

FS17 Prof. Dr. Johan Chang

Discussion on 17th May

Due on 24^{th} May

Exercise 1 Electron / hole density and Hall effect in GaAs In the lecture, we derived for the electron density $n = 2 \left(\frac{m_e k_B T}{2\pi\hbar^2}\right)^{3/2} \exp[(\mu - E_c)/k_B T]$ and a similar formula for the hole density p.

- (a) Use the effective mass and the band gap (see table values of the lecture slides) to estimate n and p (for light holes).
- (b) Calculate the Hall coefficient if only holes or electrons contribute.

Exercise 2 Quantum oscillations on quasi two-dimensional systems

In Tl₂Ba₂CuO_{6+ δ}, quantum oscillations with a frequency of $F = 18.1 \,\text{kT}$ are observed (B. Vignolle et al., Nature **455**, 952-955 (2008)).

- (a) Use the Onsager relation $(S = 2\pi \frac{eF}{\hbar})$ to calculate the Fermi surface area.
- (b) If we assume a circular Fermi surface shape, what is the Fermi momentum?

Exercise 3 Quantum oscillations in gold

Estimate the Fermi energy of gold (in eV) based on the oscillations of the spin susceptibility in a magnetic field, see figure 1. Which of the two superimposed oscillations corresponds to the largest orbit on the Fermi-sphere? Compare the result with the literature value $\epsilon_{\rm F} = 5.51 \, {\rm eV}$. Where is the other oscillation originating from?



Figure 1: The spin susceptibility of gold in a magnetic field.