



Crystallisation

free energy has two main terms

$$\text{Volume: } L \cdot V \frac{\Delta T}{T_c} = -L \frac{4\pi}{3} R^3 \frac{\Delta T}{T_c}$$

\uparrow latent heat \uparrow Volume

$$\text{Surface tension: } \sigma \cdot A = \sigma 4\pi R^2$$

\uparrow surface tension \uparrow surface area

$$F = -L \frac{4\pi}{3} R^3 \frac{\Delta T}{T_c} + \sigma 4\pi R^2$$

$$\text{Point} \Rightarrow \frac{\partial F}{\partial R} = 0 \rightarrow \frac{\partial F}{\partial R} = -4\pi L R^2 \frac{\Delta T}{T_c} + 2 \cdot \sigma 4\pi R \stackrel{!}{=} 0$$

$$R_{\text{crit}} \Rightarrow \frac{\partial F}{\partial R} = 0 \rightarrow \frac{\partial F}{\partial R} = - \cancel{3L} \frac{\cancel{4\pi}}{3} R^2 \frac{\Delta T}{T_c} + 2 \cdot \cancel{\sigma} \cancel{L} \geq 0$$

$$R_{\text{crit}} = \frac{2T_c \sigma}{\Delta T L}$$