
The LHCb Experiment

The LHCb Detector



- Create new particles
- 2 new particles decay
- properties of decay products measured (e.g. flight path)

Silicon Strip Detector



Detector hardware

- tracking detector
- 4 layers
- 1036 silicon sensors
- 143360 channels in total

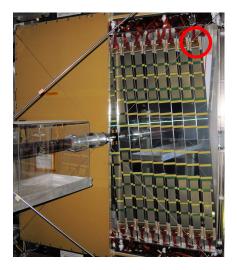
Reading out

• 128 channels in one Beetle readout chip

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32 channels in one port

Silicon Strip Detector



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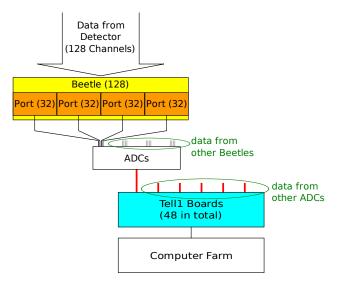
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Readout Electronics



What did I do?

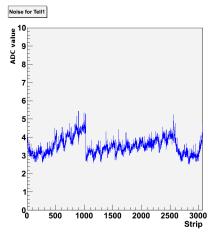
Part 1: Enhance Online Monitoring

Part 2: Study Common Mode Subtraction Algorithms

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Feedback on the Data Quality

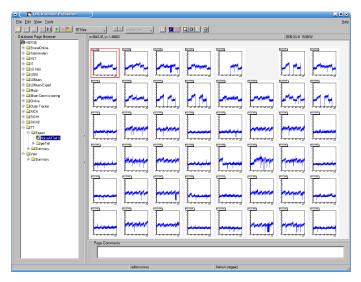
Online Monitoring



- important to get fast feedback
- continuously analyse data
- create histograms (e.g. of noise)
- display for person on shift

Feedback on the Data Quality

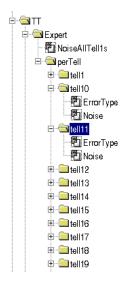
Display Monitoring Pages



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Managing the Display

Tool to Automate Configurations



- 48 Tell1 boards
- create pages per Tell1 board
- very tedious and error prone to setup by hand
- implemented tool to automate
- tool is not TT specific
- already used by two other subdetectors

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Managing the Display

Example Code

```
folderBase = "Expert/perTell/tell"
page = "Noise"
```

histoSet = "CMS/cms_\$tell" histoNum = range(1, 49)

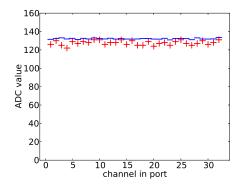
What did I do?

Part 1: Enhance Online Monitoring

Part 2: Study Common Mode Subtraction Algorithms

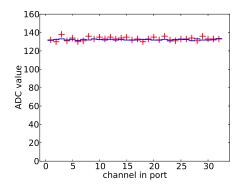
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Raw Noise



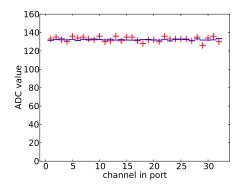
- readout registers ADC value even without particle
- ADC value fluctuates around pedestal
- pedestal different for each channel
- pedestal is subtracted
- rms of this fluctuation: raw noise

Raw Noise



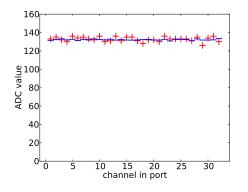
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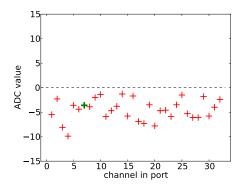
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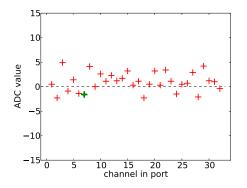
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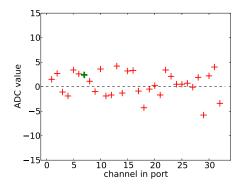
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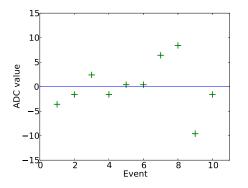
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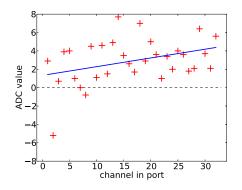
Raw Noise



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Two Types of Noise

Common Mode Subtracted (CMS) Noise

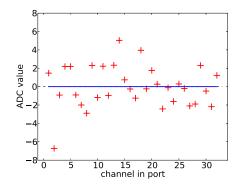


- after subtracting pedestal
- common mode:
 - linear effect on all channels
 - different for each event

- common mode is subtracted
- rms of this fluctuation: CMS noise

Two Types of Noise

Common Mode Subtracted (CMS) Noise



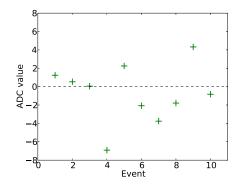
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Two Types of Noise

Common Mode Subtracted (CMS) Noise



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Comparing Algorithms

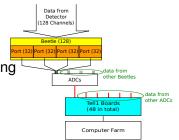
Common Mode calculation

- done on the Tell1 boards
- additionally implemented for monitoring

Studied configurations

- 3 different algorithms
- 7 different implementations
- many different parameters (e.g. pedestal calculation, hit detection)

Selected results presented below.



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Comparing Two Algorithms

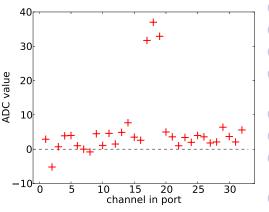
Looking at Two Algorithms

- explain the two algorithms
- compare results for different numbers of hits

ST algorithm

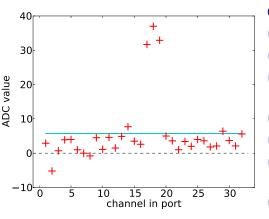
- implemented on Tell1 board at the moment
- strongly motivated by limitations on Tell1 boards
 - no floating point arithmetic
 - limited resources
 - only divisions by powers of 2

ST Algorithm



- calculate mean
- 2 subtract mean
- 3 detect hits
- set hits and neighbours to zero
- 5 calculate new mean
- subtract new mean
- fit straight line (using least-squares)

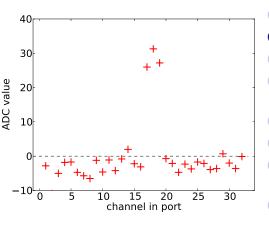
ST Algorithm



calculate mean

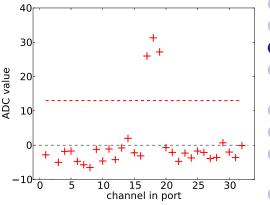
- subtract mean
- 3 detect hits
- set hits and neighbours to zero
- 5 calculate new mean
- subtract new mean
- fit straight line (using least-squares)

ST Algorithm



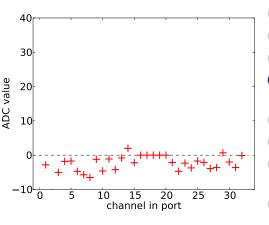
- calculate mean
- Subtract mean
- 3 detect hits
- set hits and neighbours to zero
- 5 calculate new mean
- subtract new mean
- fit straight line (using least-squares)

ST Algorithm



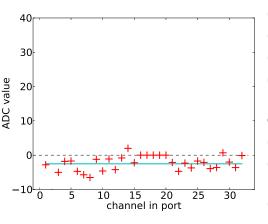
- calculate mean
- 3 subtract mean
- detect hits
 - set hits and neighbours to zero
- 5 calculate new mean
- subtract new mean
- fit straight line (using least-squares)
- subtract line

ST Algorithm



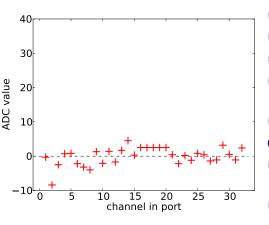
- calculate mean
- subtract mean
- 3 detect hits
- set hits and neighbours to zero
 - calculate new mean
 - subtract new mean
 - fit straight line (using least-squares)

ST Algorithm



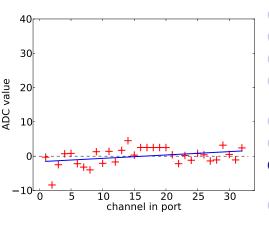
- calculate mean
- 2 subtract mean
- 3 detect hits
- set hits and neighbours to zero
- calculate new mean
 - subtract new mean
 - fit straight line (using least-squares)

ST Algorithm



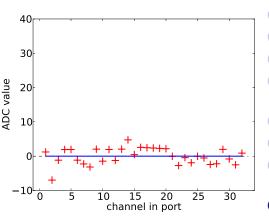
- calculate mean
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ST Algorithm



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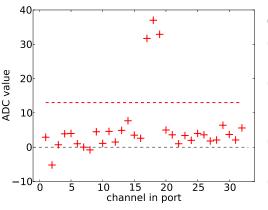
Comparing Two Algorithms

2P Algorithm

Why another algorithm?

- avoid least-squares method
- look for simple algorithm for monitoring
- two point algorithm (2P)

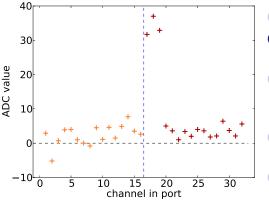
2P Algorithm



detect hits

- split channels in two sets (channels 1-16, 17-32)
- calculate mean ADC and mean strip ignoring hits
- calculate slope and offset of line through 2 points

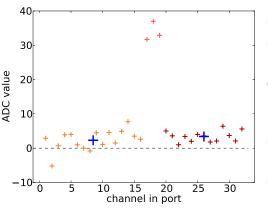
2P Algorithm



detect hits

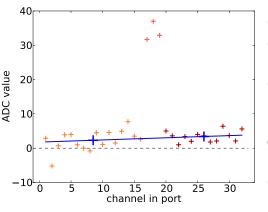
- split channels in two sets (channels 1-16, 17-32)
- calculate mean ADC and mean strip ignoring hits
- calculate slope and offset of line through 2 points

2P Algorithm



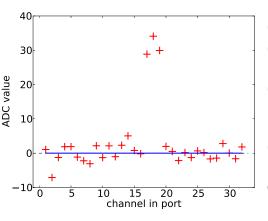
- detect hits
- split channels in two sets (channels 1-16, 17-32)
- calculate mean ADC and mean strip ignoring hits
 - calculate slope and offset of line through 2 points

2P Algorithm



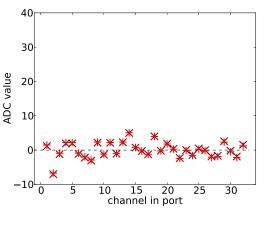
- detect hits
- Split channels in two sets (channels 1-16, 17-32)
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2P Algorithm



- detect hits
- Split channels in two sets (channels 1-16, 17-32)
- calculate mean ADC and mean strip ignoring hits
- calculate slope and offset of line through 2 points

Comparison of the Two Algorithms



+ ST × 2P

Without hits comparable results

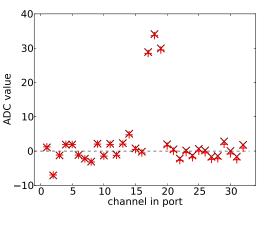
Few hits

comparable results

Many hits

ST algorithm gives wrong common mode

Comparison of the Two Algorithms



+ ST × 2P

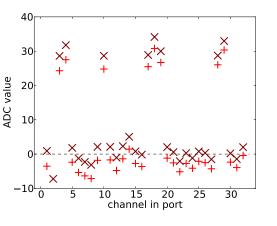
Without hits comparable results

Few hits comparable results

Many hits

ST algorithm gives wrong common mode

Comparison of the Two Algorithms



+ ST × 2P

Without hits comparable results

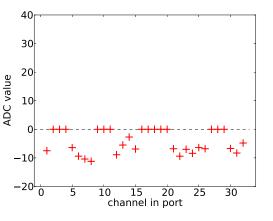
Few hits comparable results

Many hits

ST algorithm gives wrong common mode

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Reason for Wrong Common Mode



Way hits are treated

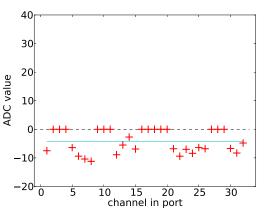
- ST sets to zero
- 2P ignores completely

Setting hits to zero

- zeros influence calculations
- 2nd mean wrong
- common mode wrong

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Reason for Wrong Common Mode



Way hits are treated

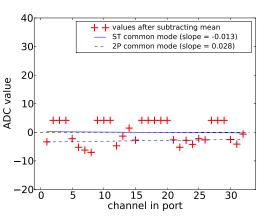
- ST sets to zero
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Setting hits to zero

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Reason for Wrong Common Mode



Way hits are treated

- ST sets to zero
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Setting hits to zero

- zeros influence calculations
- 2nd mean wrong
- common mode wrong

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Comparing Two Algorithms

What Did We Learn?

Most important difference

- ST sets hits to zero
- 2P ignores hits completely

Reason

- only divisions by powers of 2 on Tell1 boards
- 2P implemented without this constraint

Result

- comparable without hits/with few hits
- ST algorithm wrong for many hits

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Summary

Online Monitoring

- new pages and histograms added
- developed tool for management

Common Mode subtraction algorithms

- treatment of hits is important
- ST algorithm: possible improvements?
- 2P algorithm: implementation on Tell1?

Thank you for your attention

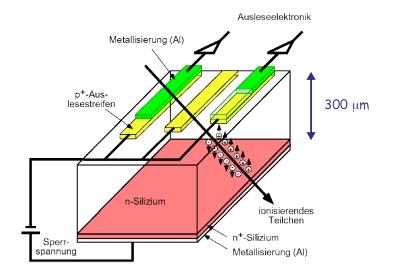
Questions?

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Further Results

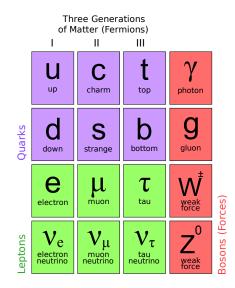
Algorithm	ST	VELO	2P
integers	+0.03	n/a	n/a
PCN- pedestals	+0.02 (- Xtalk)	similar to ST algorithm	similar to ST algorithm
CMS no hits	reference	-0.01	—0.01 (+ at Ends)
CMS 1% occ.	< 0.01	+0.08 (hit detection)	< 0.01
CMS 10% occ.	+0.08	n/a	-0.1

How do Silicon Sensors Work?



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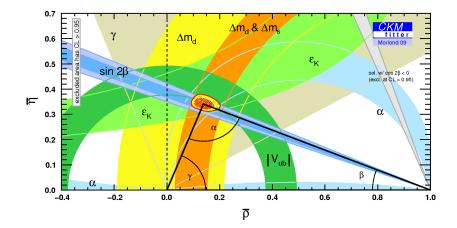
Particles in the Standardmodel



Appendix

Unitarity Triangle

Unitarity Triangle



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Appendix

Elementary Big Bang

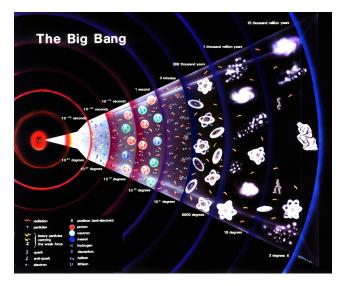
Pair Production

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Appendix

Big Bang



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