



Electroweak precision measurements at hadron colliders

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Outline of the talk

- precision tests of the Standard Model
- observables at high-energy hadron colliders and determination of the EW parameters
- tools necessary to extract the EW parameters from the kinematical distributions
- present limitations and future perspectives

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LHC can be a precision physics machine, provided that...

The past

from the Fermi theory to the LEP measurements of M_W and $\sin^2\theta$

From the Fermi theory of weak interactions to the discovery of W and Z

Fermi theory of β decay

muon decay $\mu^- \rightarrow \nu_\mu e^- \bar{\nu}_e$ $\frac{1}{\tau_\mu} \rightarrow \Gamma_\mu \rightarrow G_\mu$

QED corrections to Γ_μ necessary for precise determination of G_μ
computable in the Fermi theory (Kinoshita, Sirlin, 1959)

The independence of the QED corrections of the underlying model (Fermi theory vs SM) allows

- to define G_μ and to measure its value with high precision

$$G_\mu = 1.1663787(6) \cdot 10^{-5} \text{ GeV}^{-2}$$

- to establish a relation between G_μ and the SM parameters

$$\frac{G_\mu}{\sqrt{2}} = \frac{g^2}{8m_W^2} (1 + \Delta r)$$

The properties of physics at the EW scale
with sensitivity to the full SM and possibly to BSM via virtual corrections (Δr)
are related to a very well measured low-energy constant

From the Fermi theory of weak interactions to the discovery of W and Z

The SM predicts the existence of a new neutral current, different than the electromagnetic one
(Glashow 1961, Weinberg 1967, Salam 1968)

The observation of weak neutral current immediately allowed the estimate of the value of the weak mixing angle in the correct range
GARGAMELLE, Phys.Lett. 46B (1973) 138-140

From the basic relation among the EW parameters it was immediately possible to estimate the order of magnitude of the mass of the weak bosons, in the 80 GeV range
(Antonelli, Maiani, 1981)

The discovery at the CERN SPPS of the W and Z bosons and the first determination of their masses allowed the planning of a new phase of precision studies culminated with the construction of two e^+e^- colliders (SLC and LEP) running at the Z resonance

The precise determination of M_Z and of the couplings of the Z boson to fermions and in particular the value of the effective weak mixing angle allowed to establish a framework for a test of the SM at the level of its quantum corrections

There is evidence of EW corrections beyond QED with 26σ significance!
Full 1-loop and leading 2-loop radiative corrections are needed to describe the data
(indirect evidence of bosonic quantum effects)

The renormalisation of the SM and a framework for precision tests

- The Standard Model is a **renormalizable** gauge theory based on $SU(3) \times SU(2)_L \times U(1)_Y$
- The gauge sector of the SM lagrangian is assigned specifying (g, g', v, λ) in terms of 4 measurable inputs
- More observables can be computed and expressed in terms of the input parameters, including the available radiative corrections, at any order in perturbation theory
- The validity of the SM can be tested comparing these predictions with the corresponding experimental results
- The input choice $(g, g', v, \lambda) \leftrightarrow (\alpha, G_\mu, M_Z, M_H)$ **minimises the parametric uncertainty** of the predictions

$$\alpha(0) = 1/137.035999139(31)$$

$$G_\mu = 1.1663787(6) \times 10^{-5} \text{ GeV}^{-2}$$

$$m_Z = 91.1876(21) \text{ GeV}/c^2$$

$$m_H = 125.09(24) \text{ GeV}/c^2$$

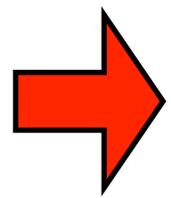
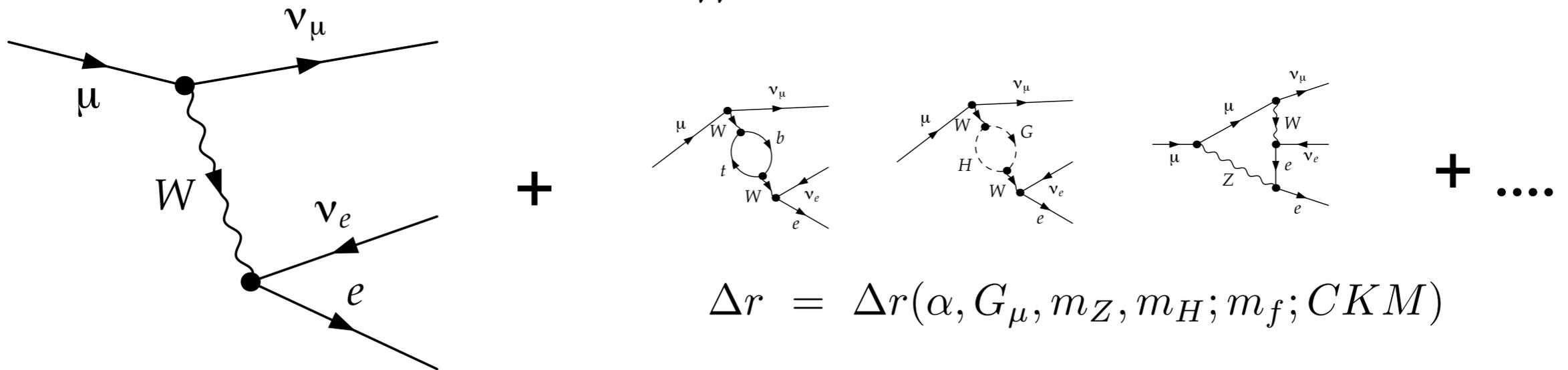
- M_W and the weak mixing angle are **predictions** of the SM, to be tested against the experimental data

The W boson mass: theoretical prediction

$$\mathcal{L}_{SM} = \mathcal{L}_{SM}(\alpha, G_\mu, m_Z; m_H; m_f; CKM)$$

→ we can compute m_W

$$\frac{G_\mu}{\sqrt{2}} = \frac{g^2}{8m_W^2} (1 + \Delta r)$$



$$m_W^2 = \frac{m_Z^2}{2} \left(1 + \sqrt{1 - \frac{4\pi\alpha}{G_\mu \sqrt{2} m_Z^2} (1 + \Delta r)} \right)$$

The W boson mass: theoretical prediction

Sirlin, 1980, 1984; Marciano, Sirlin, 1980, 1981;

van der Bij, Veltman, 1984; Barbieri, Ciafaloni, Strumia 1993;

Djouadi, Verzegnassi 1987; Consoli, Hollik, Jegerlehner, 1989;

Chetyrkin, Kühn, Steinhauser, 1995;

Barbieri, Beccaria, Ciafaloni, Curci, Viceré, 1992, 1993; Fleischer, Tarasov, Jegerlehner, 1993;

Degrassi, Gambino, AV, 1996; Degrassi, Gambino, Sirlin, 1997;

Freitas, Hollik, Walter, Weiglein, 2000, 2003;

Awramik, Czakon, 2002; Awramik, Czakon, Onishchenko, Veretin, 2003; Onishchenko, Veretin, 2003

The best available prediction includes

the full 2-loop EW result, higher-order QCD corrections, resummation of reducible terms

$$m_W = w_0 + w_1 dH + w_2 dH^2 + w_3 dh + w_4 dt + w_5 dH dt + w_6 da_s + w_7 da^{(5)}$$

$$dt = [(M_t/173.34 \text{ GeV})^2 - 1]$$

$$da^{(5)} = [\Delta\alpha_{\text{had}}^{(5)}(m_Z^2)/0.02750 - 1]$$

$$dH = \ln\left(\frac{m_H}{125.15 \text{ GeV}}\right)$$

$$dh = [(m_H/125.15 \text{ GeV})^2 - 1]$$

$$da_s = \left(\frac{\alpha_s(m_Z)}{0.1184} - 1\right)$$

	$124.42 \leq m_H \leq 125.87 \text{ GeV}$	$50 \leq m_H \leq 450 \text{ GeV}$
w_0	80.35712	80.35714
w_1	-0.06017	-0.06094
w_2	0.0	-0.00971
w_3	0.0	0.00028
w_4	0.52749	0.52655
w_5	-0.00613	-0.00646
w_6	-0.08178	-0.08199
w_7	-0.50530	-0.50259

G.Degrassi, P.Gambino, P.Giardino, arXiv:1411.7040

The W boson mass: theoretical prediction

re-evaluation of the MW prediction G.Degrassi, P.Gambino, P.Giardino, arXiv:1411.7040

$$M_W = 80.357 \pm 0.009 \pm 0.003 \text{ GeV} \quad (\text{parametric and missing higher orders})$$

parametric uncertainties

$$\begin{array}{lll} \text{MW varies with } m_t: & \Delta m_t = +1 \text{ GeV} & \rightarrow \Delta M_W = +6 \text{ MeV} \\ \text{with } \Delta\alpha_{\text{had}}(M_Z): & \Delta\alpha_{\text{had}}(M_Z) = +0.0003 & \rightarrow \Delta M_W = -6 \text{ MeV} \end{array}$$

estimate of missing higher-order contributions

two calculations performed directly in the OS renormalization scheme or
in the MSbar scheme with the eventual translation to OS values
MSbar scheme \rightarrow systematic inclusion of higher-order corrections in the couplings

the comparison of the two numerical results

suggests that missing higher orders might have a residual effect of $O(6 \text{ MeV})$

Global electroweak fit (Gfitter, arXiv:1407.3792)

$$M_W = 80.358 \pm 0.008 \text{ GeV} \quad \text{indirect determination more precise than direct measurement}$$

The weak mixing angle(s): theoretical prediction(s)

- the prediction of the weak mixing angle can be computed in different renormalisation schemes differing for the systematic inclusion of large higher-order corrections

- on-shell** definition:
$$\sin^2 \theta_{OS} = 1 - \frac{m_W^2}{m_Z^2} \quad \text{definition valid to all orders}$$

- MSbar** definition:

$$\frac{G_\mu}{\sqrt{2}} = \frac{g^2}{8m_W^2} \longrightarrow \hat{s}^2 \hat{c}^2 = \frac{\pi\alpha}{\sqrt{2}G_\mu m_Z^2 (1 - \Delta\hat{r})} \quad \hat{s}^2 \equiv \sin^2 \hat{\theta}$$

weak dependence on top-quark corrections

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weak dependence on top-quark corrections

- the **effective leptonic weak mixing** angle enters in the definition of the effective Z-f-fbar vertex at the Z resonance

$$\mathcal{M}_{Zl+l-}^{eff} = \bar{u}_l \gamma_\alpha [\mathcal{G}_v^f(m_Z^2) - \mathcal{G}_a^f(m_Z^2) \gamma_5] v_l \varepsilon_Z^\alpha \quad 4|Q_f| \sin^2 \theta_{eff}^f = 1 - \frac{g_V^f}{g_A^f}$$

and can be computed in the SM (or in other models) in different renormalisation schemes

$$\sin^2 \theta_{eff}^{lep} = \kappa(m_Z^2) \sin^2 \theta_{OS} = \hat{\kappa}(m_Z^2) \sin^2 \hat{\theta}$$

- the parameterization of the full two-loop EW calculation is

$$\begin{aligned} \sin^2 \theta_{eff}^f = & s_0 + d_1 L_H + d_2 L_H^2 + d_3 L_H^4 + d_4 (\Delta_H^2 - 1) + d_5 \Delta_\alpha \\ & + d_6 \Delta_t + d_7 \Delta_t^2 + d_8 \Delta_t (\Delta_H - 1) + d_9 \Delta_{\alpha_s} + d_{10} \Delta_Z, \end{aligned}$$

Awramik, Czakon, Freitas, hep-ph/0608099

f	e, μ, τ	$\nu_{e, \mu, \tau}$	u, c	d, s
s_0	0.2312527	0.2308772	0.2311395	0.2310286
d_1 [10^{-4}]	4.729	4.713	4.726	4.720
d_2 [10^{-5}]	2.07	2.05	2.07	2.06
d_3 [10^{-6}]	3.85	3.85	3.85	3.85
d_4 [10^{-6}]	-1.85	-1.85	-1.85	-1.85
d_5 [10^{-2}]	2.07	2.06	2.07	2.07
d_6 [10^{-3}]	-2.851	-2.850	-2.853	-2.848
d_7 [10^{-4}]	1.82	1.82	1.83	1.81
d_8 [10^{-6}]	-9.74	-9.71	-9.73	-9.73
d_9 [10^{-4}]	3.98	3.96	3.98	3.97
d_{10} [10^{-1}]	-6.55	-6.54	-6.55	-6.55

Results from LEP and SLC: $\sin^2\theta_{\text{eff}}(\text{leptonic})$

- the forward-backward asymmetry in e^+e^- collisions: “forward” is defined w.r.t. the incoming e^-
- Born-level relation

$$A_{FB}(m_Z^2) = \frac{3}{4} \frac{2g_v^e g_a^e \times 2g_v^f g_a^f}{[(g_v^e)^2 + (g_a^e)^2][(g_v^f)^2 + (g_a^f)^2]} \equiv \frac{3}{4} \mathcal{A}^e \mathcal{A}^f$$

- radiative corrections in the SM at the Z resonance, “Z-pole approximation” :
neglecting non-resonant box contributions and bosonic corrections to photon-exchange diagrams
⇒ factorisation of the Z amplitude as the product of initial- and final-state EW form factors
⇒ the structure of AFB remains $3/4 \mathcal{A}^e \mathcal{A}^f$, tree-level couplings replaced by form factors
⇒ definition of an effective coupling at $\sqrt{s}=M_Z$, with the real part of the form factors

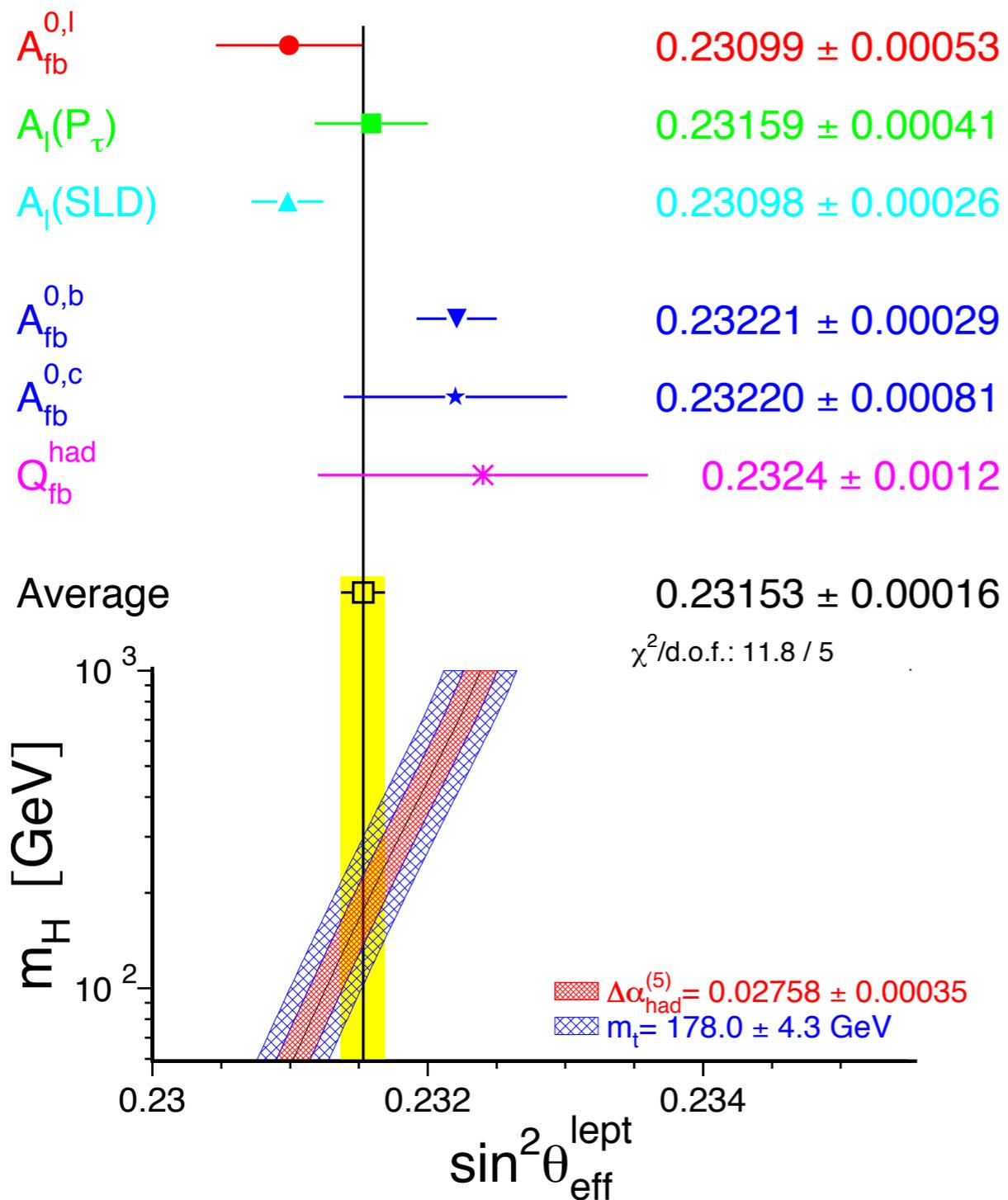
$$4|Q_f| \sin^2 \theta_{eff}^f = 1 - \frac{g_V^f}{g_A^f}$$

- “model independent” parameterisation of the Z boson couplings to fermions at the Z resonance used for the fit to the experimental data
→ sensitivity to Higgs and to BSM physics
entering via the gauge boson vacuum polarization (oblique corrections)

- the left-right polarization asymmetry at the Z resonance allowed at SLD
crucial complementary tests of the effective angle

$$A_{LR}(m_Z^2) = \mathcal{A}^e$$

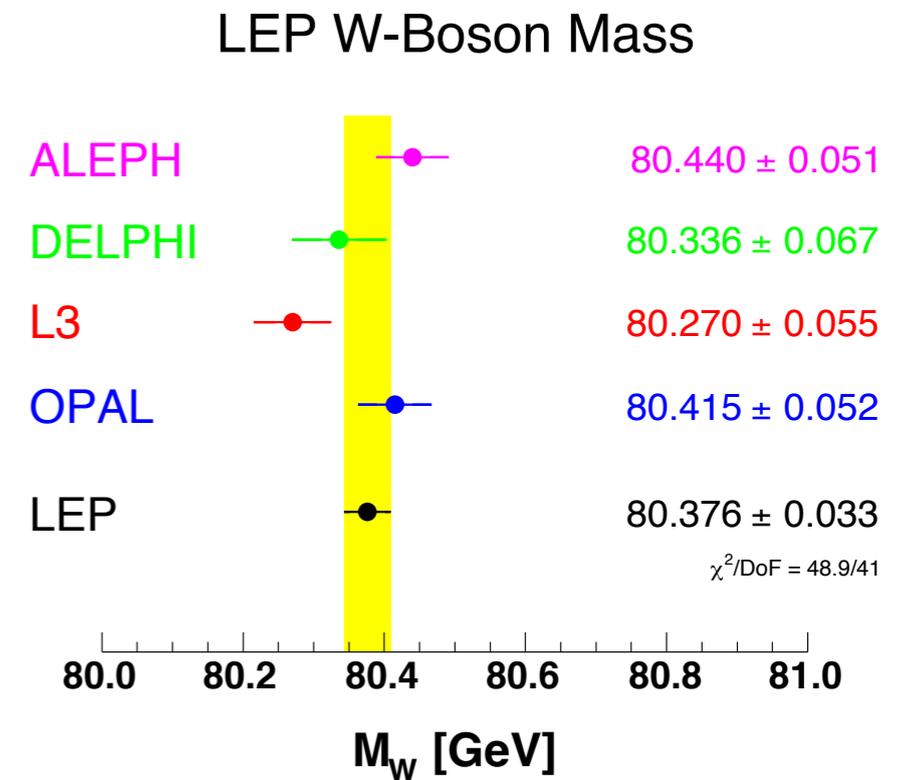
Results from LEP and SLC: $\sin^2\theta_{\text{eff}}^{\text{leptonic}}$



- good sensitivity to the Higgs mass value
- tension between SLD and LEP results
- tension between leptonic and b-quark asymmetries

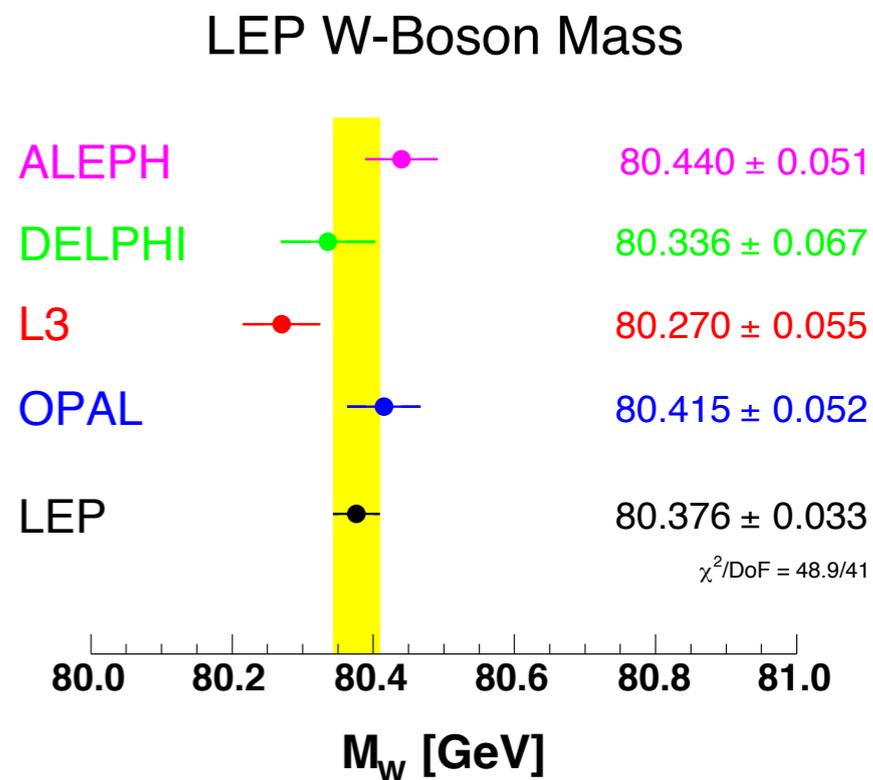
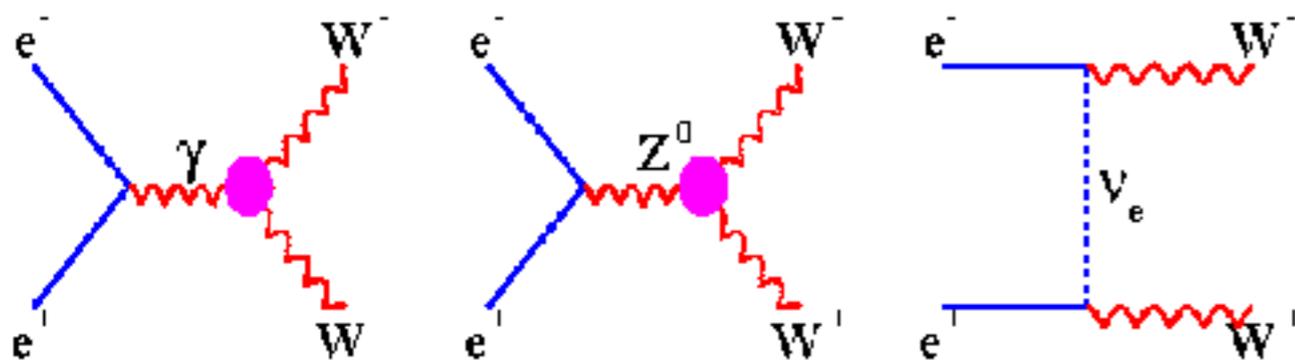
an independent measurement at hadron colliders can help to test the likelihood of the SM

Results from LEP2 for MW



- the semi-leptonic channel was “golden” because
 - ▷ only two jets → unique **invariant mass** reconstruction
 - ▷ no colour reconnection or Bose-Einstein correlation problems
- LEP2 measurement mostly limited by statistics

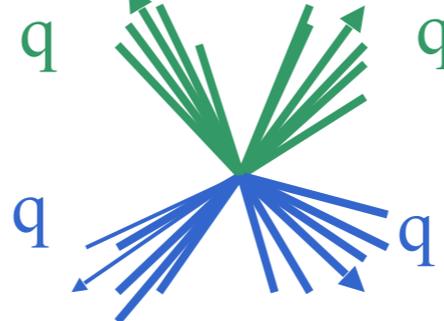
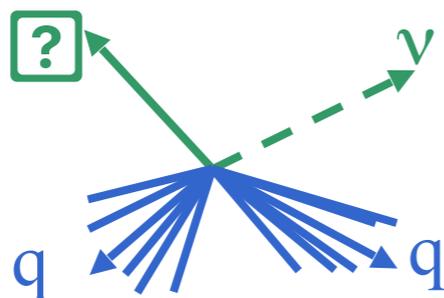
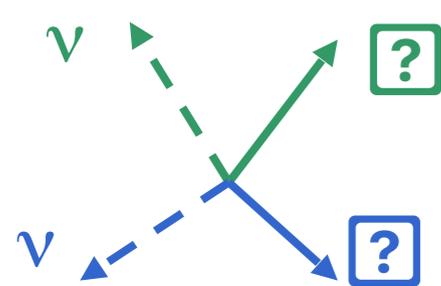
Results from LEP2 for MW



Leptonic

Semileptonic (qqlv)

Hadronic (4q)



Low Mw sensitivity

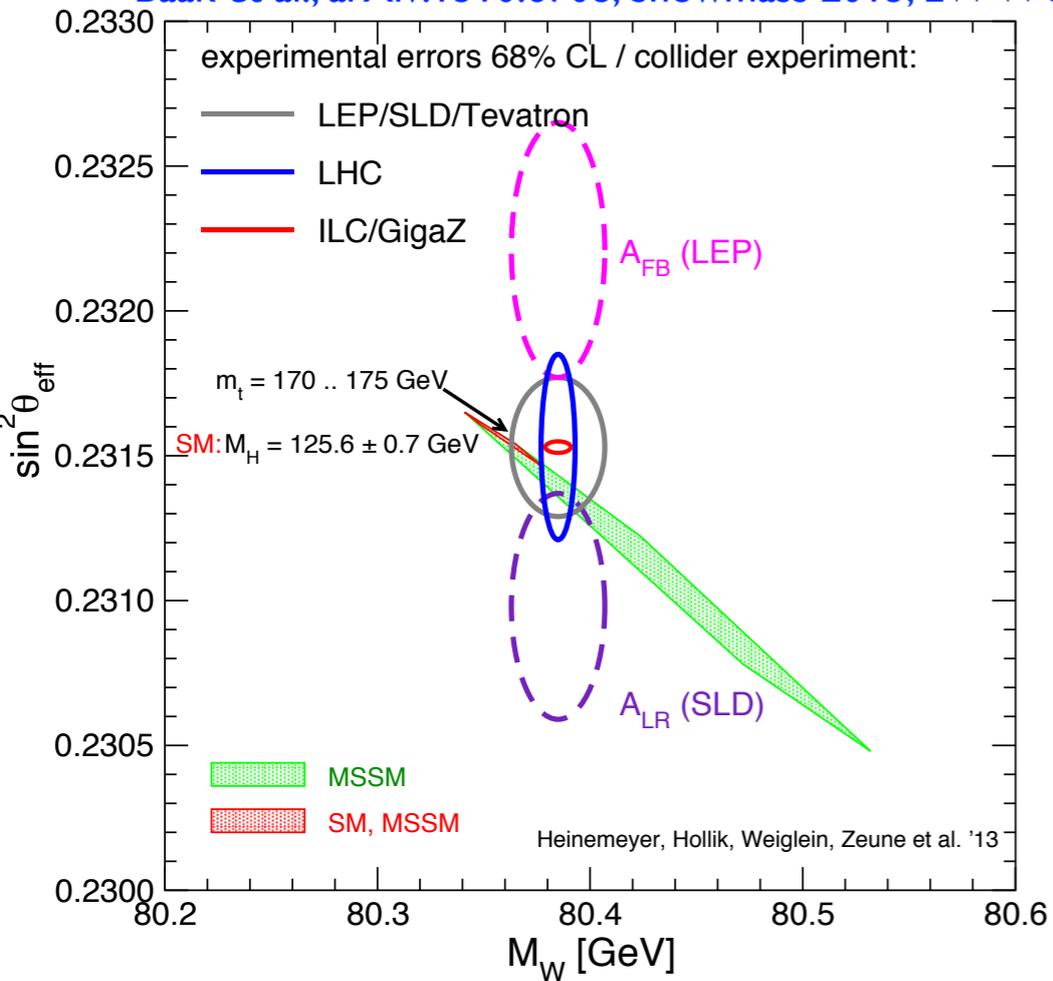
44%

46%

- the semi-leptonic channel was “golden” because
 - only two jets \rightarrow unique **invariant mass** reconstruction
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- LEP2 measurement mostly limited by statistics

Relevance of new high-precision measurement of EW parameters

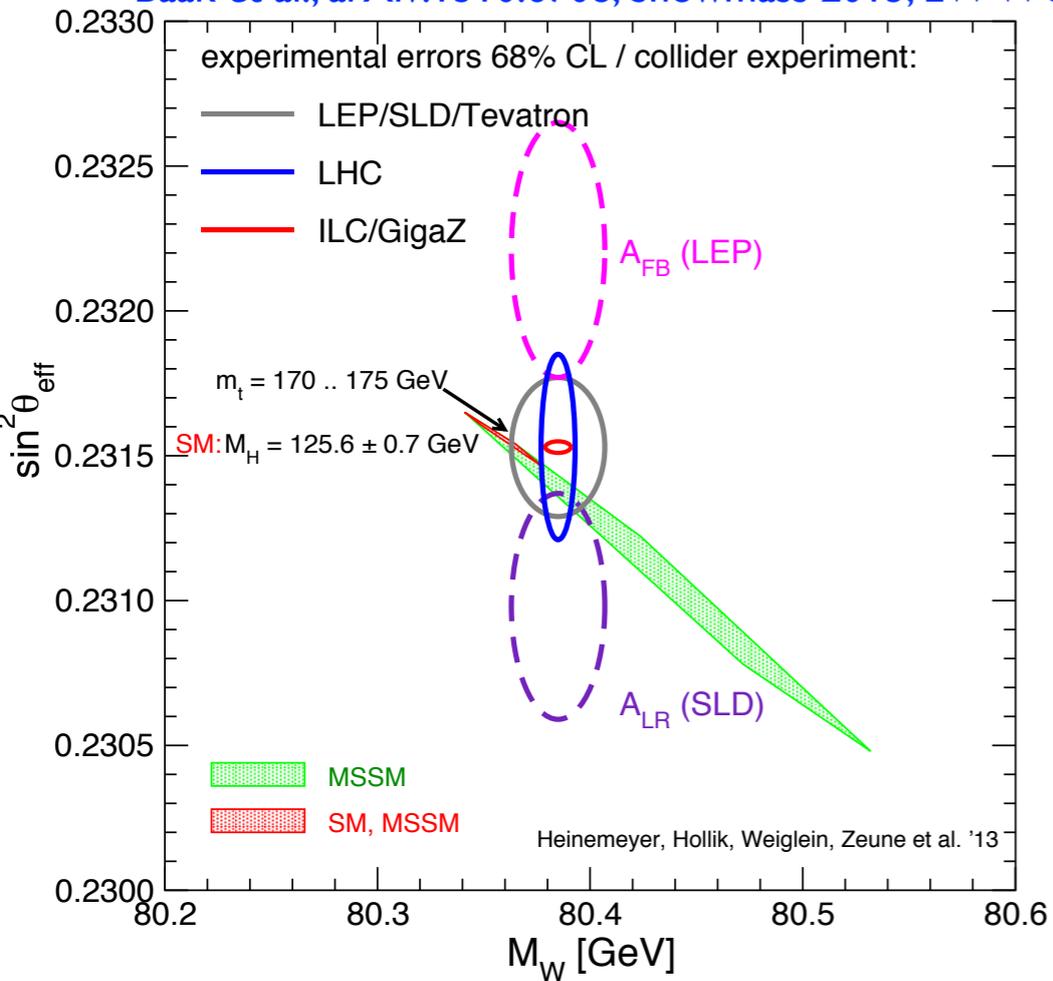
Baak et al., arXiv:1310.6708, Snowmass 2013, EW WG



The precision measurement of M_W and $\sin^2 \theta_{\text{eff}}$ with an error of 5 MeV and 0.00021 (formidable challenges!) would offer a very stringent **test of the SM likelihood**

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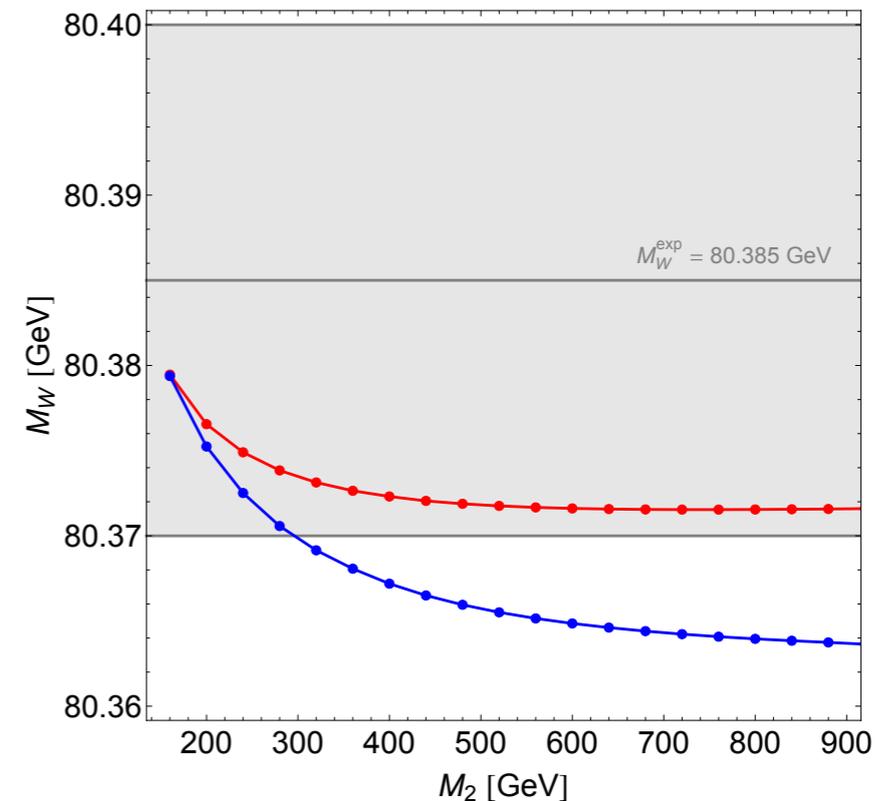


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In the case a BSM particle had been discovered a very precise M_W value would offer **a strongly discriminating tool about the mass spectra in BSM models**

different dependence on the neutralino mass M_2 of the M_W prediction in the **MSSM** and **NMSSM**

O. Stål, G. Weiglein, L. Zeune, arXiv:1506.07465

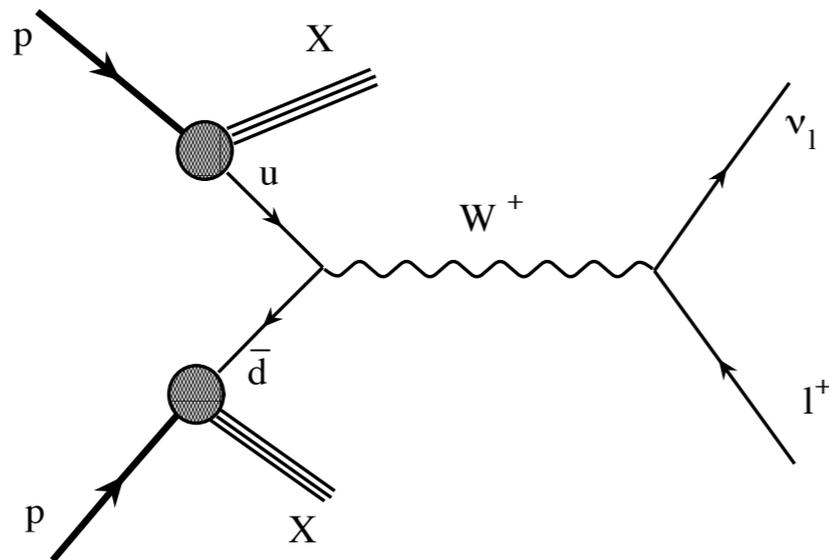


The present

M_W and $\sin^2\theta$ determination at hadron colliders

The Drell-Yan process

- production of a pair of leptons with high transverse (missing) momentum in hadron-hadron collisions (either collider or fixed target experiments)
 - along the beam axis large soft (i.e. non-perturbative) hadronic activity
- the large lepton momenta in the plane transverse to the beam axis guarantee a clean signature
the perturbative regime of QCD



- important probe of QCD dynamics:

- 1) the lepton pair recoils in the transverse plane against initial state QCD radiation
- 2) the lepton-pair rapidity is directly connected to the proton PDFs

these d.o.f. are two of the mostly relevant (limiting) factors for precision EW measurements

MW determination at hadron colliders

In charged-current DY, it is **NOT** possible to reconstruct the lepton-pair invariant mass

Full reconstruction is possible (but not easy) only in the transverse plane

MW extracted from the study of the **shape** of the $M_T, p_{T_lep}, E_{T_miss}$ distributions in CC-DY thanks to the **jacobian peak** that enhances the sensitivity to MW

$$\frac{d}{dp_{\perp}^2} \rightarrow \frac{2}{s} \frac{1}{\sqrt{1 - 4p_{\perp}^2/s}} \frac{d}{d \cos \theta}$$

MW determination at hadron colliders

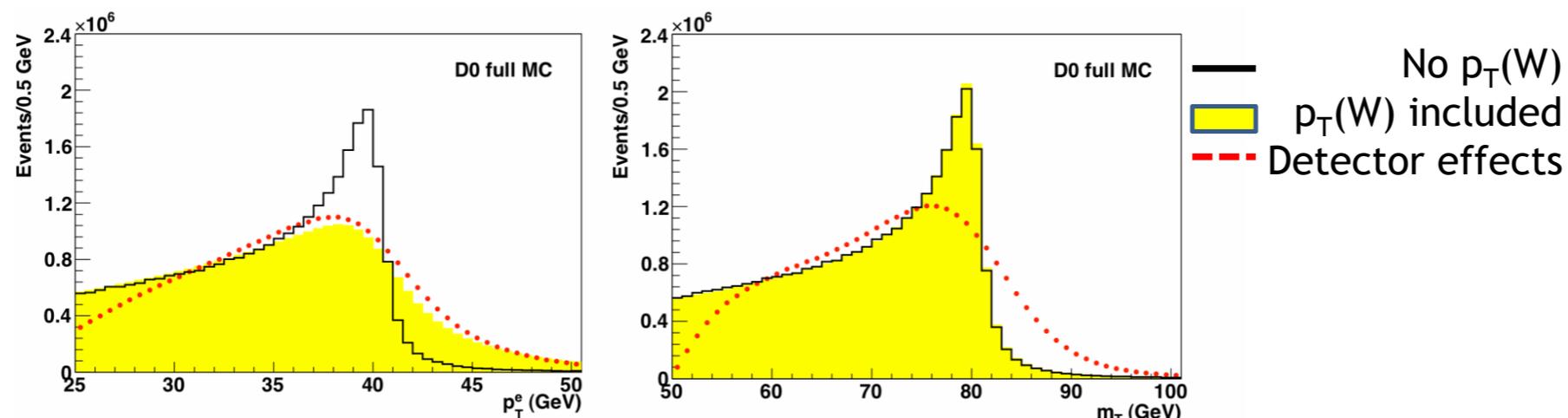
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problems are due to

- the smearing of the distributions due to difficult neutrino reconstruction
- strong sensitivity to the modelling of initial state QCD effects



MW determination at hadron colliders

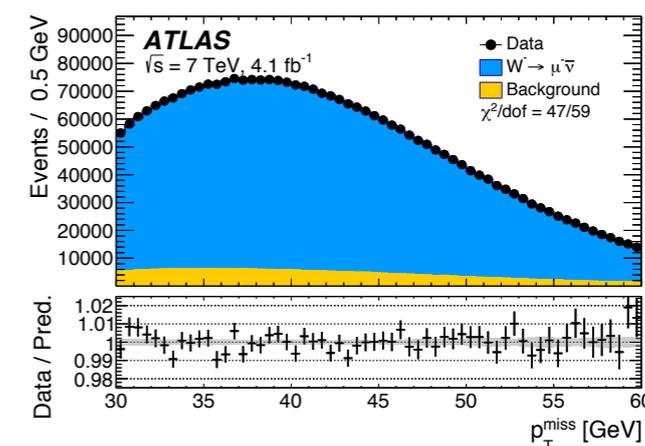
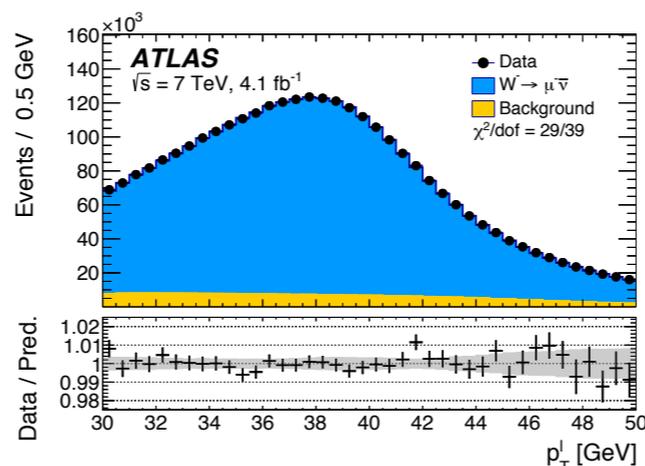
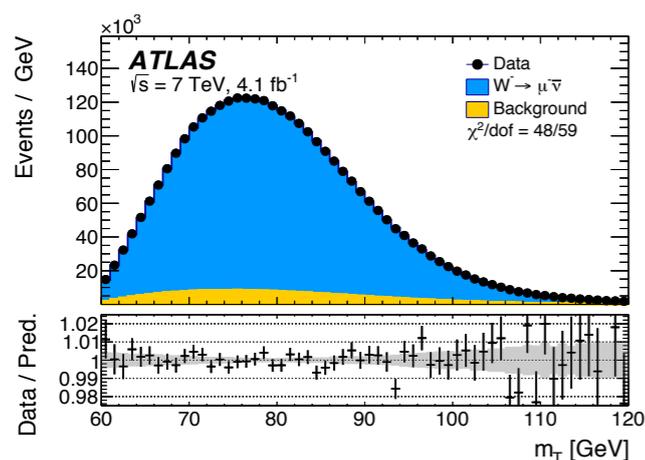
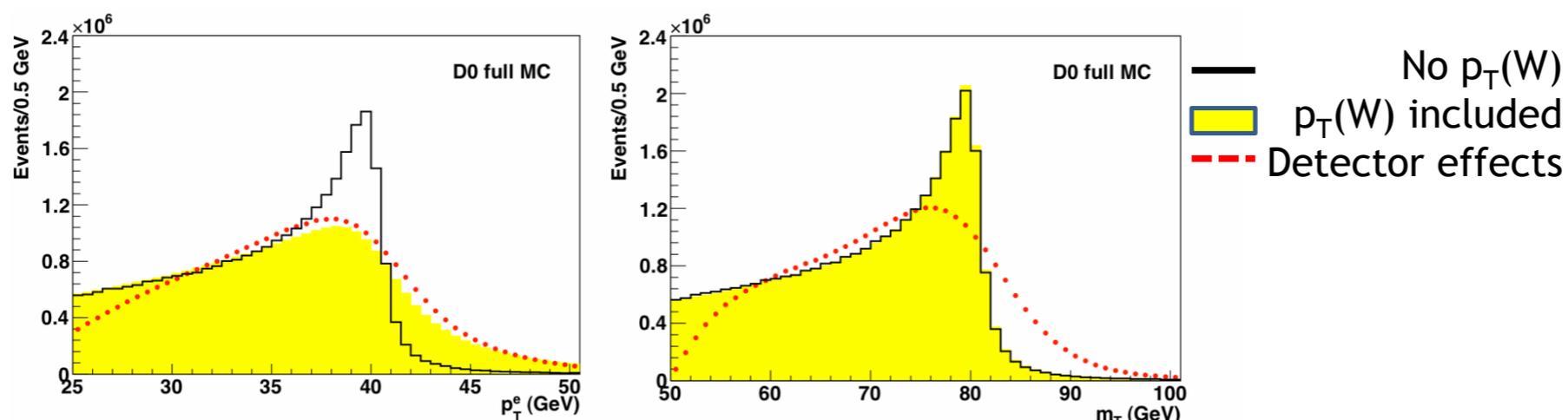
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$$m_W = 80369.5 \pm 6.8 \text{ MeV(stat.)} \pm 10.6 \text{ MeV(exp. syst.)} \pm 13.6 \text{ MeV(mod. syst.)}$$

$$= 80369.5 \pm 18.5 \text{ MeV,}$$

error dominated by modelling systematics

Weak mixing angle determination at hadron colliders (I)

invariant mass Forward-Backward asymmetry
in neutral-current DY

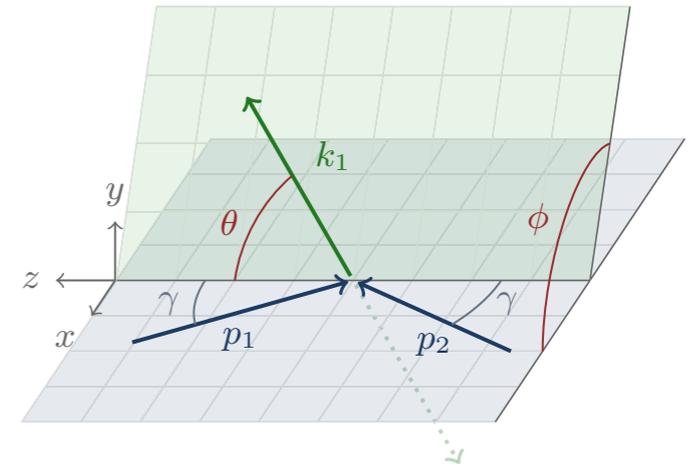
$$A_{FB}(M_{l+l-}) = \frac{F(M_{l+l-}) - B(M_{l+l-})}{F(M_{l+l-}) + B(M_{l+l-})}$$

$$F(M_{l+l-}) = \int_0^1 \frac{d\sigma}{d\cos\theta^*} d\cos\theta^* \quad B(M_{l+l-}) = \int_{-1}^0 \frac{d\sigma}{d\cos\theta^*} d\cos\theta^*$$

scattering angle defined in the Collins-Soper frame → “Forward” (“Backward”)

$$\cos\theta^* = f \frac{2}{M(l+l-)\sqrt{M^2(l+l-) + p_t^2(l+l-)}} [p^+(l^-)p^-(l^+) - p^-(l^-)p^+(l^+)]$$

$$p^\pm = \frac{1}{\sqrt{2}}(E \pm p_z) \quad f = \frac{|p_z(l+l-)|}{p_z(l+l-)}$$



we would like to appreciate parity violation like at LEP,

observing an asymmetry with respect to the direction of the incoming particle

→ it is not possible because we have both q-qbar and qbar-q annihilation processes

→ at the LHC the symmetry of the collider (p-p) removes one possible preferred direction

but...

Weak mixing angle determination at hadron colliders (I)

...but

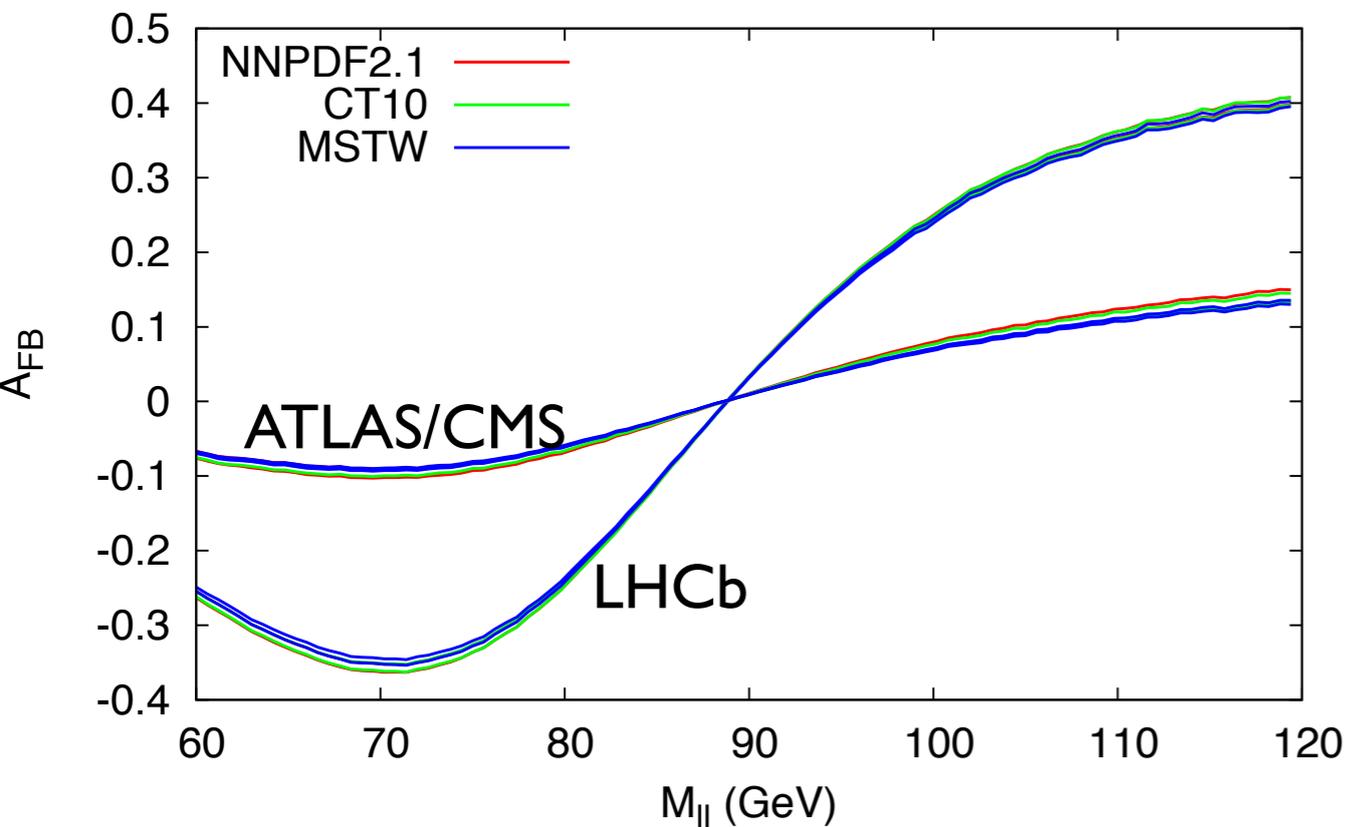
at a given lepton-pair rapidity Y

q - q bar and q bar- q have different weight because of the PDFs \Rightarrow do not cancel each other

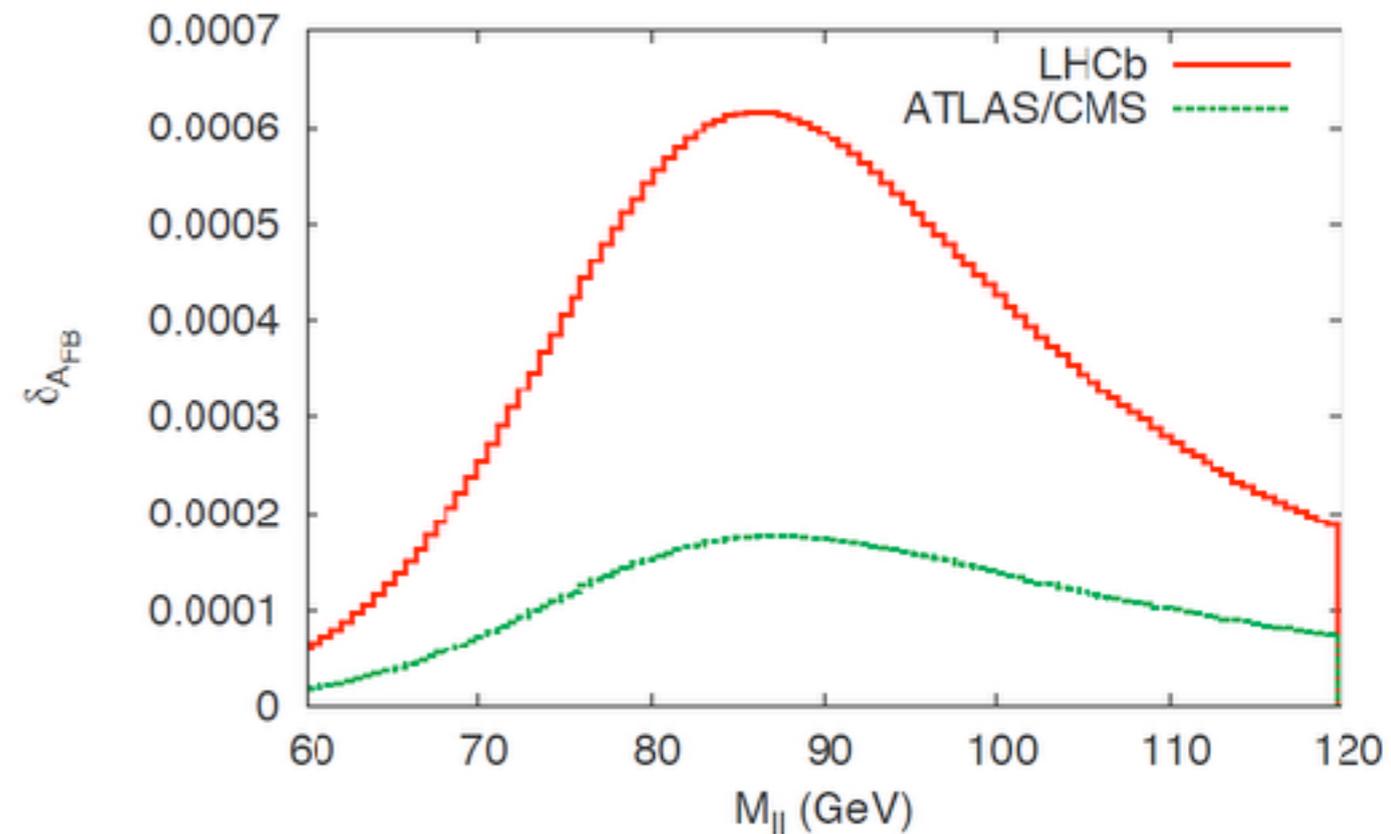
the parton luminosity unbalance is due to the different x dependence of the valence and sea quarks

AFB is more pronounced at large Y , e.g. at LHCb

ATLAS/CMS and LHCb, AFB, Born, LHC 7 TeV



NNPDF2.1, AFB, Born, LHC 7 TeV



$$\delta A_{FB} = A_{FB}(\sin^2 \theta_W + \delta \sin^2 \theta_W) - A_{FB}(\sin^2 \theta_W - \delta \sin^2 \theta_W)$$

$$\delta \sin^2 \theta_W = 0.0001$$

close to MZ : small AFB but good sensitivity to the weak mixing angle

away from MZ : large AFB, no sensitivity to the weak mixing angle, possible effects from new Z' ...

away from MZ: “model independent” parameterisation of AFB is not possible, we compute it in the SM

AFB probes a PDF weighted combination of up, down and leptonic effective angles

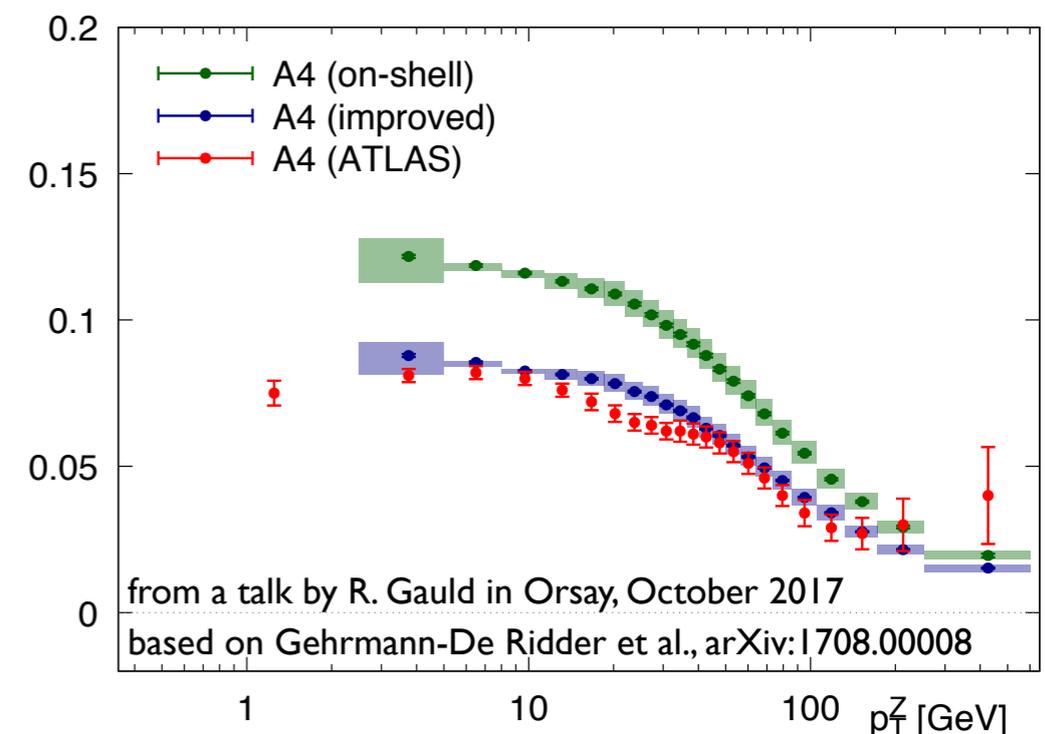
Weak mixing angle determination at hadron colliders (II)

The Drell-Yan process, including QCD corrections only, can be described as the production of a vector boson and its subsequent decay

The leptons kinematics can be described in terms of angular coefficients A_i , which carry the information about the initial state QCD dynamics (pt, invariant mass, rapidity of the lepton pair)

$$\frac{d\sigma}{d^4q d\cos\theta d\phi} = \frac{3}{16\pi} \frac{d\sigma^{unpol}}{d^4q} \left\{ \begin{array}{l} \text{normalised by } d\sigma(\text{unpol}) \\ \text{even under parity} \\ \text{odd under parity} \\ \text{start at } \mathcal{O}(\alpha_s^2) \end{array} \right. \left\{ 1 + \cos^2\theta + A_0(1 - \cos^2\theta) + A_1 \sin(2\theta) \cos\phi + \frac{1}{2} A_2 \sin^2\theta \cos(2\phi) + A_3 \sin\theta \cos\phi + A_4 \cos\theta + A_5 \sin^2\theta \sin(2\phi) + A_6 \sin(2\theta) \sin\phi + A_7 \sin\theta \sin\phi \right\}$$

The coefficients A_3 and A_4 describe the contribution of the cross section odd under parity and in turn are sensitive to the weak mixing angle.



Observables and pseudo-observables, template fitting

Observables quantities accessible via **counting experiments**
cross sections and asymmetries

Pseudo-Observables quantities that are functions of the cross section and asymmetries
require a model to be properly defined

- the Z boson mass at LEP as the pole of the Breit-Wigner resonance factor
- the W mass at hadron collider as the fitting parameter of a template fit procedure
the templates are computed in a model (typically the SM)

Template fit

- several histograms describing a differential distribution are computed with the highest available theoretical accuracy and degree of realism in the detector simulation letting the fit parameter (e.g. MW) vary in a range
- the histogram that best describes the data selects the preferred, i.e. measured, MW value
- the result of the fit depends on the **hypotheses used to compute the templates**
these hypotheses **should be treated as theoretical systematic errors**
- more accurate calculations, properly implemented in Monte Carlo event generators are needed to reduce this systematic error

Pseudo-observables and EW input schemes

To fit a pseudo-observable, the templates are computed in a given model (e.g. SM)

Every quantity (observable and pseudo-observable) predicted e.g. in the SM is expressed in terms of the lagrangian input parameters

The lagrangian inputs are the only parameters which can be varied in the template fitting procedure

example: when using $(\alpha, G_\mu, M_Z, M_H)$ as inputs,
then M_W is a prediction and can NOT be used as fitting parameter

The G_μ scheme is commonly used at hadron colliders and treats (G_μ, M_W, M_Z, M_H) as inputs

in this scheme we can fit M_W

$\sin^2\theta_w$ is a derived quantity, which can be computed for a given M_W value

Tools for Drell-Yan simulations: inclusive lepton-pair production

i.e. how we compute the templates

Codes including fixed-order results

FEWZ	NNLO QCD (W) NNLO QCD + NLO EW (Z)
DYNNLO	NNLO QCD
MCFM	NLO QCD
WZGRAD	NLO EW
SANC	NLO QCD + NLO EW
RADY	NLO QCD + NLO EW

Codes including the matching of fixed- and all-order results

DYRes	NNLO+NNLL QCD
ResBos (RadISH)	(N)NLO+NNLL QCD NNLO+N3LL
MC@NLO	NLO+PS QCD
POWHEG	NLO+PS QCD
DYNNLOPS	NNLO+PS QCD
Sherpa	NNLO+PS QCD
HORACE	NLO-EW + QED-PS
POWHEG	NLO-(QCD+EW) + (QCD+QED)-PS

Technical comparison and systematic **classification** of higher orders in Alioli et al., arXiv:1606.02330

Exact $O(\alpha\alpha_s)$ results are not available,

bulk of these contributions included in approximated way in simulation codes

Coupling expansion and logarithmic enhancements (I)

$$\alpha_s(m_Z) \simeq 0.118, \quad \alpha_{em}(m_Z) \simeq 0.0078 \quad \frac{\alpha_s(m_Z)}{\alpha_{em}(m_Z)} \simeq 15.1 \quad \frac{\alpha_s^2(m_Z)}{\alpha_{em}(m_Z)} \simeq 1.8$$

Coupling strength \rightarrow first classification (NNLO-QCD \sim NLO-EW) is **appropriate** for those observables that do not receive any logarithmically enhanced correction

$$\begin{aligned} \sigma_{tot} = & \sigma_0 + \alpha_s \sigma_{\alpha_s} + \alpha_s^2 \sigma_{\alpha_s^2} + \dots && \text{QCD} \\ & + \alpha \sigma_{\alpha} + \alpha^2 \sigma_{\alpha^2} + \dots && \text{EW} \\ & + \alpha \alpha_s \sigma_{\alpha \alpha_s} + \alpha \alpha_s^2 \sigma_{\alpha \alpha_s^2} + \dots && \text{mixed QCDxEW} \end{aligned}$$

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At differential level, **in specific phase-space corners, a plain coupling constant expansion is inadequate**

\rightarrow fixed-order EW corrections can become as large as (or even bigger than) QCD corrections because of log-enhanced factors

\rightarrow log-enhanced corrections have to be resummed to all orders, if possible,

analytically or via Parton Shower, rearranging the structure of the perturbative expansion

In presence of resummed expressions, the QCDxEW interplay entangles classes of corrections to all orders in α_s and α

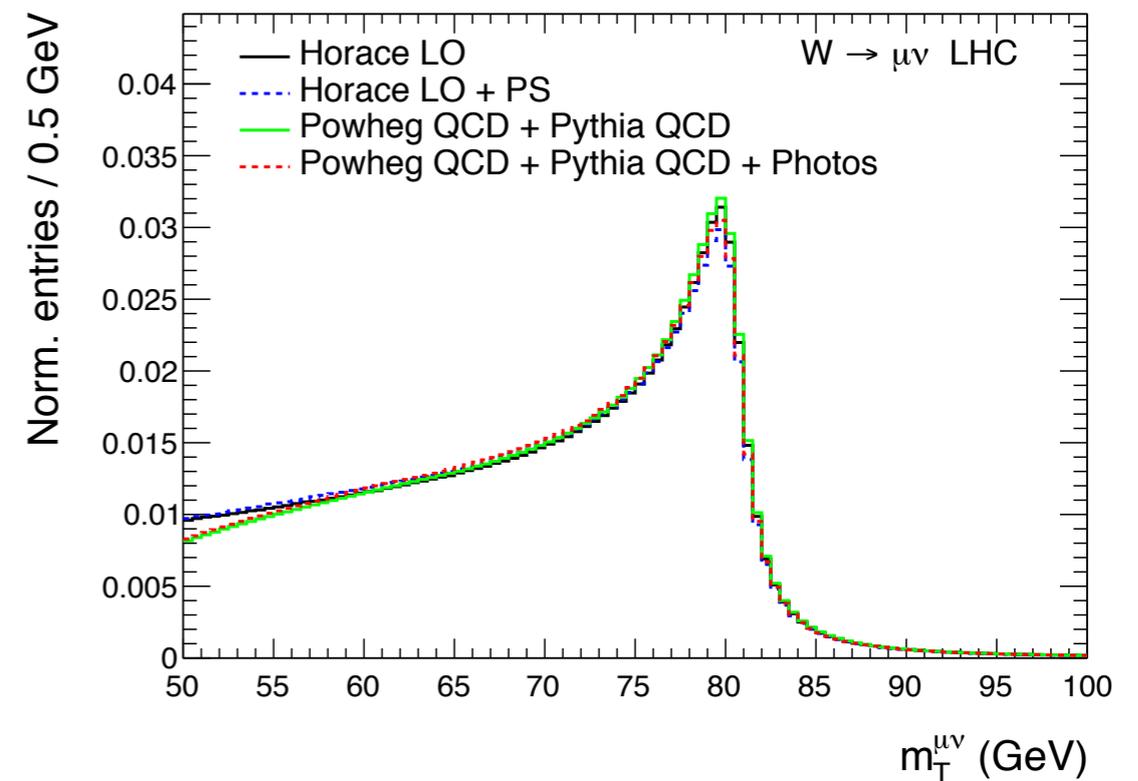
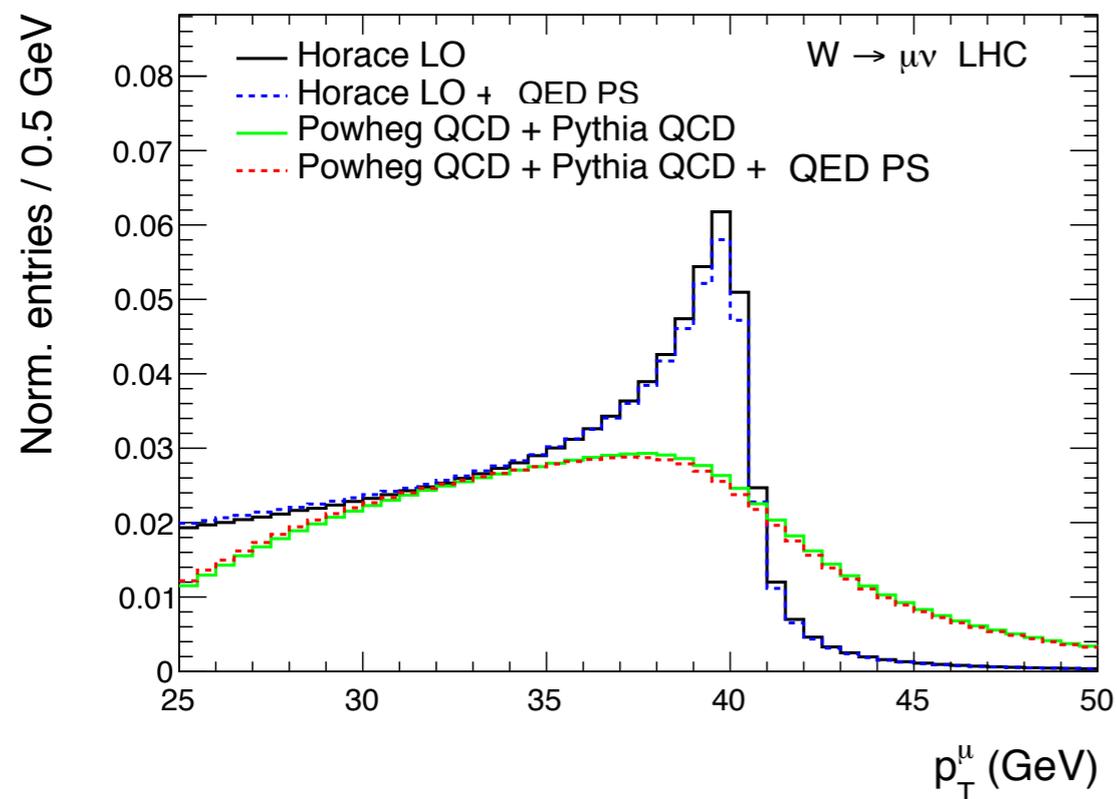
The perturbative convergence depends on the presence of all allowed partonic channel that may contribute to a given final state.

Coupling expansion and logarithmic enhancements (2): QCD

- QCD ISR is responsible for large logarithmic corrections $\sim L_{\text{QCD}} \stackrel{\text{def}}{=} \log(\text{ptV} / m_V)$ for a final state V which need to be resummed to all orders, e.g. via QCD Parton Shower

two examples in DY: single lepton p_T needs resummation, fixed-order QCD prediction meaningless
lepton-pair transverse mass is very mildly affected when integrating over QCD

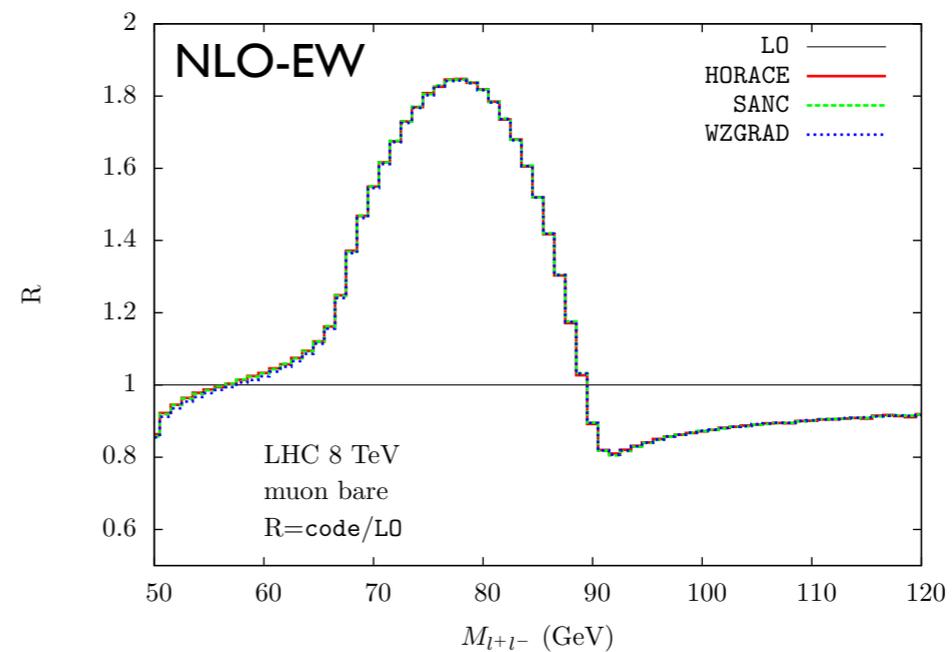
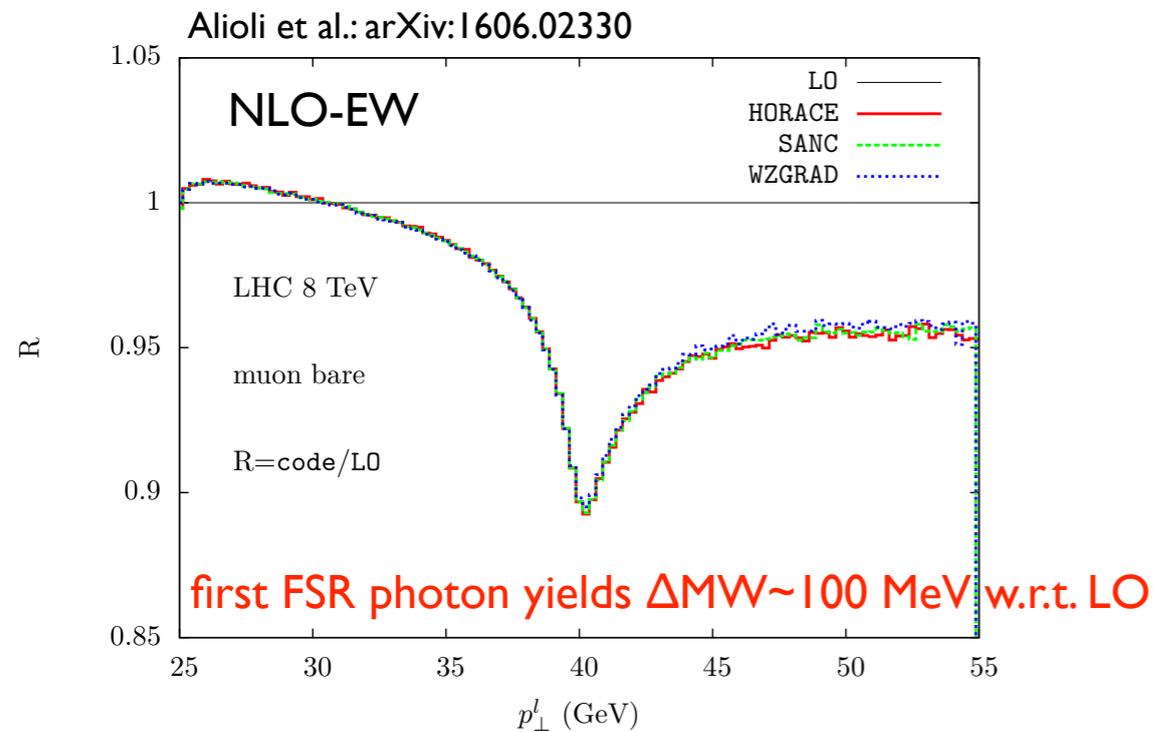
Carlioni Calame, Chiesa, Martinez, Montagna, Nicosini, Piccinini, AV, arXiv:1612.02841



single lepton p_T : sensible lowest order approximation offered by LO+PS

Coupling expansion and logarithmic enhancements (2): EW

- QED FSR is responsible for the energy/momentum loss of final state particles, e.g. leptons, yielding large collinear logarithmic corrections $\sim L_{\text{QED}} \stackrel{\text{def}}{=} \log(\hat{s}/m_f^2)$ which strongly affect the value of reconstructed observables

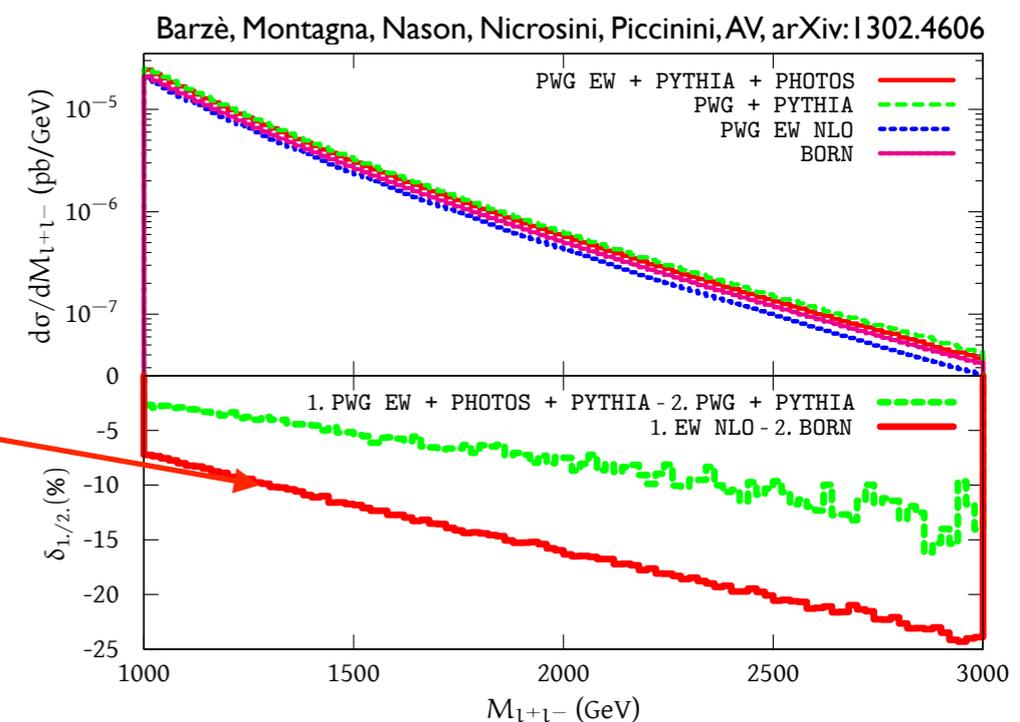


- EW Sudakov logs appear in virtual correction with W or Z bosons when one kinematical invariant becomes large \Rightarrow large negative corrections

in the high-energy limit the EW Sudakov logs

factorize as (Denner, Pozzorini, hep-ph/0010201)

$$\delta \mathcal{M}_{\text{LL+NLL}}^{1\text{-loop}} = \frac{\alpha}{4\pi} \sum_{k=1}^n \left\{ \frac{1}{2} \sum_{l \neq k} \sum_{a=\gamma, Z, W^\pm} I^a(k) I^{\bar{a}}(l) \ln^2 \frac{\hat{s}_{kl}}{M^2} + \gamma^{\text{ew}}(k) \ln \frac{\hat{s}}{M^2} \right\} \mathcal{M}_0$$



Which are the most relevant **radiative corrections** and **uncertainties** for precision EW measurements?

- ▷ QCD modelling
- ▷ EW and mixed QCDxEW effects
- ▷ PDF uncertainties

Which are the most relevant **radiative corrections** and **uncertainties** for precision EW measurements?

- ▷ QCD modelling
- ▷ EW and mixed QCDxEW effects
- ▷ PDF uncertainties

Disclaimer: no final table with uncertainties on M_W and $\sin^2\theta_w$
partially because the calculation of some higher-order effect is missing
mostly because the complexity of the modelling has not yet been solved
i.e. **we do not know explicitly all the correlations between NC and CC DY**

QCD modelling

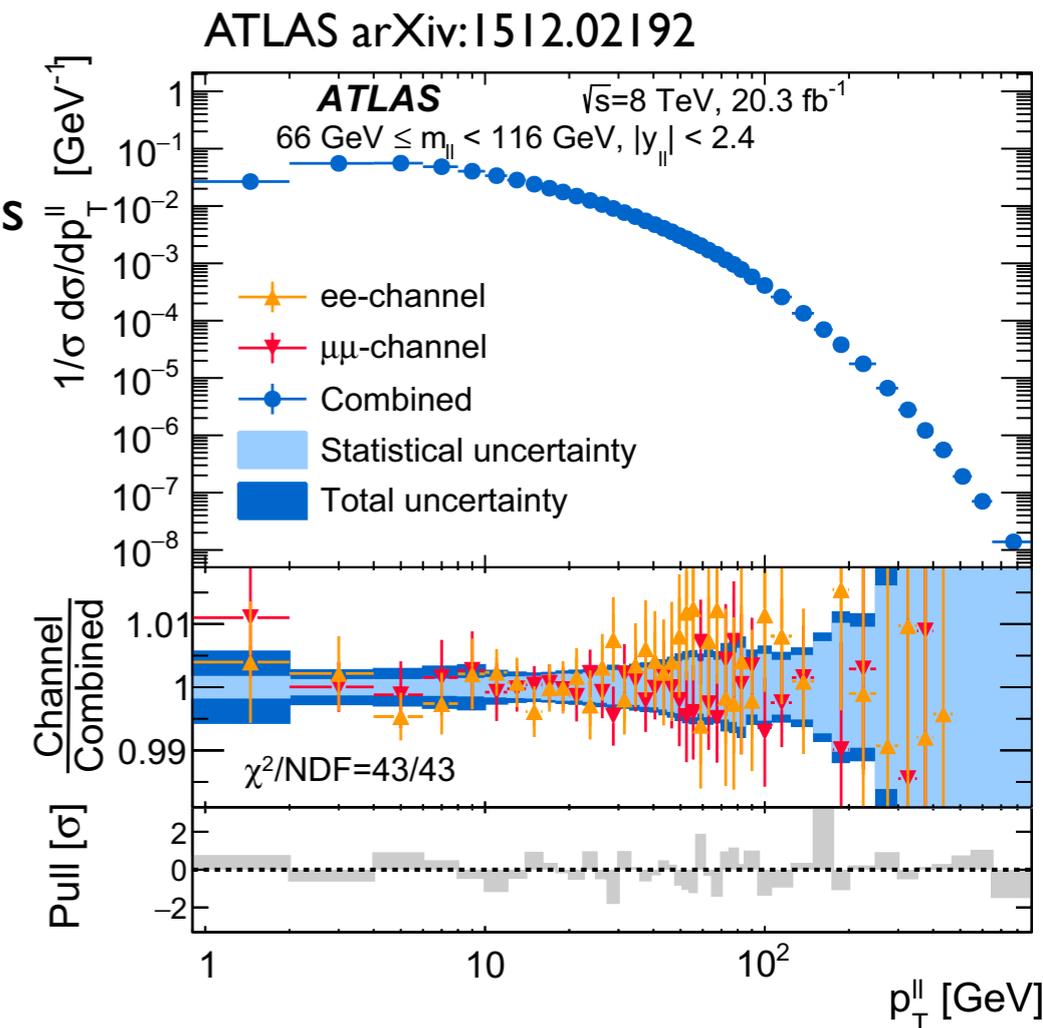
Lepton-pair transverse momentum distribution

- A crucial role in precision EW measurements (MW in particular) is played by the pt_Z distribution
 - ▷ MW is extracted from the fit to the pt_{lep} , MT and ET_{miss} distributions
 - ▷ the pt_{lep} and pt_ν determination strongly depends on a precise control of the pt_W distribution
 - ▷ a precise pt_W measurement is not available → we rely on pt_Z and extrapolate from it
 - ▷ pt_Z is used to calibrate 1) detectors 2) Monte Carlo tools (Parton Shower at low- pt_Z)

Lepton-pair transverse momentum distribution

- A crucial role in precision EW measurements (MW in particular) is played by the p_T^Z distribution
 - ▷ MW is extracted from the fit to the p_{T_lep} , MT and ET_miss distributions
 - ▷ the p_{T_lep} and p_{T_V} determination strongly depends on a precise control of the p_{TW} distribution
 - ▷ a precise p_{TW} measurement is not available → we rely on p_{TZ} and extrapolate from it
 - ▷ p_{TZ} is used to calibrate 1) detectors 2) Monte Carlo tools (Parton Shower at low- p_{TZ})

- The excellent measurement of p_{TZ} by the LHC collaborations is
 - ▷ a powerful benchmark for the calibration phase
 - ▷ a formidable challenge to the theoretical predictions



Lepton-pair transverse momentum distribution

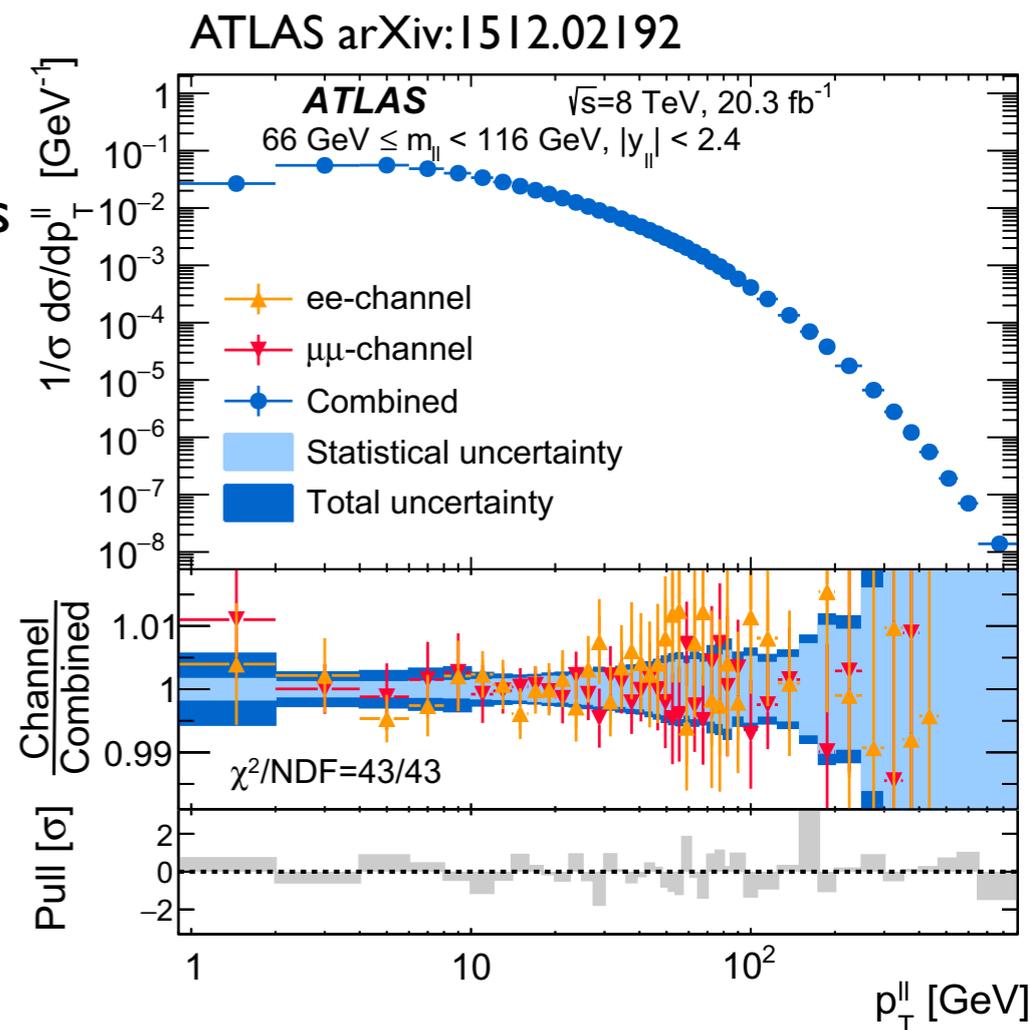
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- The excellent measurement of p_T^Z by the LHC collaborations is
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⇒ Do the best theoretical predictions describe the p_T^Z data (absolute and normalised distributions) ?

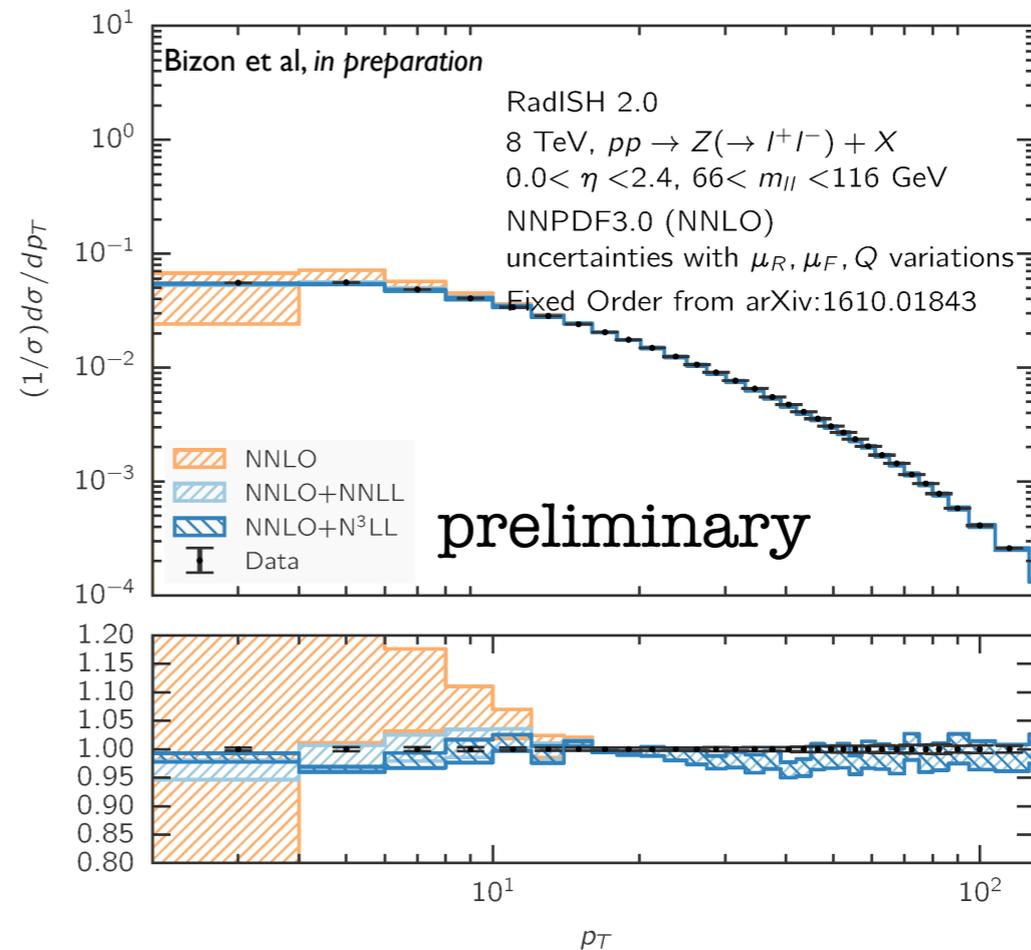
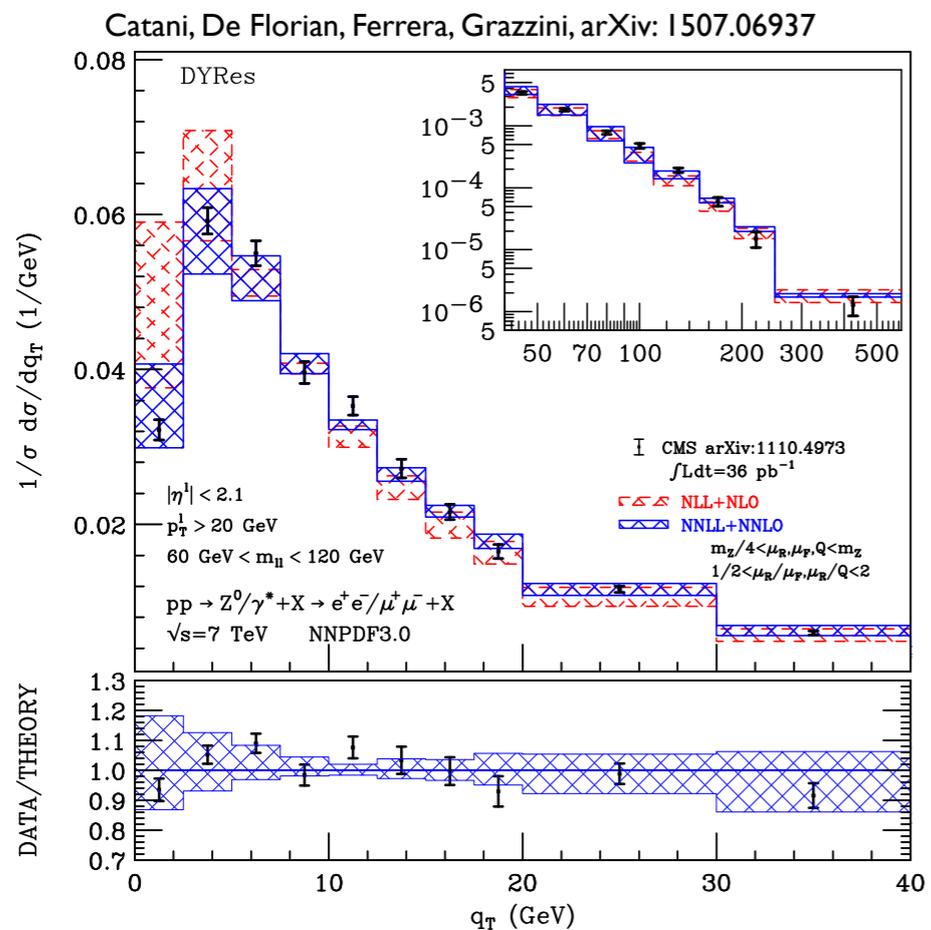
⇒ What is the accuracy of the available simulation tools?

⇒ For the p_T^W/p_T^Z ratio, can we predict its central value? and its theoretical uncertainty?



Lepton-pair transverse momentum distribution

- The precision of the theoretical prediction for $p_T Z$, in dedicated calculations/tools, depends on:
 - ▷ logarithmic accuracy (N3LL) in the $\log(p_T Z/MZ)$ resummation → relevant at small $p_T Z$
 - ▷ fixed-order accuracy (NNLO) in the $p_T Z$ spectrum → relevant at large $p_T Z$
 - ▷ matching prescription → relevant at intermediate $p_T Z$



shape of the distribution

- The progress in analytical resummation does not easily directly apply to the MW measurement.

Lepton-pair transverse momentum distribution

Matched shower Monte Carlo event generators (cfr. DYNNLOPS, or SHERPA+UN2LOPS)

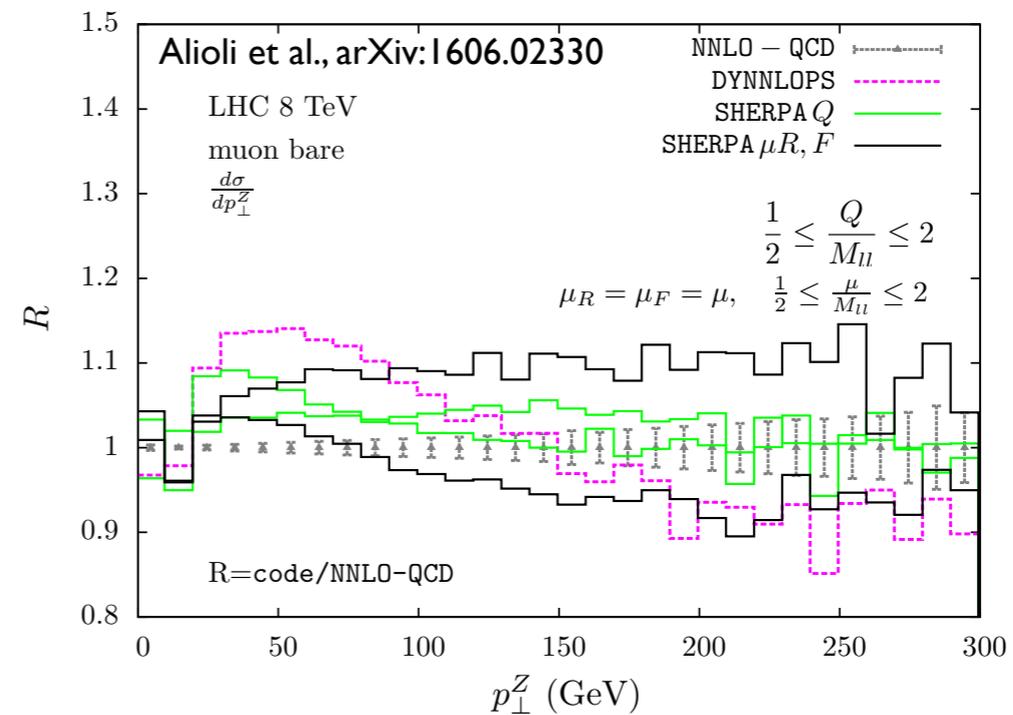
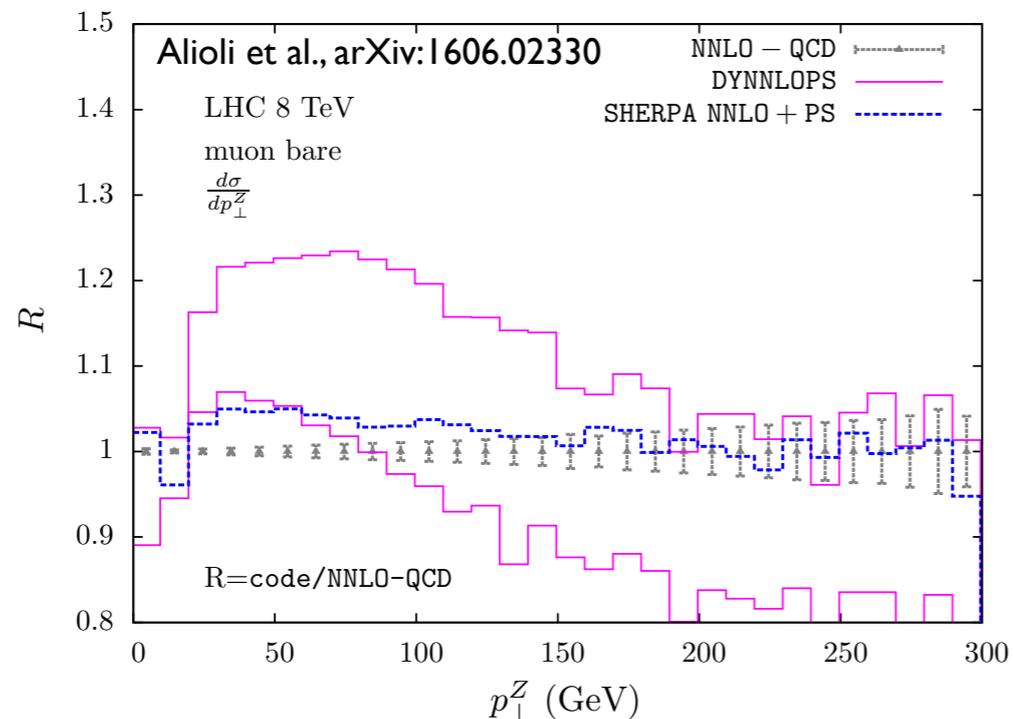
- ▷ are fully exclusive, general purpose tools; crucial in the experimental analyses
- ▷ accuracy: NNLO-QCD on the inclusive observables, NLO-QCD at large pt_Z , (N)LL at small pt_Z
- ▷ require a tuning of the Parton Shower parameters (non perturbative effects at low pt_Z)
- ▷ are affected by non-negligible matching uncertainties (recipe, matching param's dependence)
- ▷ depend on several algorithmic details (e.g. Parton-Shower phase space)

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Comparison of the DYNNLOPS and SHERPA+UN2LOPS scale uncertainty bands

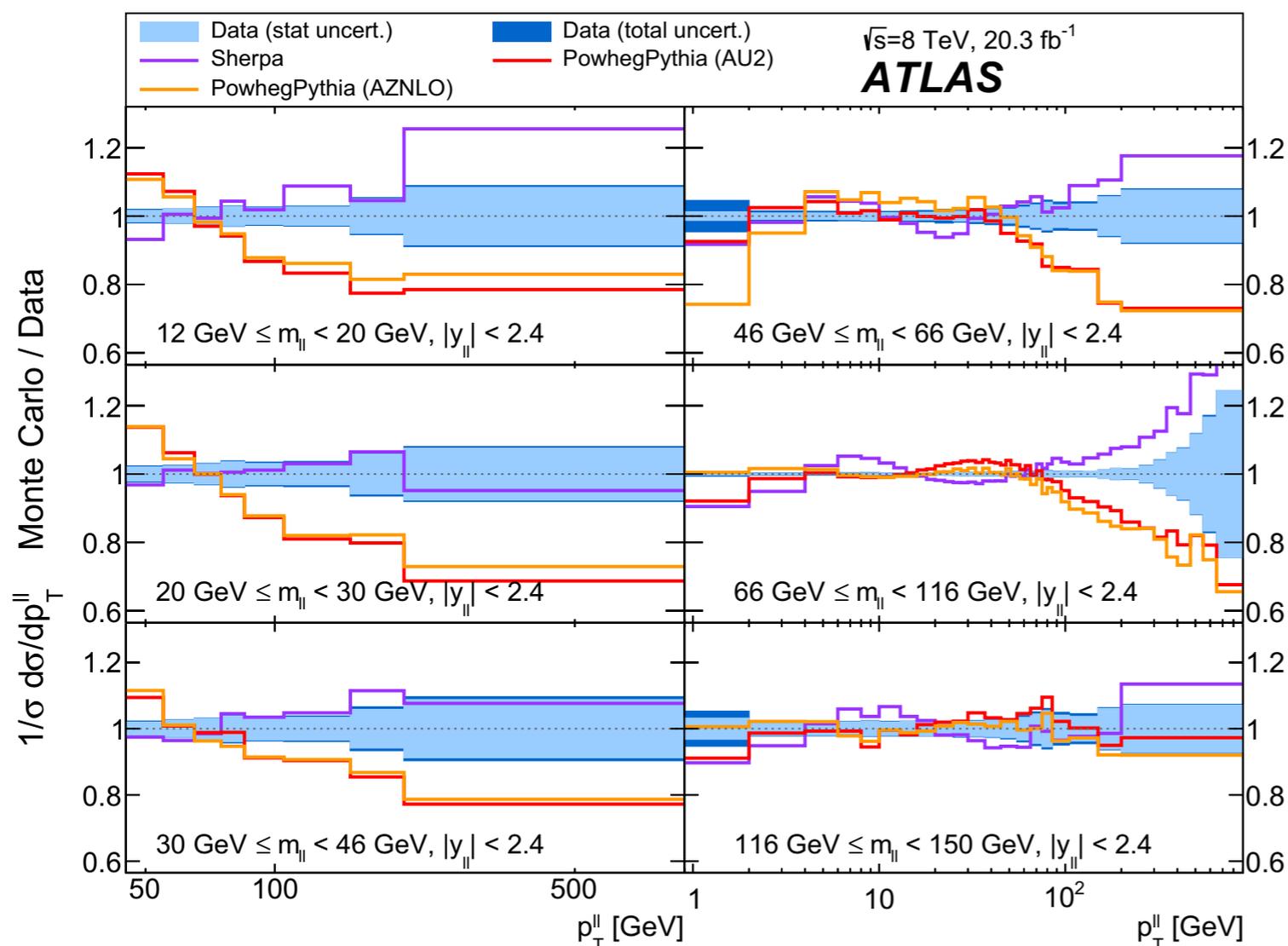


comparison
of absolute
distributions

Lepton-pair transverse momentum distribution

Matched shower Monte Carlo event generators (cfr. DYNNLOPS, or SHERPA+UN2LOPS)

- ▷ are fully exclusive, general purpose tools; crucial in the experimental analyses
- ▷ accuracy: NNLO-QCD on the inclusive observables, NLO-QCD at large $p_{T,Z}$, (N)LL at small $p_{T,Z}$
- ▷ require a tuning of the Parton Shower parameters (non perturbative effects at low $p_{T,Z}$)
- ▷ are affected by non-negligible matching uncertainties (recipe, matching param's dependence)
- ▷ depend on several algorithmic details (e.g. Parton-Shower phase space)



tuning of the Parton Shower
in the combination POWHEG + Pythia 8
at the Z resonance

extrapolation to different
invariant mass windows

Lepton-pair transverse momentum distribution: Z to W extrapolation

The parameters (intrinsic k_t , α_s in the PS, hadronization) derived from the calibration on pt_Z are used in the CC-DY studies to determine M_W .

- ▷ are these param's 1) universal (i.e. flavour independent)
2) scale independent ($M_W \neq M_Z$!) ?

- ▷ the flavour structure of CC-DY and NC-DY is different

CC-DY: $u \bar{d}, c \bar{s}, \dots \rightarrow W^+ \rightarrow l^+ \nu$

NC-DY: $u \bar{u}, d \bar{d}, c \bar{c}, s \bar{s}, b \bar{b}, \dots \rightarrow \gamma^*/Z \rightarrow l^+ l^-$

how do the different flavour structures affect (Z to W)?

e.g. is the effect of scale variations different (different DGLAP evolution) ?

role of heavy quarks?

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role of heavy quarks?

For a realistic estimate of the QCD theoretical uncertainties, we need:

- ▷ an improved description of all the elements of difference between CC-DY and NC-DY
- ▷ a good control over the correlation between Z and W w.r.t. the different sources of uncertainty
any uncertainty estimate (PDFs, scale variations, etc.) based on CC-DY alone
leads to a (huge) overestimate of the uncertainty

The M_W measurement studies the M_Z - M_W interdependence; it's not an absolute measurement of M_W

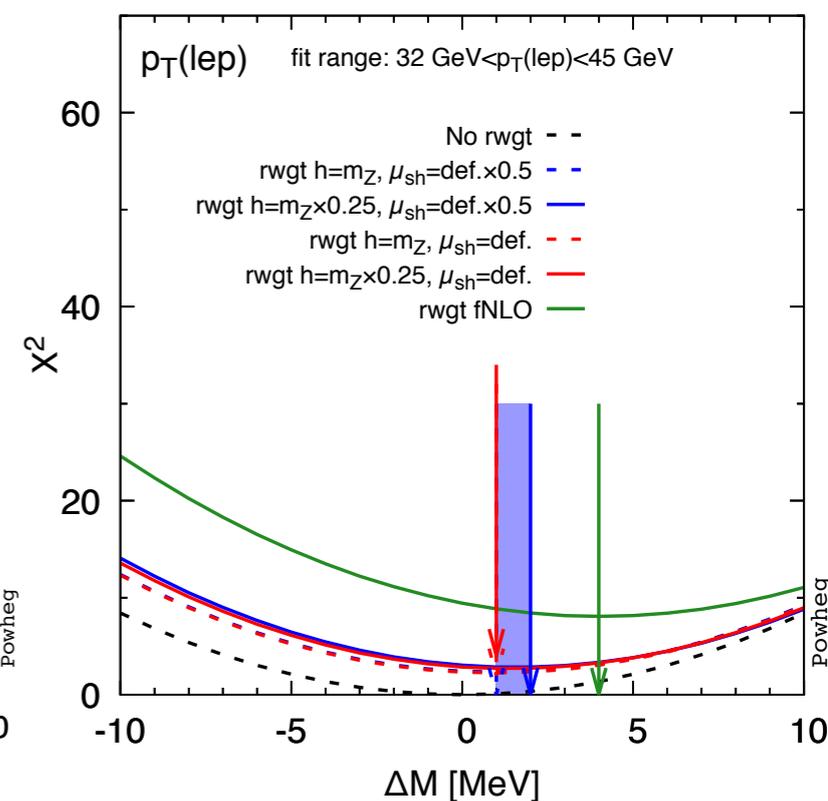
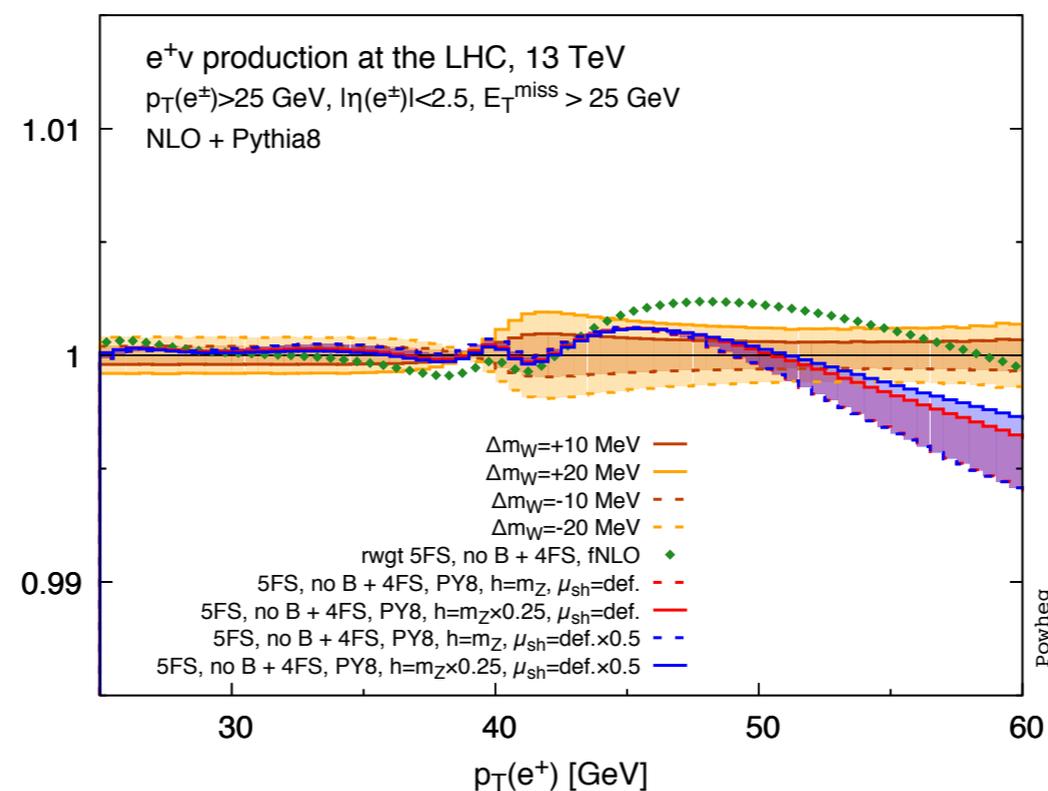
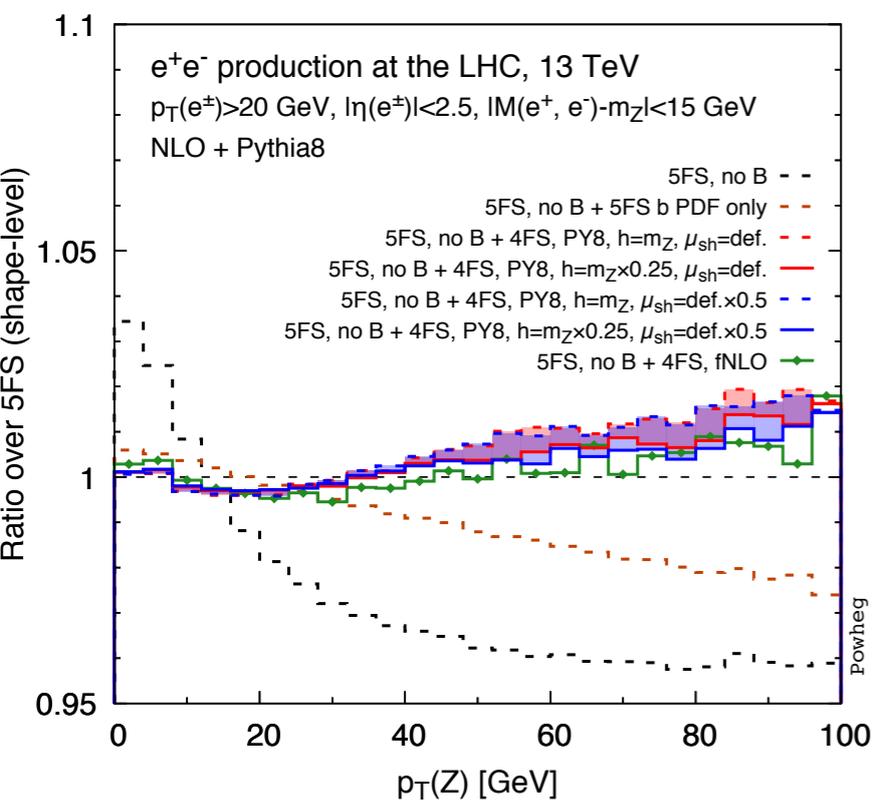
Improving the description of the bottom contributions to $p_T Z$

preliminary results, work in collaboration with Bagnaschi, Maltoni, Zaro

the standard MW analysis is based on massless 5FS description of Drell-Yan processes

→ which would be the impact of a description of the bottom as a massive quark? 1) on $p_T Z$; 2) on MW

- ▷ a combination of 4FS and 5FS results improves the $p_T Z$ description, in the region $p_T Z \sim 0-25$ GeV
- ▷ the tuning of the Parton Shower would be affected by this improved NC-DY description
 - the CC-DY simulation would be in turn modified
- ▷ the change in the CC-DY templates would lead to a different value of MW extracted from the data



the impact on MW is small but not vanishing!

EW and mixed QCDxEW effects

Overall status of EW and QCDxEW corrections

EW corrections affect the final state lepton distributions

leading effects are mostly due to QED-FSR

after the matching with a full NLO-EW all first order subleading effects included

residual subleading second order effects are tiny

QCDxEW the QCD modelling modulates the EW effects

the bulk of the effects is included in the simulations (with some caveats)

a sound estimate of the associated uncertainties is not available (NNLO QCDxEW frontier)

Impact of EW corrections on the MW determination

Carloni Calame, Chiesa, Martinez, Montagna, Nicrosini, Piccinini, AV, arXiv:1612.02841

Templates accuracy: LO		M_W shifts (MeV)			
		$W^+ \rightarrow \mu^+ \nu$		$W^+ \rightarrow e^+ \nu$	
Pseudodata accuracy		M_T	p_T^ℓ	M_T	p_T^ℓ
1	HORACE only FSR-LL at $\mathcal{O}(\alpha)$	-94±1	-104±1	-204±1	-230±2
2	HORACE FSR-LL	-89±1	-97±1	-179±1	-195±1
3	HORACE NLO-EW with QED shower	-90±1	-94±1	-177±1	-190±2
4	HORACE FSR-LL + Pairs	-94±1	-102±1	-182±2	-199±1
5	PHOTOS FSR-LL	-92±1	-100±2	-182±1	-199±2

estimate of shifts based on a template fit approach

- 1 · the first final state photon dominates the correction on MW
- 2 · multiple photon radiation has still a sizeable $\mathcal{O}(-10\%)$ effect
- 3 · subleading QED and weak effects are negligible, $\mathcal{O}(1-2 \text{ MeV})$
- 4 · additional pair production is not negligible, with a shift ranging from 3 to 5 MeV
- 5 · the agreement between PHOTOS and HORACE QED-PS is acceptable, given the subleading differences of the two implementations

Combination of QCD and EW corrections in DY simulation tools (I)

- Fixed-order tools:

additive combination of exact $O(\alpha_s)$, $O(\alpha_s^2)$ and $O(\alpha)$ corrections (e.g. FEWZ)

$$\sigma = \sigma_0 (1 + \delta\alpha_s + \delta\alpha_s^2 + \delta\alpha + \dots)$$

possibility to arrange terms in factorized combinations

$$\sigma = \sigma_0 (1 + \delta\alpha_s + \dots) (1 + \delta\alpha)$$

→ estimate of size $O(\alpha\alpha_s)$ terms

WARNING: kinematics plays a very important role

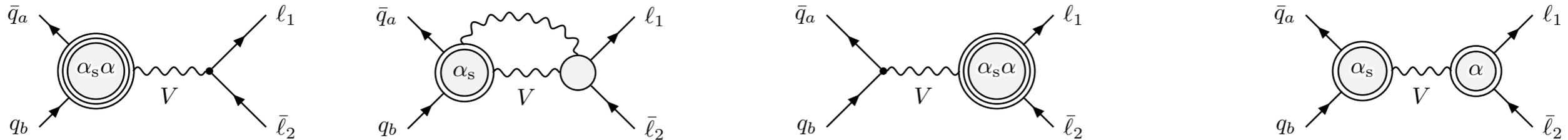
multiplying integrated corrections factors \neq **convoluting** fully differential corrections

$O(\alpha\alpha_s)$ corrections in pole approximation

S. Dittmaier, A. Huss, C. Schwinn, Nucl.Phys.B885 (2014) 318, Nucl.Phys.B904 (2016) 216

- The pole approximation provides a good description of the W (Z) region, as it has already been checked for the pure NLO-EW corrections

- At $O(\alpha\alpha_s)$ there are 4 groups of contributions



- The last group yields the dominant correction to the process, due to factorizable corrections QCD-initial x QED-final

$$\sigma_{\text{NNLO}_{s\otimes\text{ew}}} = \sigma_{\text{NLO}_s} + \alpha \sigma_\alpha + \alpha\alpha_s \sigma_{\alpha\alpha_s}^{\text{prod}\times\text{dec}}, \quad \delta_{\alpha\alpha_s}^{\text{prod}\times\text{dec}} = \frac{\alpha\alpha_s \sigma_{\alpha\alpha_s}^{\text{prod}\times\text{dec}}}{\sigma_{\text{LO}}}, \quad \begin{array}{l} \text{full result} \\ \text{pole approximation} \end{array}$$

$$\sigma_{\text{NNLO}_{s\otimes\text{ew}}}^{\text{naive fact}} = \sigma_{\text{NLO}_s} (1 + \delta_\alpha) \quad \text{naive factorization}$$

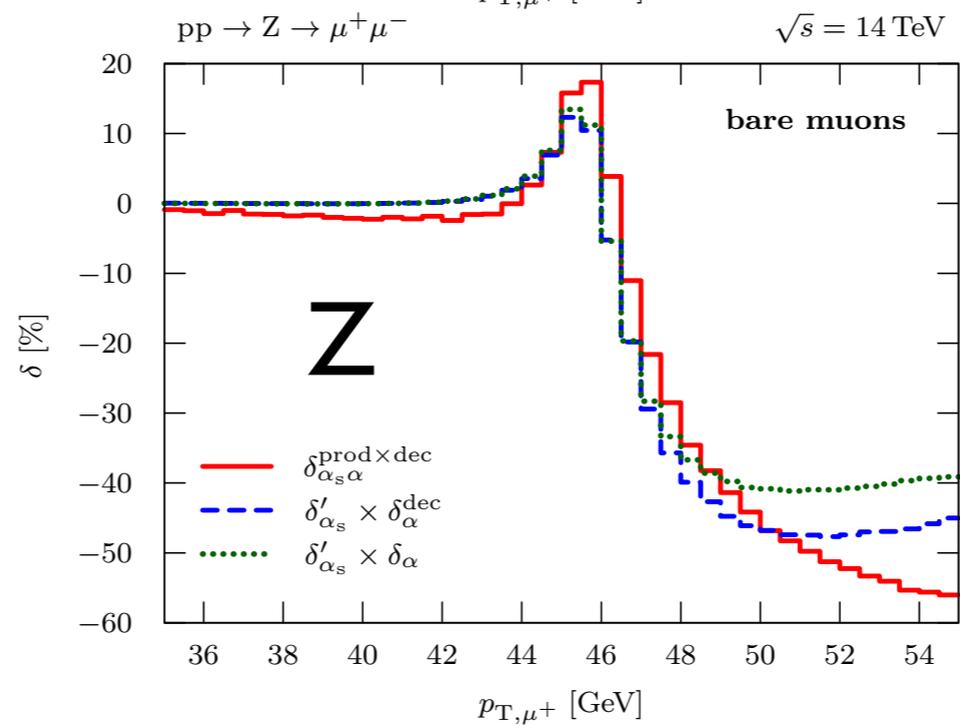
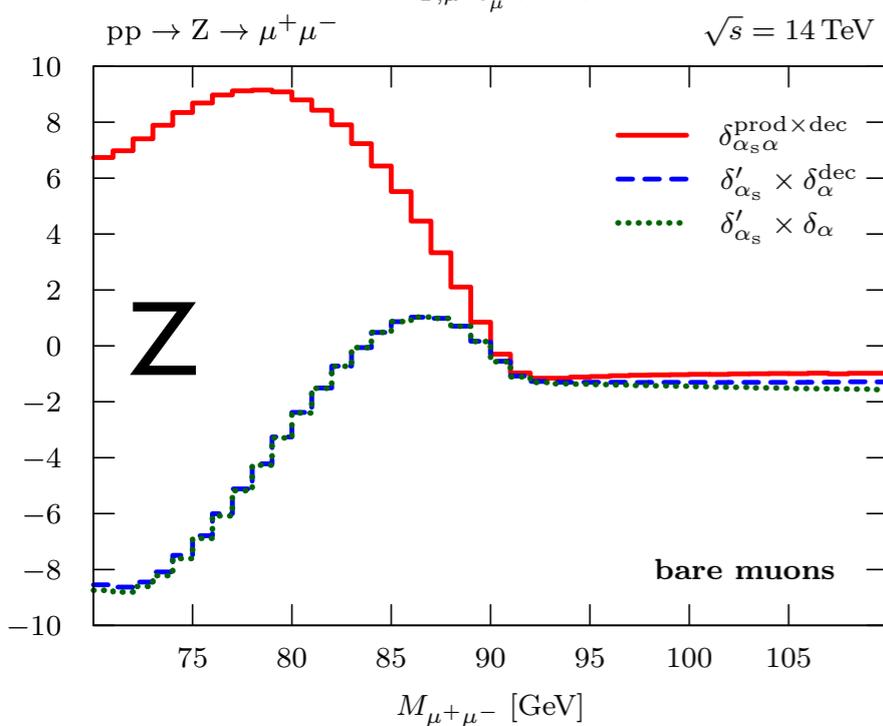
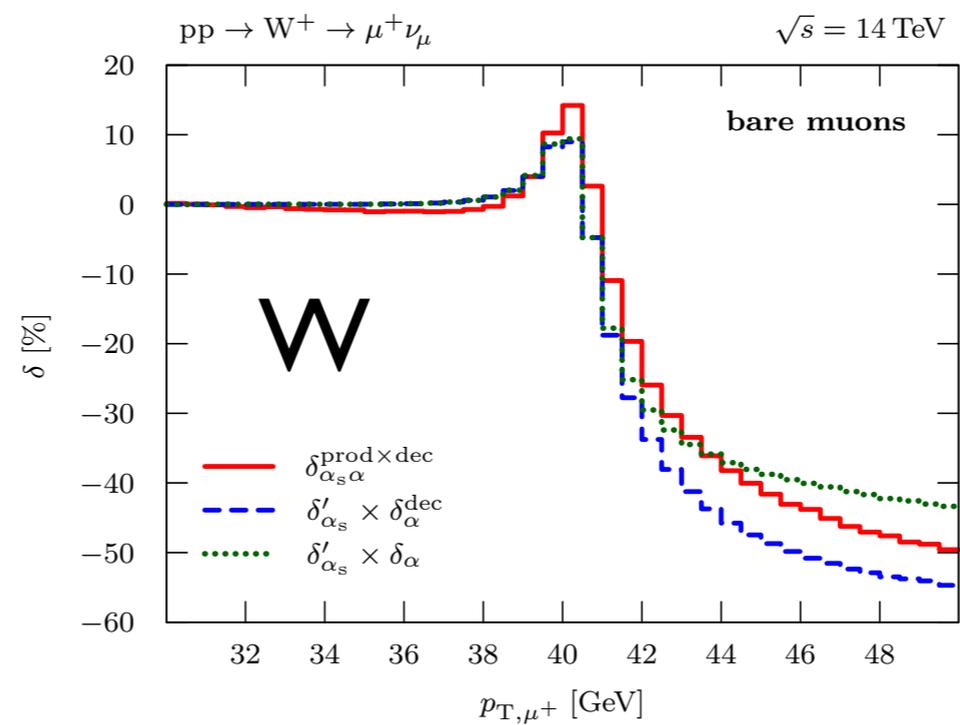
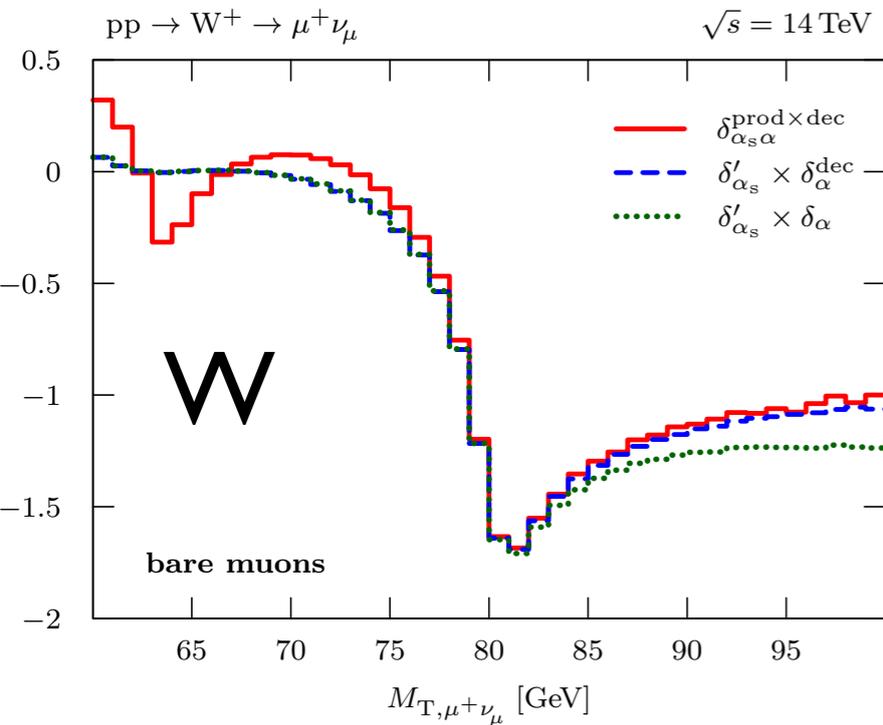
$$\frac{\sigma_{\text{NNLO}_{s\otimes\text{ew}}} - \sigma_{\text{NNLO}_{s\otimes\text{ew}}}^{\text{naive fact}}}{\sigma_{\text{LO}}} = \delta_{\alpha\alpha_s}^{\text{prod}\times\text{dec}} - \delta_\alpha \delta'_{\alpha_s} \quad \text{test of the validity of the naive factorization}$$

the δ are the inclusive correction factor

- We need to compare these results with the $O(\alpha\alpha_s)$ terms available in Monte Carlo (POWHEG)

$O(\alpha\alpha_s)$ corrections in pole approximation

S. Dittmaier, A. Huss, C. Schwinn, Nucl.Phys.B885 (2014) 318, Nucl.Phys.B904 (2016) 216



— full result
- - - pole approximation
⋯ QED-FSR
— NLO-EW

the difference between red and the others tests the naive factorization

the difference between green and blue tests the impact of weak corr. and the pole approximation

the naive factorization works nicely for the W transverse mass, at the resonance
 fails in the lepton pt case, where the kinematical interplay of photons and gluons is crucial
 fails in the Z invariant mass, where the large FSR correction is modulated by ISR QCD radiation and requires exact kinematics

$$d\sigma = \sum_{f_b} \bar{B}^{f_b}(\Phi_n) d\Phi_n \left\{ \Delta^{f_b}(\Phi_n, p_T^{min}) + \sum_{\alpha_r \in \{\alpha_r | f_b\}} \frac{[d\Phi_{rad} \theta(k_T - p_T^{min}) \Delta^{f_b}(\Phi_n, k_T) R(\Phi_{n+1})]_{\alpha_r}^{\bar{\Phi}_n^{\alpha_r} = \Phi_n}}{B^{f_b}(\Phi_n)} \right\}$$

The NLO-(QCD+EW) accuracy on the total cross section is always guaranteed by the Bbar function but

standard POWHEG algorithm: competition between QCD and QED to choose the hardest parton

→ very often a QCD parton is the hardest

→ QED radiation is left to the shower

→ **no improvement from EW matching**

solution:

the presence of a resonance allows to treat separately higher-order emissions

from the resonance (preserving its correct virtuality) → QED

from the initial state → QCD+QED-ISR

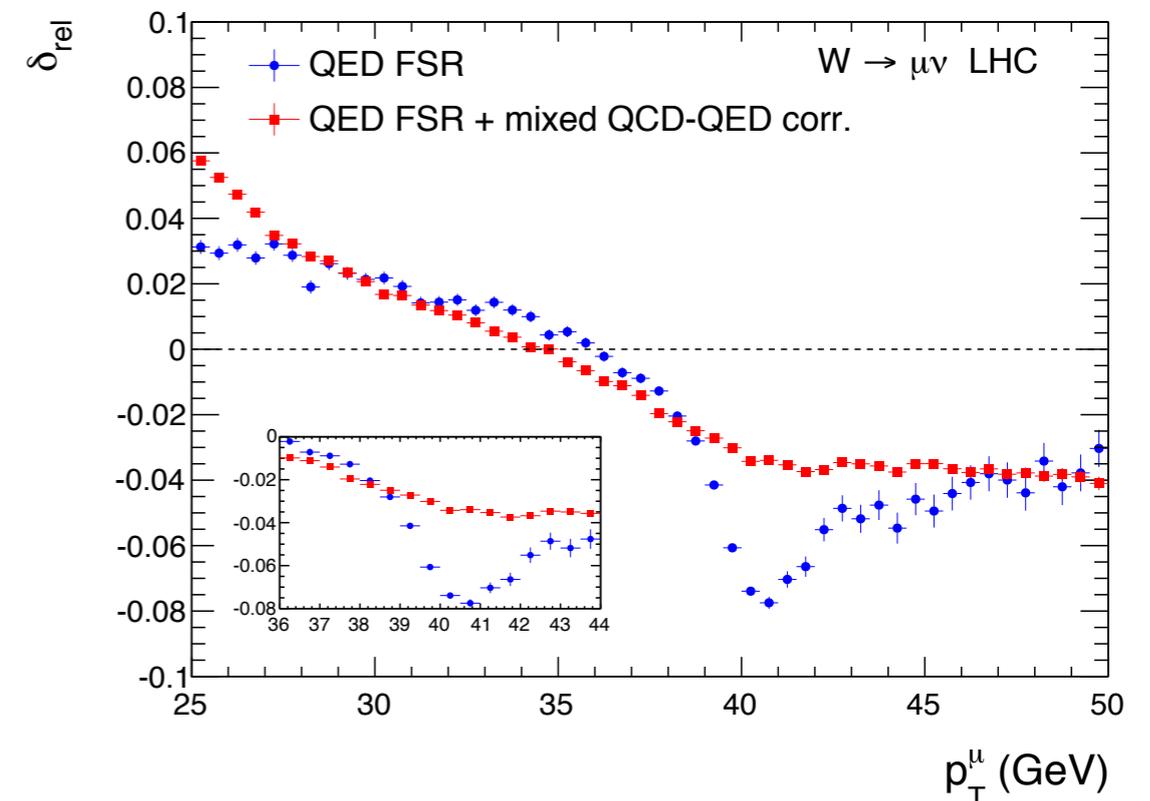
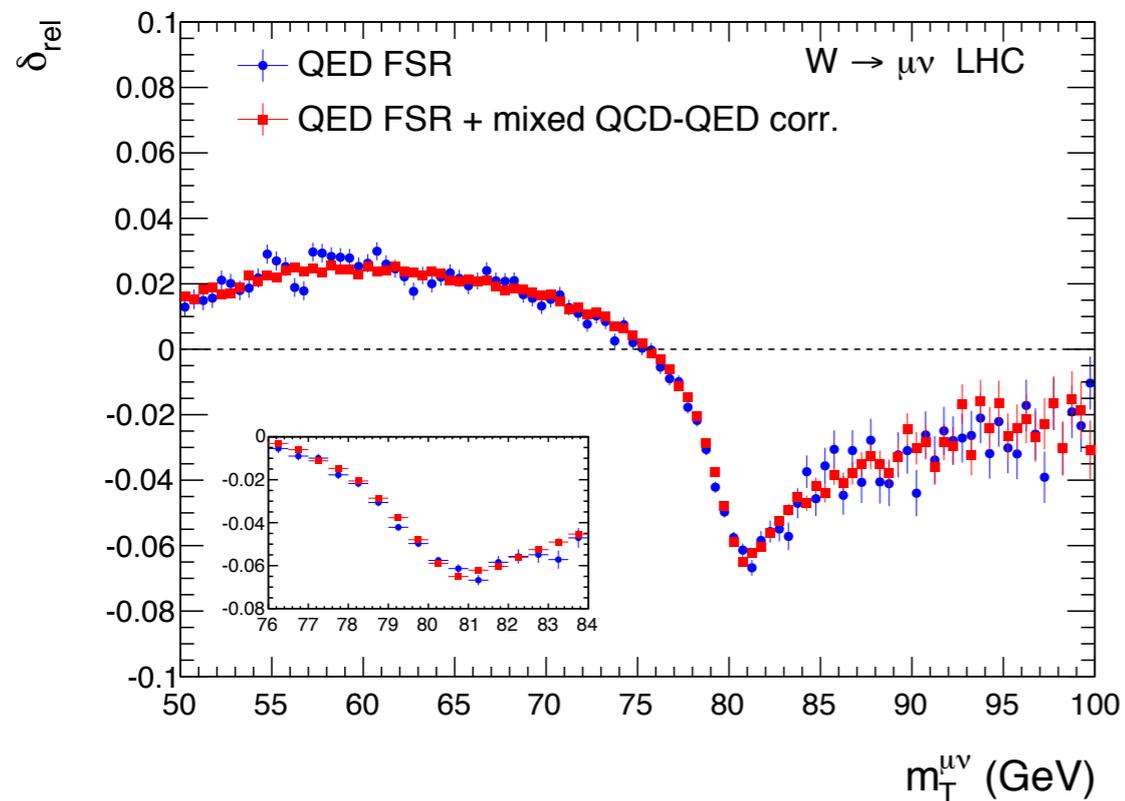
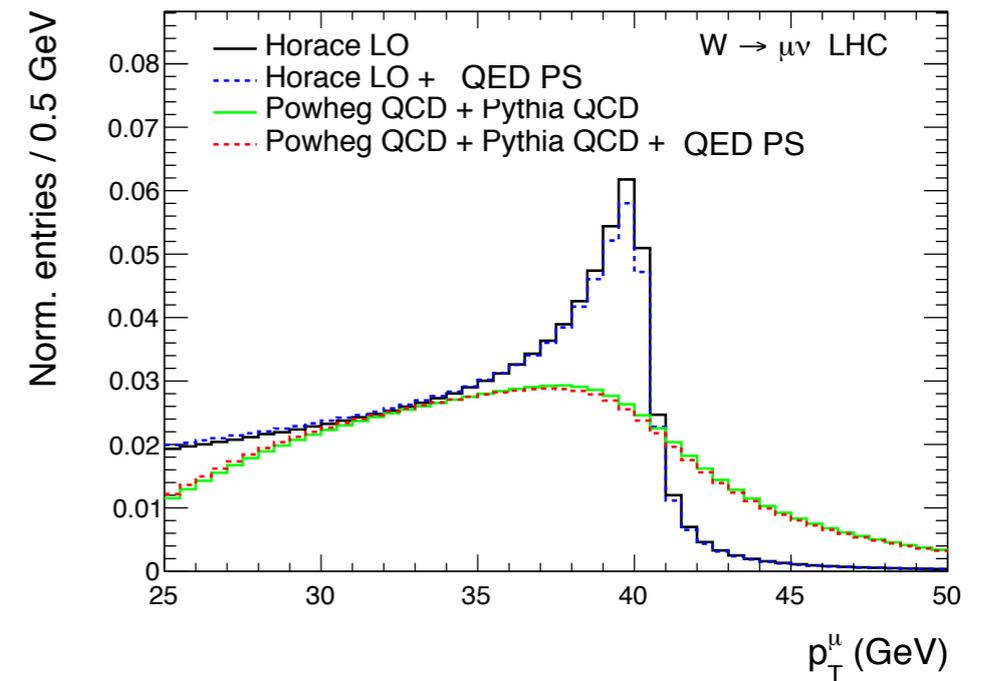
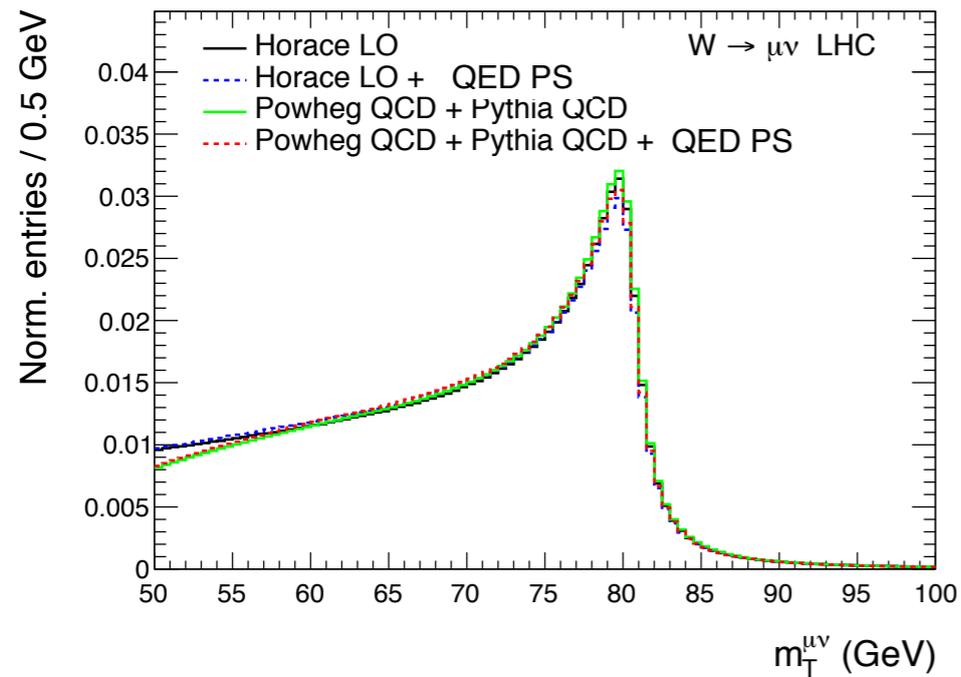
(two distinct parameters scalup are computed)

preserving the logarithmic accuracy of both QCD and QED emissions

Combination of QCD and QED corrections: POWHEG results

Carloni Calame, Chiesa, Martinez, Montagna, Nicrosini, Piccinini, AV, arXiv:1612.02841

Does the convolution with QCD corrections preserve the QED effects ?



the difference between red and blue is due to mixed QCDxQED terms

Is the impact of QED corrections preserved in a QCD environment ?

Carloni Calame, Chiesa, Martinez, Montagna, Nicrosini, Piccinini, AV, arXiv:1612.02841

Template fit applied to classify the impact of sets of radiative corrections

Templates accuracy: LO		M_W shifts (MeV)			
Pseudodata accuracy		$W^+ \rightarrow \mu^+ \nu$		$W^+ \rightarrow e^+ \nu$	
		M_T	p_T^ℓ	M_T	p_T^ℓ
1	HORACE only FSR-LL at $\mathcal{O}(\alpha)$	-94±1	-104±1	-204±1	-230±2
2	HORACE FSR-LL	-89±1	-97±1	-179±1	-195±1
3	HORACE NLO-EW with QED shower	-90±1	-94±1	-177±1	-190±2
4	HORACE FSR-LL + Pairs	-94±1	-102±1	-182±2	-199±1
5	PHOTOS FSR-LL	-92±1	-100±2	-182±1	-199±2

$pp \rightarrow W^+, \sqrt{s} = 14$ TeV			M_W shifts (MeV)			
Templates accuracy: NLO-QCD+QCD _{PS}			$W^+ \rightarrow \mu^+ \nu$		$W^+ \rightarrow e^+ \nu$ (dres)	
Pseudodata accuracy		QED FSR	M_T	p_T^ℓ	M_T	p_T^ℓ
1	NLO-QCD+(QCD+QED) _{PS}	PYTHIA	-95.2±0.6	-400±3	-38.0±0.6	-149±2
2	NLO-QCD+(QCD+QED) _{PS}	PHOTOS	-88.0±0.6	-368±2	-38.4±0.6	-150±3
3	NLO-(QCD+EW)+(QCD+QED) _{PS} two-rad	PYTHIA	-89.0±0.6	-371±3	-38.8±0.6	-157±3
4	NLO-(QCD+EW)+(QCD+QED) _{PS} two-rad	PHOTOS	-88.6±0.6	-370±3	-39.2±0.6	-159±2

Lepton-pair transverse mass: yes!

Lepton transverse momentum: no, the shifts are sizeably amplified

(these effects are already taken into account in the Tevatron and LHC analyses)

The lepton transverse momentum has a 85% weight in the final ATLAS M_W combination and a sound estimate of the uncertainty on the QCDxEW effects is crucial

Better control over higher-order subleading terms after matching

Carloni Calame, Chiesa, Martinez, Montagna, Nicrosini, Piccinini, AV, arXiv:1612.02841

$pp \rightarrow W^+, \sqrt{s} = 14 \text{ TeV}$			M_W shifts (MeV)			
Templates accuracy: NLO-QCD+QCD _{PS}			$W^+ \rightarrow \mu^+ \nu$		$W^+ \rightarrow e^+ \nu(\text{dres})$	
Pseudodata accuracy		QED FSR	M_T	p_T^ℓ	M_T	p_T^ℓ
1	NLO-QCD+(QCD+QED) _{PS}	PYTHIA	-95.2±0.6	-400±3	-38.0±0.6	-149±2
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4	NLO-(QCD+EW)+(QCD+QED) _{PS} two-rad	PHOTOS	-88.6±0.6	-370±3	-39.2±0.6	-159±2

PHOTOS and PYTHIA-QED differ at the level of $O(\alpha)$ subleading terms

→ large impact when used on top of a pure QCD code to describe also the first photon emission

After the matching with the $O(\alpha)$ matrix elements,
the role of the QED-PS starts from the second photon emission
and the difference are of $O(\alpha^2)$ subleading, yielding vanishing M_W shifts

At the W (Z) resonance PHOTOS offers a good description of the exact NLO result
(can not be extrapolated at larger invariant masses)

Exact mixed QCDxEW corrections the Drell-Yan cross section

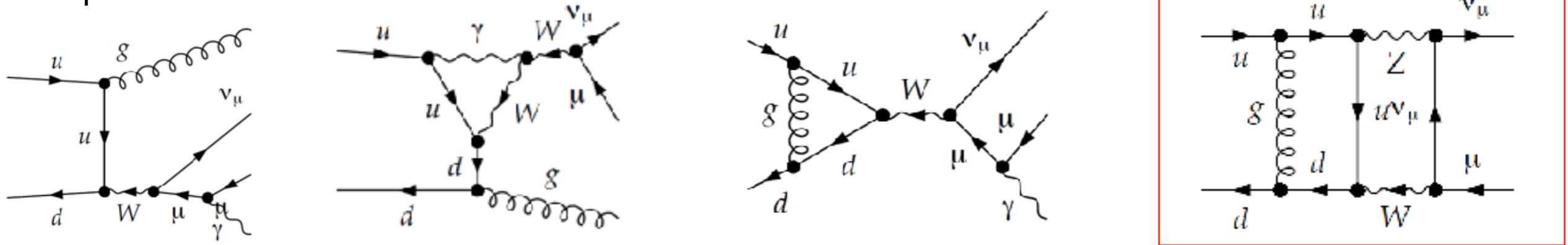
• The first mixed QCDxEW corrections of $O(\alpha\alpha_s)$ include different contributions:

- emission of two real additional partons (one photon + one gluon/quark)
- emission of one real additional parton (one photon with QCD virtual corrections, one gluon/quark with EW virtual corrections)
- two-loop virtual corrections

$$\sigma_{tot} = \sigma_0 + \alpha_s \sigma_{\alpha_s} + \alpha_s^2 \sigma_{\alpha_s^2} + \dots$$

$$+ \alpha \sigma_{\alpha} + \alpha^2 \sigma_{\alpha^2} + \dots$$

$$+ \boxed{\alpha \alpha_s \sigma_{\alpha \alpha_s}} + \alpha \alpha_s^2 \sigma_{\alpha \alpha_s^2} + \dots$$



→ exact complete calculation is not yet available, neither for DY nor for single gauge boson production

• The bulk of the mixed QCDxEW corrections, relevant for a precision MW measurement,

- is factorized in QCD and EW contributions:
 (leading-log part of final state QED radiation) X (leading-log part of initial state QCD radiation || NLO-QCD contribution to the K-factor)



- is included in all Monte Carlo simulation tools

Analytic progress: Master Integrals for DY processes at $O(\alpha\alpha_s)$

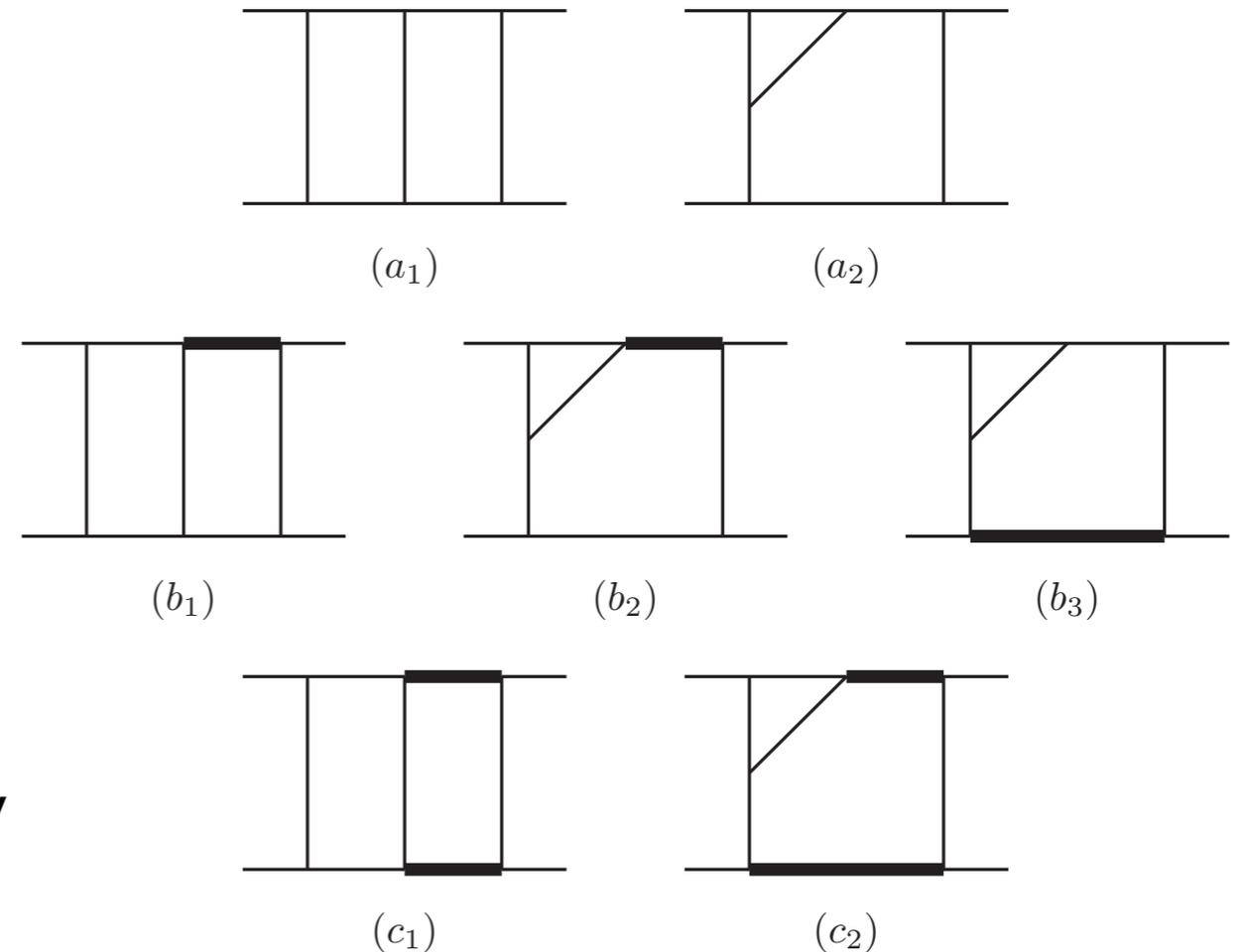
R. Bonciani, S. Di Vita, P. Mastrolia, U. Schubert, arXiv:1604.08581

thin lines massless
thick lines massive
topologies **b** and **c** were not known

2 masses topologies evaluated with the same mass

SM results, where both W and Z appear,
can be evaluated with an expansion in $\Delta M = M_Z - M_W$

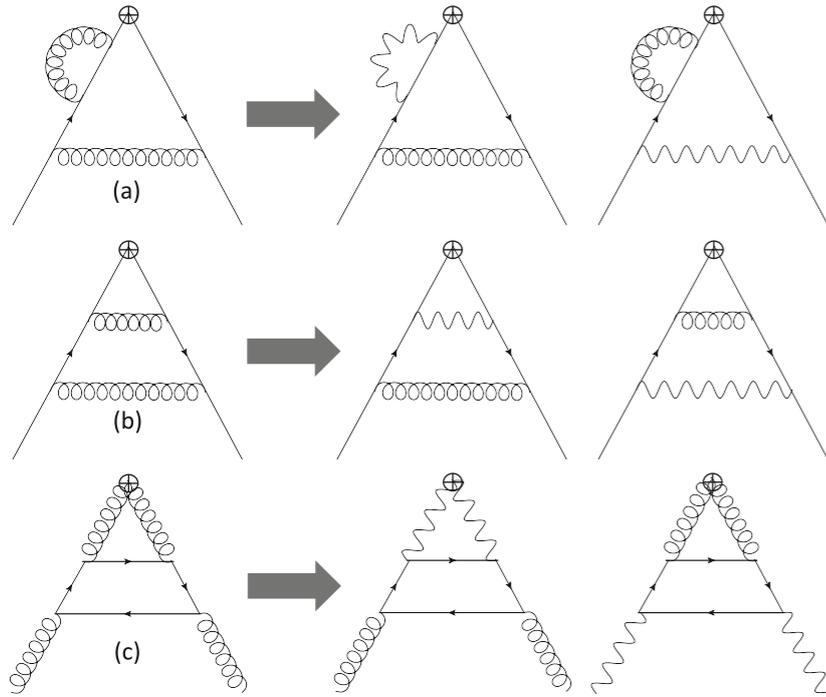
49 MI identified (8 massless, 24 1-mass, 17 2-masses)
solution of differential equations expressed in terms of
iterated integrals (mixed Chen-Goncharov representation)



Splitting functions at $O(\alpha\alpha_s)$

D. de Florian, G.F.R. Sborlini, G. Rodrigo, Eur.Phys.J. C76 (2016) no.5, 282 , arXiv:1606.02887

starting from the expressions by Curci-Furmanski-Petronzio



needed for a complete subtraction in partonic calculations of initial state collinear singularities at $O(\alpha\alpha_s)$

not sufficient for a consistent PDF evolution at the same order

$$P_{q\gamma}^{(1,1)} = \frac{C_F C_A e_q^2}{2} \left\{ 4 - 9x - (1 - 4x) \ln(x) - (1 - 2x) \times \ln^2(x) + 4 \ln(1 - x) + p_{qg}(x) \left[2 \ln^2\left(\frac{1-x}{x}\right) - 4 \ln\left(\frac{1-x}{x}\right) - \frac{2\pi^2}{3} + 10 \right] \right\}, \quad (26)$$

$$P_{g\gamma}^{(1,1)} = C_F C_A \left(\sum_{j=1}^{n_F} e_{q_j}^2 \right) \left\{ -16 + 8x + \frac{20}{3}x^2 + \frac{4}{3x} - (6 + 10x) \ln(x) - 2(1 + x) \ln^2(x) \right\}, \quad (27)$$

$$P_{\gamma\gamma}^{(1,1)} = -C_F C_A \left(\sum_{j=1}^{n_F} e_{q_j}^2 \right) \delta(1 - x), \quad (28)$$

$$P_{qg}^{(1,1)} = \frac{T_R e_q^2}{2} \left\{ 4 - 9x - (1 - 4x) \ln(x) - (1 - 2x) \times \ln^2(x) + 4 \ln(1 - x) + p_{qg}(x) \left[2 \ln^2\left(\frac{1-x}{x}\right) - 4 \ln\left(\frac{1-x}{x}\right) - \frac{2\pi^2}{3} + 10 \right] \right\},$$

$$P_{\gamma g}^{(1,1)} = T_R \left(\sum_{j=1}^{n_F} e_{q_j}^2 \right) \left\{ -16 + 8x + \frac{20}{3}x^2 + \frac{4}{3x} - (6 + 10x) \ln(x) - 2(1 + x) \ln^2(x) \right\},$$

$$P_{gg}^{(1,1)} = -T_R \left(\sum_{j=1}^{n_F} e_{q_j}^2 \right) \delta(1 - x),$$

$$P_{qq}^{S(1,1)} = P_{q\bar{q}}^{S(1,1)} = 0, \quad (32)$$

$$P_{qq}^{V(1,1)} = -2 C_F e_q^2 \left[\left(2 \ln(1 - x) + \frac{3}{2} \right) \ln(x) p_{qq}(x) + \frac{3 + 7x}{2} \ln(x) + \frac{1 + x}{2} \ln^2(x) + 5(1 - x) + \left(\frac{\pi^2}{2} - \frac{3}{8} - 6\zeta_3 \right) \delta(1 - x) \right], \quad (33)$$

$$P_{q\bar{q}}^{V(1,1)} = 2 C_F e_q^2 [4(1 - x) + 2(1 + x) \ln(x) + 2p_{qq}(-x)S_2(x)], \quad (34)$$

$$P_{gq}^{(1,1)} = C_F e_q^2 \left[-(3 \ln(1 - x) + \ln^2(1 - x)) p_{gq}(x) + \left(2 + \frac{7}{2}x \right) \ln(x) - \left(1 - \frac{x}{2} \right) \ln^2(x) - 2x \ln(1 - x) - \frac{7}{2}x - \frac{5}{2} \right], \quad (35)$$

$$P_{\gamma q}^{(1,1)} = P_{gq}^{(1,1)}, \quad (36)$$

PDF uncertainties

PDF uncertainties and Drell-Yan processes

The experimental PDF uncertainty is represented in terms of replicas

and can be propagated to any observable, e.g. to the templates used to fit the EW parameters

→ it represents a theoretical systematic uncertainty of the EW measurements

Different observables are correlated w.r.t. a PDF replica variation

→ this correlation must be taken into account in the template fit procedure

Drell-Yan processes (NC and CC) share a similar kinematical regime,

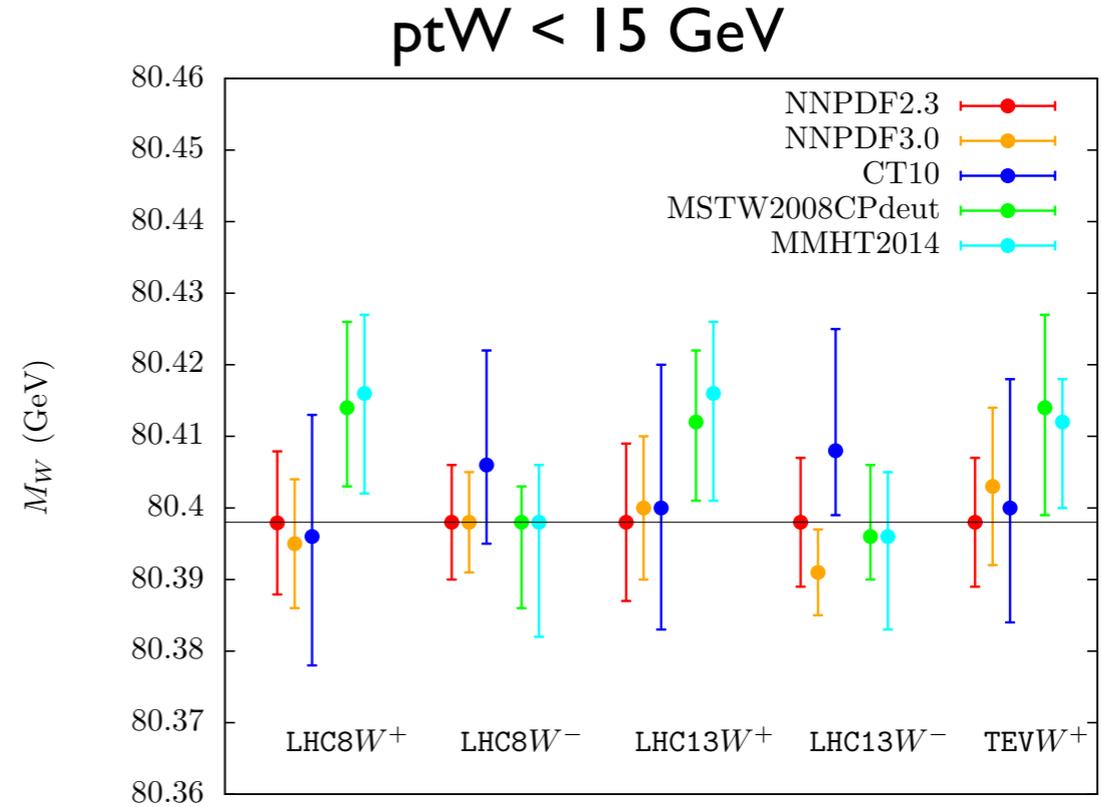
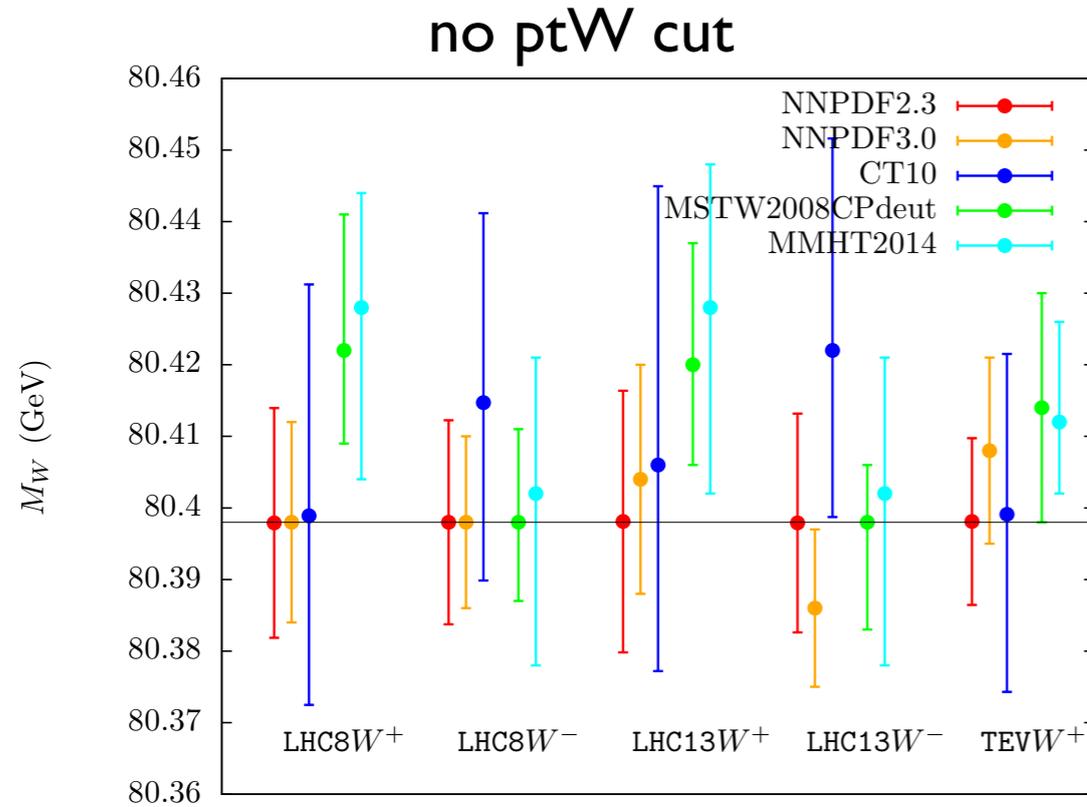
but also differ because of the different initial state flavour structure

→ we can expect a strong interplay (but not a perfect cancellation) of PDF uncertainties in a simultaneous fit of CC and NC observables

The role of a PDF4LHC prescription, often considered as too conservative, should be rediscussed to understand if it is legitimate to say that high-precision data may select (prefer) one PDF set

PDF uncertainty affecting MW extracted from the p_{lep} distribution

G.Bozzi, L.Citelli, AV, arXiv:1501.05587



	no p_{\perp}^W cut		$p_{\perp}^W < 15$ GeV	
	δ_{PDF} (MeV)	Δ_{sets} (MeV)	δ_{PDF} (MeV)	Δ_{sets} (MeV)
Tevatron 1.96 TeV	27	16	21	15
LHC 8 TeV W^+	33	26	24	18
W^-	29	16	18	8
LHC 13 TeV W^+	34	22	20	14
W^-	34	24	18	12

the PDF4LHC recipe defines
the half-width of the envelope δ_{PDF}
and the spread of the central values Δ_{sets}

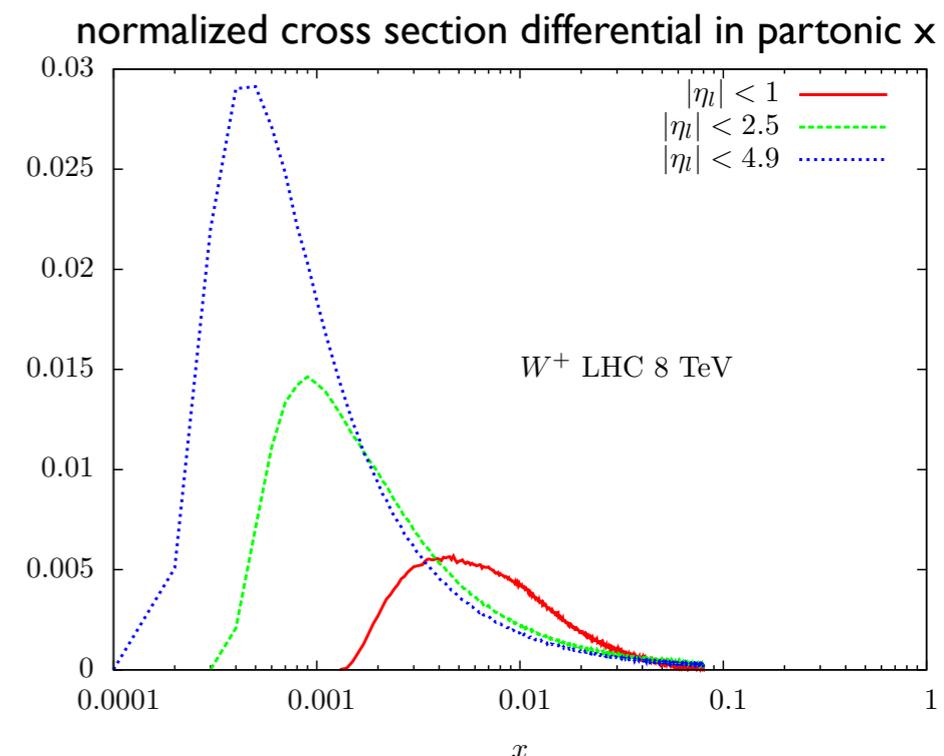
- Modern individual PDF sets provide not-pessimistic estimates, $\Delta MW \sim O(10 \text{ MeV})$, but the global envelope still shows **large discrepancies of the central values**
- The Tevatron analyses did not adopt the PDF4LHC approach
- Conservative analysis (only CC-DY values have been included)

PDF uncertainty affecting MW and acceptance cuts

G.Bozzi, L.Citelli, AV, arXiv:1501.05587

The dependence of the MW PDF uncertainty on the acceptance cuts provides interesting insights

normalized distributions			
cut on p_{\perp}^W	cut on $ \eta_l $	CT10	NNPDF3.0
inclusive	$ \eta_l < 2.5$	$80.400 + 0.032 - 0.027$	80.398 ± 0.014
$p_{\perp}^W < 20$ GeV	$ \eta_l < 2.5$	$80.396 + 0.027 - 0.020$	80.394 ± 0.012
$p_{\perp}^W < 15$ GeV	$ \eta_l < 2.5$	$80.396 + 0.017 - 0.018$	80.395 ± 0.009
$p_{\perp}^W < 10$ GeV	$ \eta_l < 2.5$	$80.392 + 0.015 - 0.012$	80.394 ± 0.007
$p_{\perp}^W < 15$ GeV	$ \eta_l < 1.0$	$80.400 + 0.032 - 0.021$	80.406 ± 0.017
$p_{\perp}^W < 15$ GeV	$ \eta_l < 2.5$	$80.396 + 0.017 - 0.018$	80.395 ± 0.009
$p_{\perp}^W < 15$ GeV	$ \eta_l < 4.9$	$80.400 + 0.009 - 0.004$	80.401 ± 0.003
$p_{\perp}^W < 15$ GeV	$1.0 < \eta_l < 2.5$	$80.392 + 0.025 - 0.018$	80.388 ± 0.012

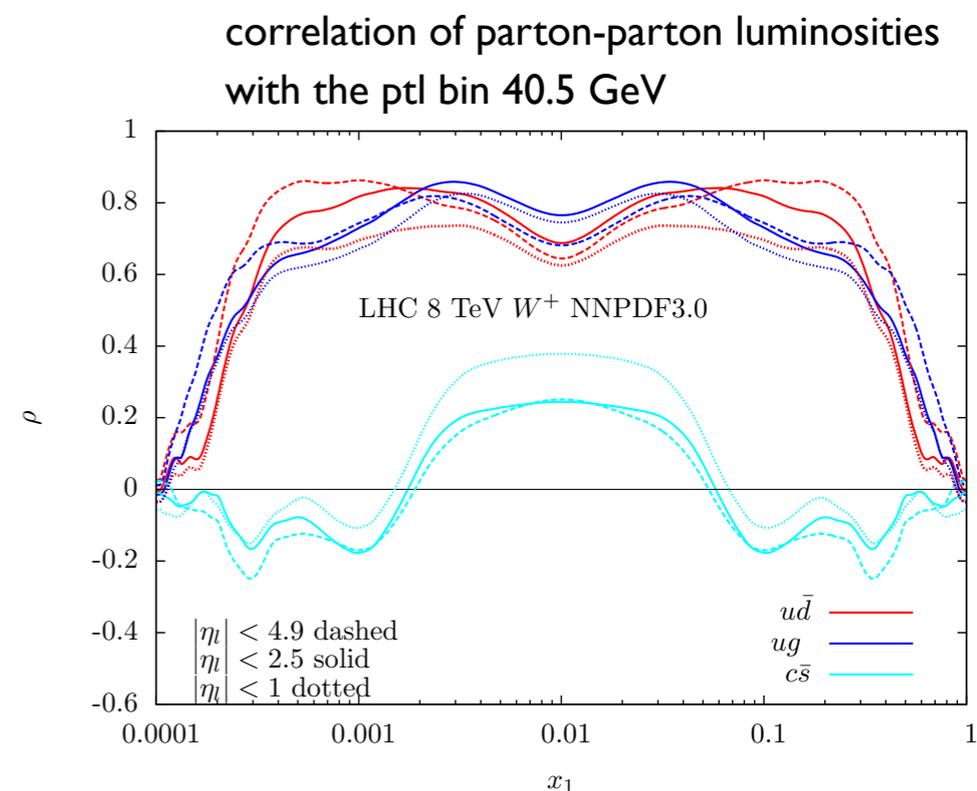


- cut on the lepton pseudorapidity

- the normalized p_{lep} distribution, integrated over the whole lepton-pair rapidity range, does not depend on x and depends very weakly on the PDF replica

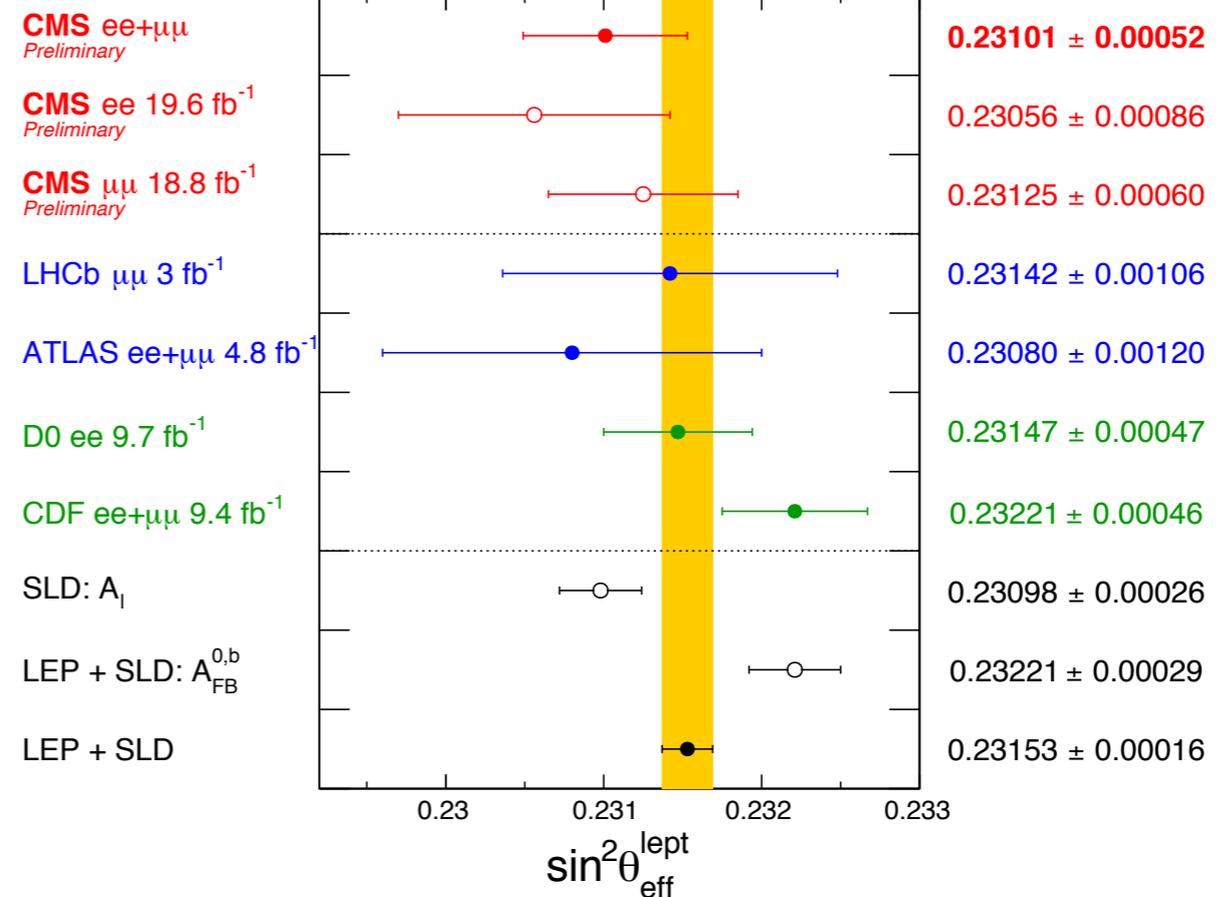
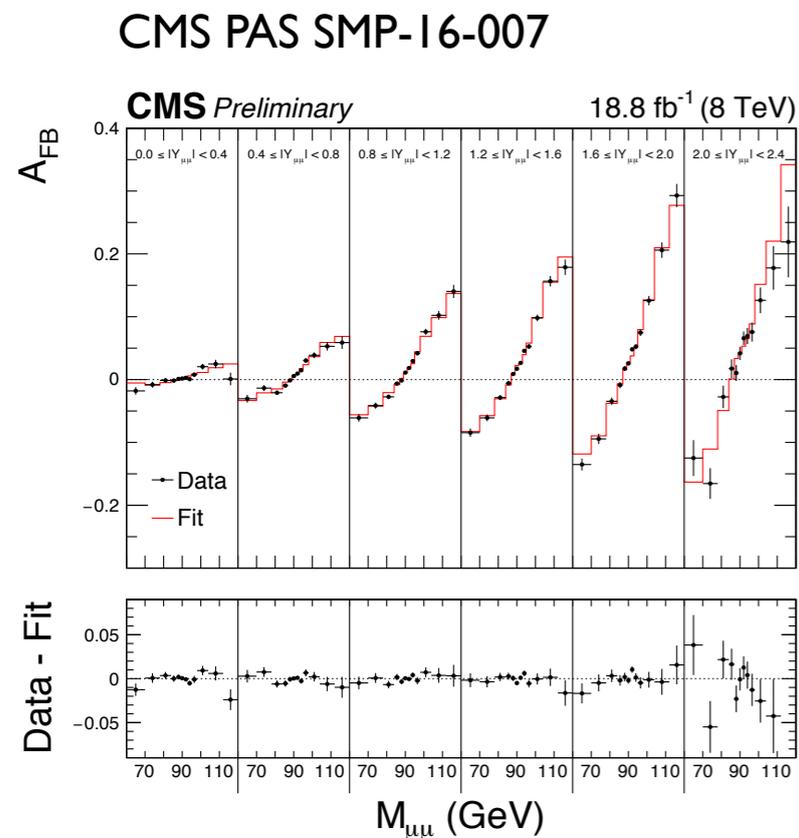
- the central rapidity region is the most uncertain

- PDF sum rules \rightarrow
non trivial compensations between different rapidity intervals among different flavors



- **MW measurement at LHCb could significantly reduce the global PDF uncertainty**

The $\sin^2\theta_{\text{eff}}(\text{leptonic})$ measurements at the LHC



different PDF dependence of the 72 (M_{ll} - Y) bins \rightarrow

the bins close to M_Z , dominated by $|M_Z|^2$ sensitive to $\sin^2\theta_{\text{eff}}(\text{leptonic})$

the bins far from M_Z , dominated by $(\mathcal{M}_\gamma \mathcal{M}_Z^\dagger)$ used to “choose” the best PDF replicas

that yield a better agreement with the data

reduction of the PDF uncertainty via

Bayesian reweighing of the PDF MC replicas

CMS PAS SMP-16-007

Channel	without constraining PDFs	with constraining PDFs
Muon	0.23125 ± 0.00054	0.23125 ± 0.00032
Electron	0.23054 ± 0.00064	0.23056 ± 0.00045
Combined	0.23102 ± 0.00057	0.23101 ± 0.00030

the inclusion of bins far from M_Z implies that the template fit is done in the SM and $\sin^2\theta_w$ (or M_W), the fit parameter, should be one of the lagrangian inputs

$\sin^2\theta_{\text{eff}}(\text{leptonic})$ can be computed from $\sin^2\theta_w$ with a theoretical relation available at 2-loop level

Conclusions

SM precision tests are the basic fundamental step to understand the likelihood of the SM itself
to start a motivated search for BSM signals

The precision measurement of EW parameters like M_W and the weak mixing angle offers
sensitivity to BSM physics active via the oblique corrections

ATLAS, CMS and LHCb are delivering impressive measurements,
which will allow a determination of M_W and $\sin^2\theta_w$ competitive with the LEP and Tevatron results

Conclusions

SM precision tests are the basic fundamental step to understand the likelihood of the SM itself
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ATLAS, CMS and LHCb are delivering impressive measurements,
which will allow a determination of M_W and $\sin^2\theta_w$ competitive with the LEP and Tevatron results

LHC can be an EW precision machine (!!!), provided that

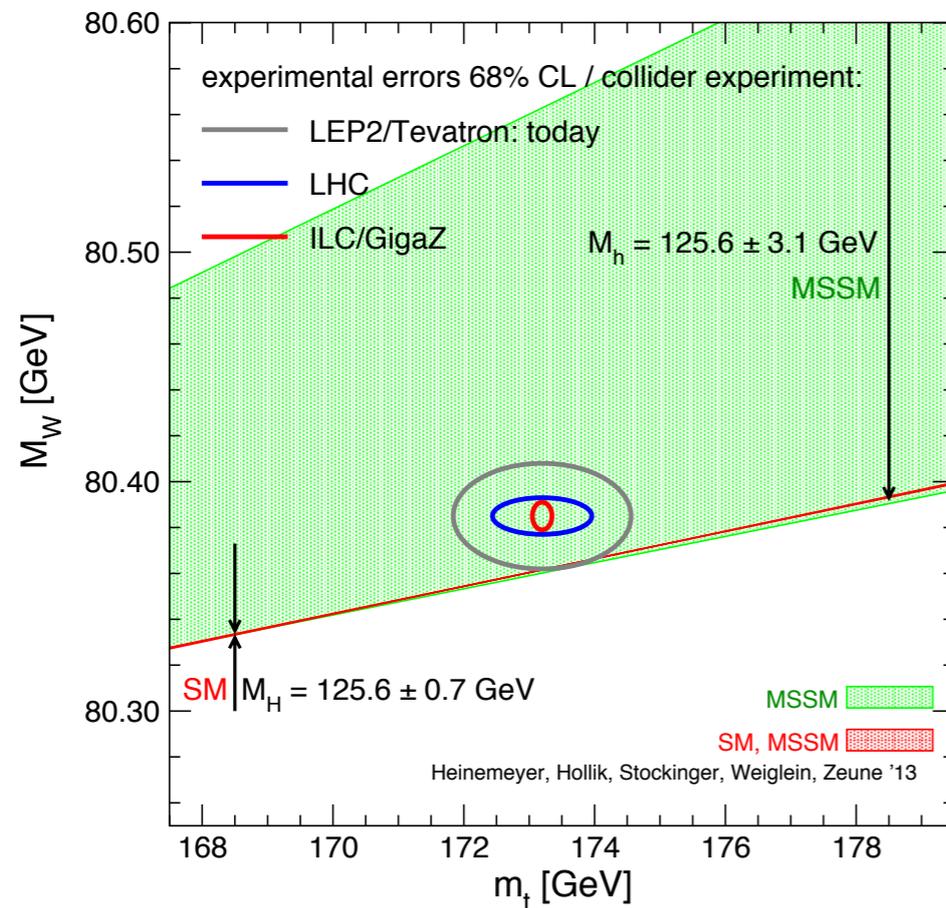
- ▷ the modelling of the QCD environment is understood
in terms of all the correlations between the processes (NC and CC) included in the analysis
PDFs, heavy quarks, low-pt non-perturbative effects
scale uncertainties in the simultaneous fit of several processes
- ▷ the exact $O(\alpha\alpha_s)$, consistently matched, are included in Monte Carlo event generators

so that

- ▷ a realistic estimate of the theoretical uncertainties becomes possible.
- ▷ the full amount of available information is extracted from the wealth of precision data

backup slides

Possible interpretation of the MW measurement



MW can be computed as a function of
 $(\alpha, G_\mu, M_Z, M_H; m_{\text{top}}, \dots)$
 in different models

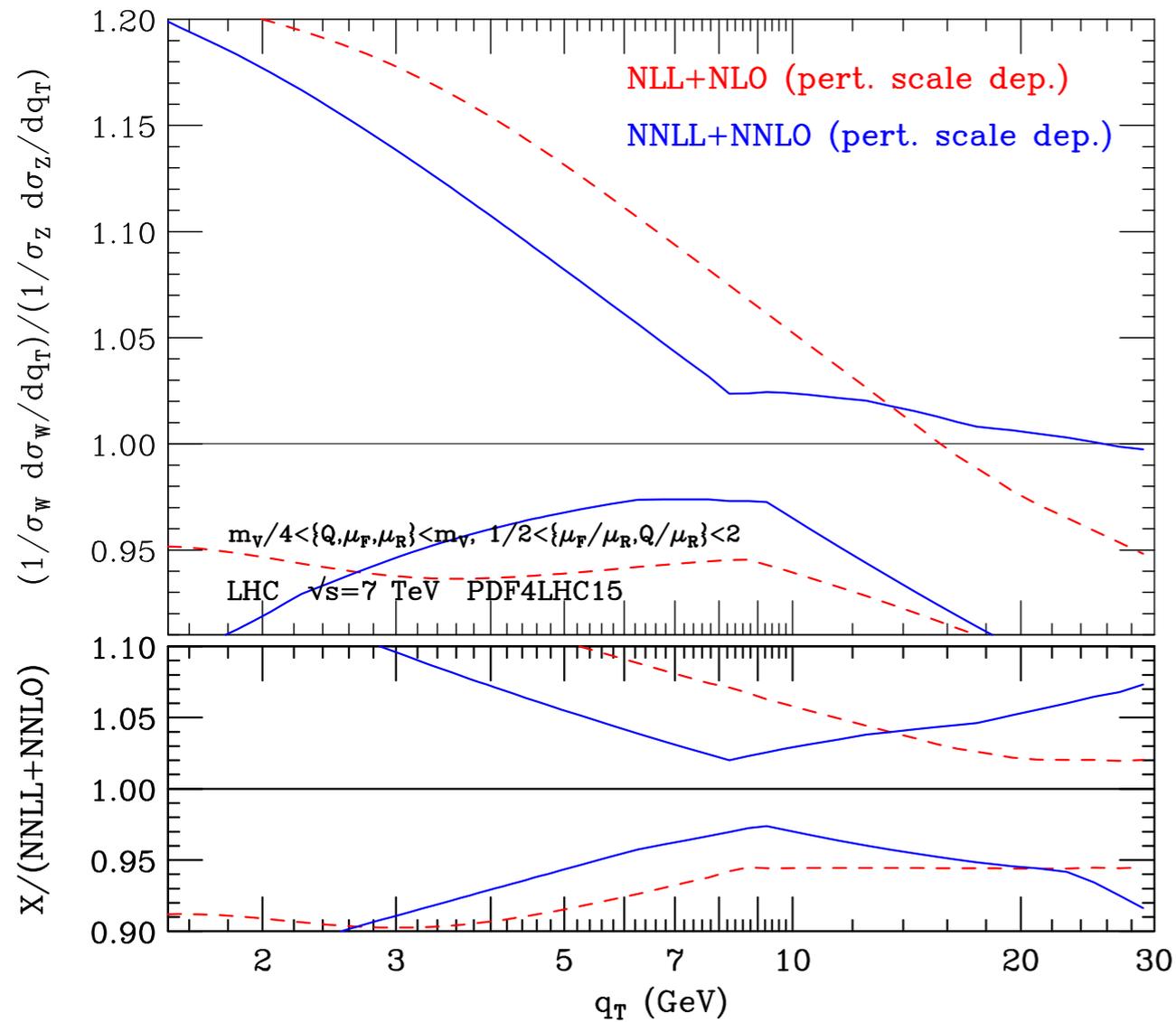
$$m_W^2 = \frac{m_Z^2}{2} \left(1 + \sqrt{1 - \frac{4\pi\alpha}{G_\mu \sqrt{2} m_Z^2} (1 + \Delta r)} \right)$$

$$m_W = m_W (\Delta r^{SM, MSSM})$$

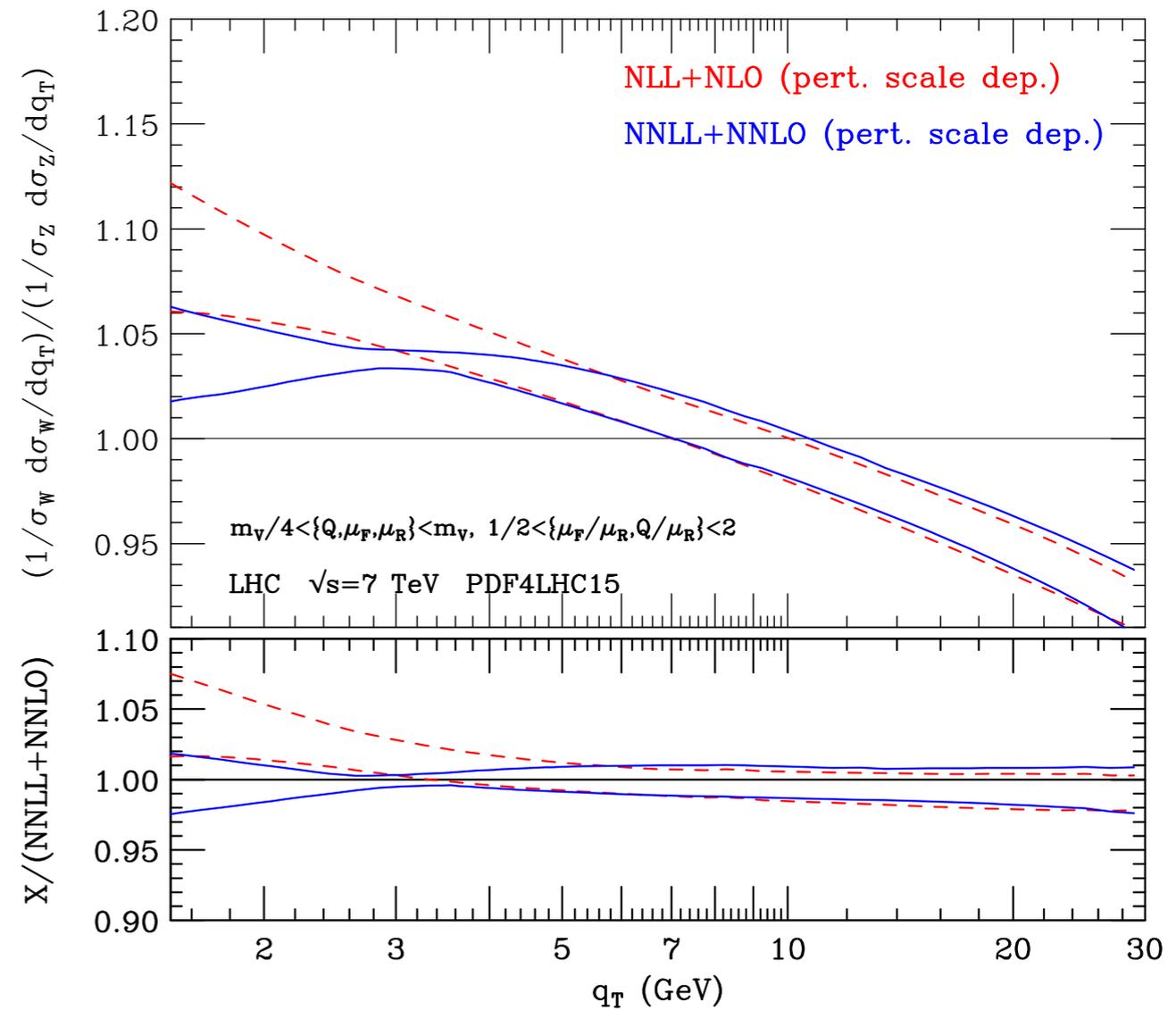
$$\Delta r^{SM, MSSM} = \Delta r^{SM, MSSM} (m_t, m_H, m^{SUSY}, \dots)$$

relevance of a correct estimate of the MW central value and associated error

W/Z ratio q_T spectrum: perturbative scale uncertainty



DY q_T resummed predictions for the ratio of W/Z normalized q_T spectra. **Uncorrelated** perturbative scale variation band.



DY q_T resummed predictions for the ratio of W/Z normalized q_T spectra. **Correlated** perturbative scale variation band.

Impact of a LHCb MW measurement in combination with the ATLAS/CMS results

G.Bozzi, L.Citelli, M.Vesterinen, AV, arXiv:1508.06954

- using the standard acceptance cuts

for ATLAS/CMS (called **G**) and for LHCb (called **L**) and both W charges

we study the MW determination from the lepton pt distribution

assuming that a LHCb measurement becomes available

- PDF uncertainty on MW according to PDF4LHC (NNPDF3.0, MMHT2014)

$$\delta_{\text{PDF}} = \begin{pmatrix} \mathbf{G}^+ & 24.8 \\ \mathbf{G}^- & 13.2 \\ \mathbf{L}^+ & 27.0 \\ \mathbf{L}^- & 49.3 \end{pmatrix}$$

- correlation matrix ρ w.r.t. PDF variation of the replicas of the NNPDF3.0 set

→ non negligible anticorrelation

consequence of the sum rules satisfied by the PDFs

it appears because we probe different rapidity regions

$$\rho = \begin{pmatrix} & \mathbf{G}^+ & \mathbf{G}^- & \mathbf{L}^+ & \mathbf{L}^- \\ \mathbf{G}^+ & 1 & & & \\ \mathbf{G}^- & -0.22 & 1 & & \\ \mathbf{L}^+ & -0.63 & 0.11 & 1 & \\ \mathbf{L}^- & -0.02 & -0.30 & 0.21 & 1 \end{pmatrix}$$

- the linear combination that minimizes the final uncertainty on MW

is given by the coefficients α

$$m_W = \sum_{i=1}^4 \alpha_i m_{W_i} \quad \alpha = \begin{pmatrix} \mathbf{G}^+ & 0.30 \\ \mathbf{G}^- & 0.45 \\ \mathbf{L}^+ & 0.21 \\ \mathbf{L}^- & 0.04 \end{pmatrix}$$

- the exercise is robust under conservative assumptions for the LHCb main systematic uncertainties and guarantees a reduction by 30% of the PDF uncertainty estimated for ATLAS/CMS alone

- potential serious bottleneck for a measurement based on ptl: ptW modeling in the LHCb acceptance

More on the structure of QCDxEW corrections in POWHEG

- EW corrections may become large in the photon soft/collinear limit or in the **EW Sudakov regime**

POWHEG NLO-(QCD+EW)

$$d\sigma = \sum_{f_b} \bar{B}^{f_b}(\Phi_n) d\Phi_n \left\{ \Delta^{f_b}(\Phi_n, p_T^{min}) + \sum_{\alpha_r \in \{\alpha_r | f_b\}} \frac{[d\Phi_{rad} \theta(k_T - p_T^{min}) \Delta^{f_b}(\Phi_n, k_T) R(\Phi_{n+1})]_{\alpha_r}^{\bar{\Phi}_n^{\alpha_r} = \Phi_n}}{B^{f_b}(\Phi_n)} \right\}$$

the difference between QCDxQED and QCDxEW approximations starts at $O(\alpha\alpha_s)$

POWHEG NLO-QCD x (QCD+QED)-PS

$$\alpha_s \alpha (c_2 L_{QCD}^2 + c_1 L_{QCD} + c_0) (c_{11} L_{QED} l_{QED} + c_{10} L_{QED} + c_{01} l_{QED})$$

POWHEG NLO-(QCD+EW) x (QCD+QED)-PS

$$\alpha_s \alpha (c_2 L_{QCD}^2 + c_1 L_{QCD} + c_0) (c_{11} L_{QED} l_{QED} + c_{10} L_{QED} + c_{01} l_{QED} + c_{00})$$

the difference $\alpha_s \alpha c_{00} (c_2 L_{QCD}^2 + c_1 L_{QCD} + c_0)$ important when c_{00} is large

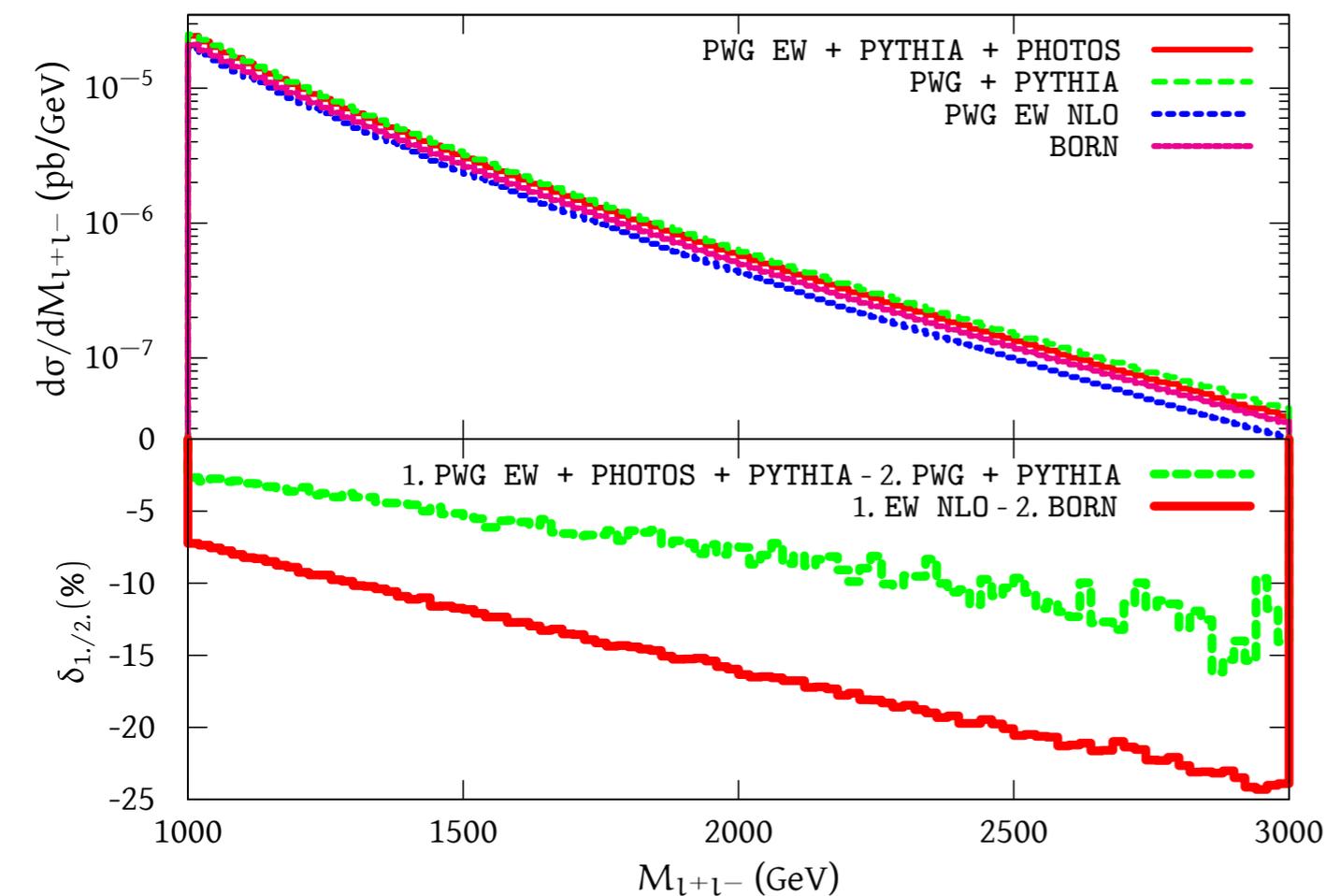
c_{00} does not contain QED logs, but Sudakov EW logs $c_{00} \propto -\frac{\alpha}{4\pi \sin^2 \theta_W} \log^2 \frac{s}{m_W^2}$

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the difference between red and green

due to $O(\alpha\alpha_s)$

arising from the product of $B_{bar} \times \{ \dots \}$

relevant when setting limits on Z' masses

terms beyond the formal accuracy of the code missing e.g. in FEWZ

→ need of exact $O(\alpha\alpha_s)$

to provide a more robust prediction

