

PHY 127 FS2025

Prof. Ben Kilminster

Lecture 11

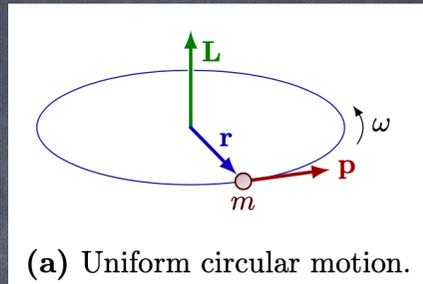
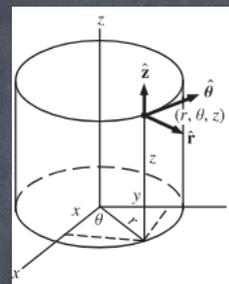
May 16th, 2025

From PHY 117:
angular momentum
torque
magnetic moment

NMR \rightarrow MRI
(spin precession of nuclei)

Angular momentum reminder





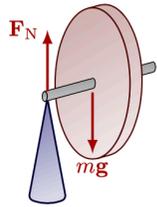
(a) Uniform circular motion.

Interesting consequences

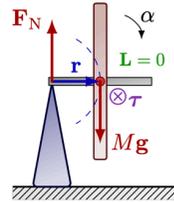


Interesting consequences

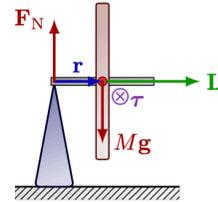




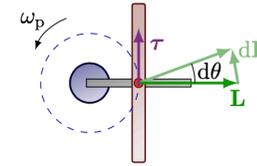
(a) The handle allows the disk to spin around its axis and around the pivot.



(b) The disk does not spin, and it will fall down due to an unbalanced torque τ .



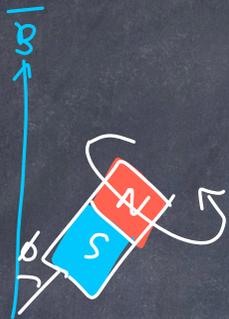
(c) The disk spins, creating an angular momentum \mathbf{L} . Torque τ will cause a precession.

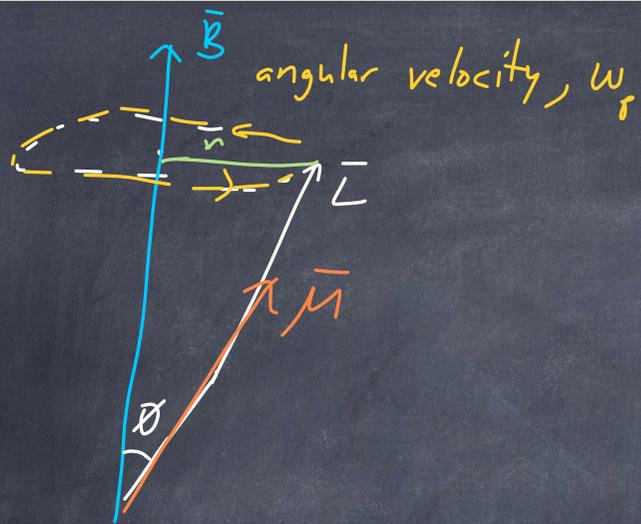


(d) Torque τ perpendicular to angular momentum \mathbf{L} , will only change its direction.



The same effect occurs for a magnet spinning in a magnetic field

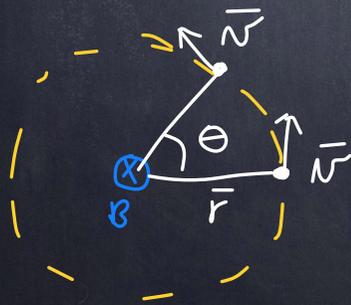




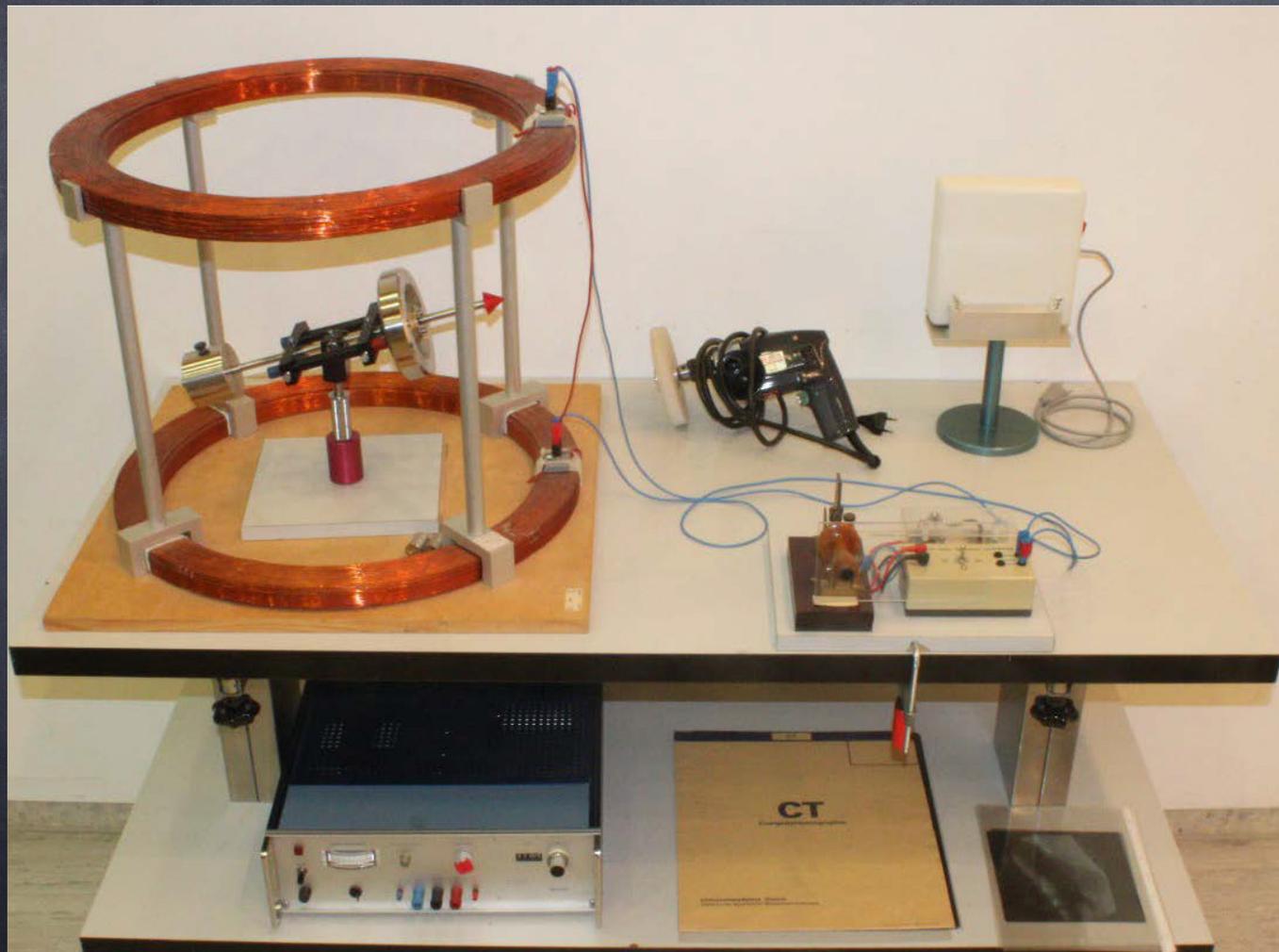
$$r = L \sin \theta$$

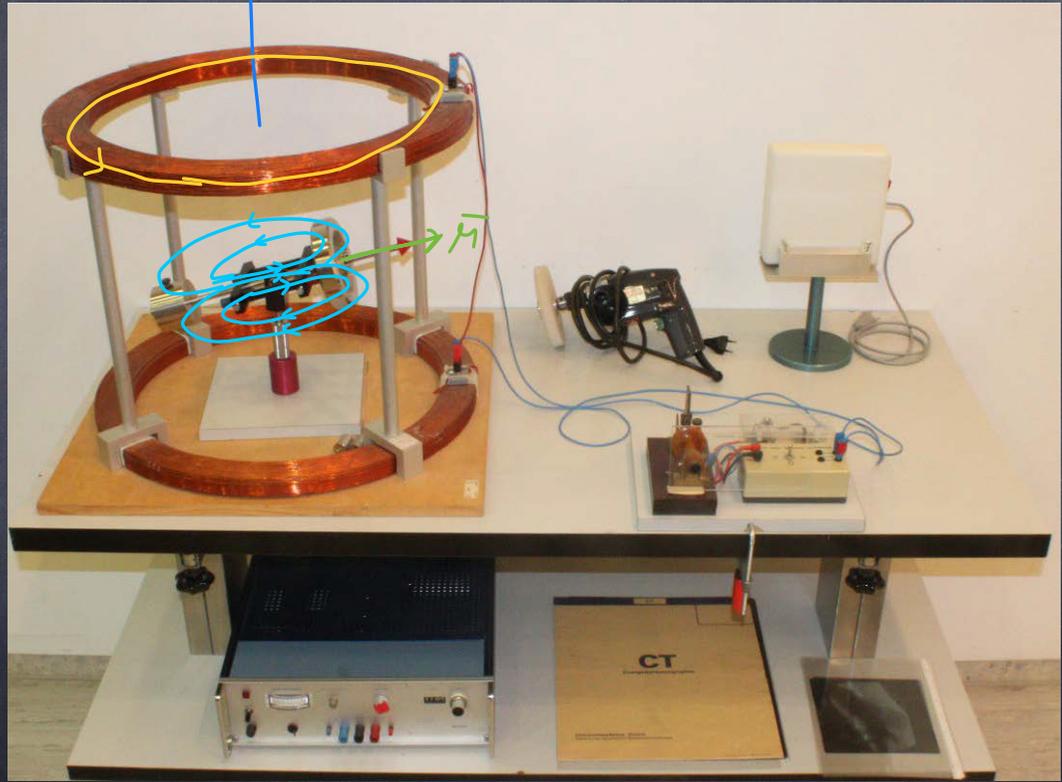
$$v = r \omega_p = \omega_p L \sin \theta$$

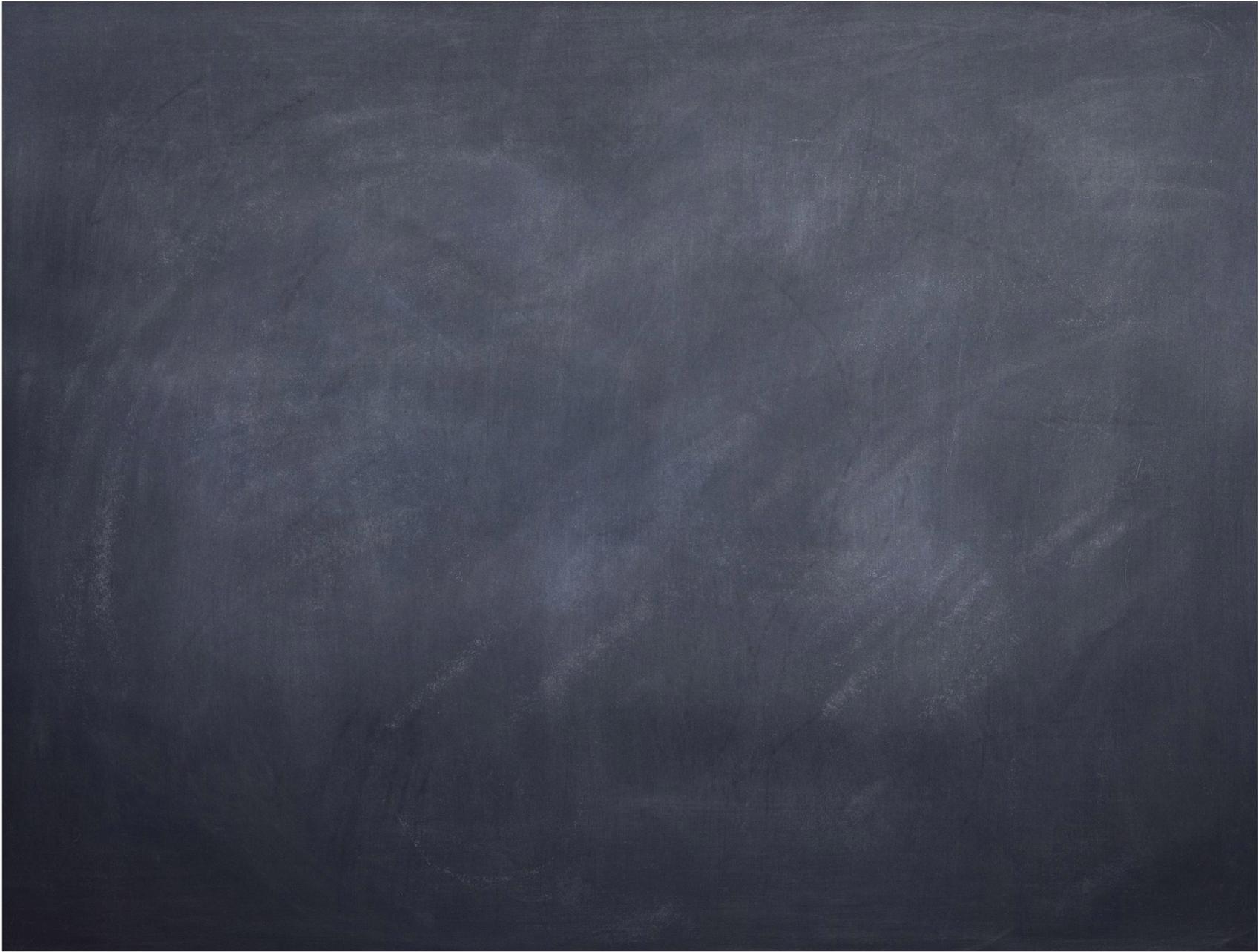
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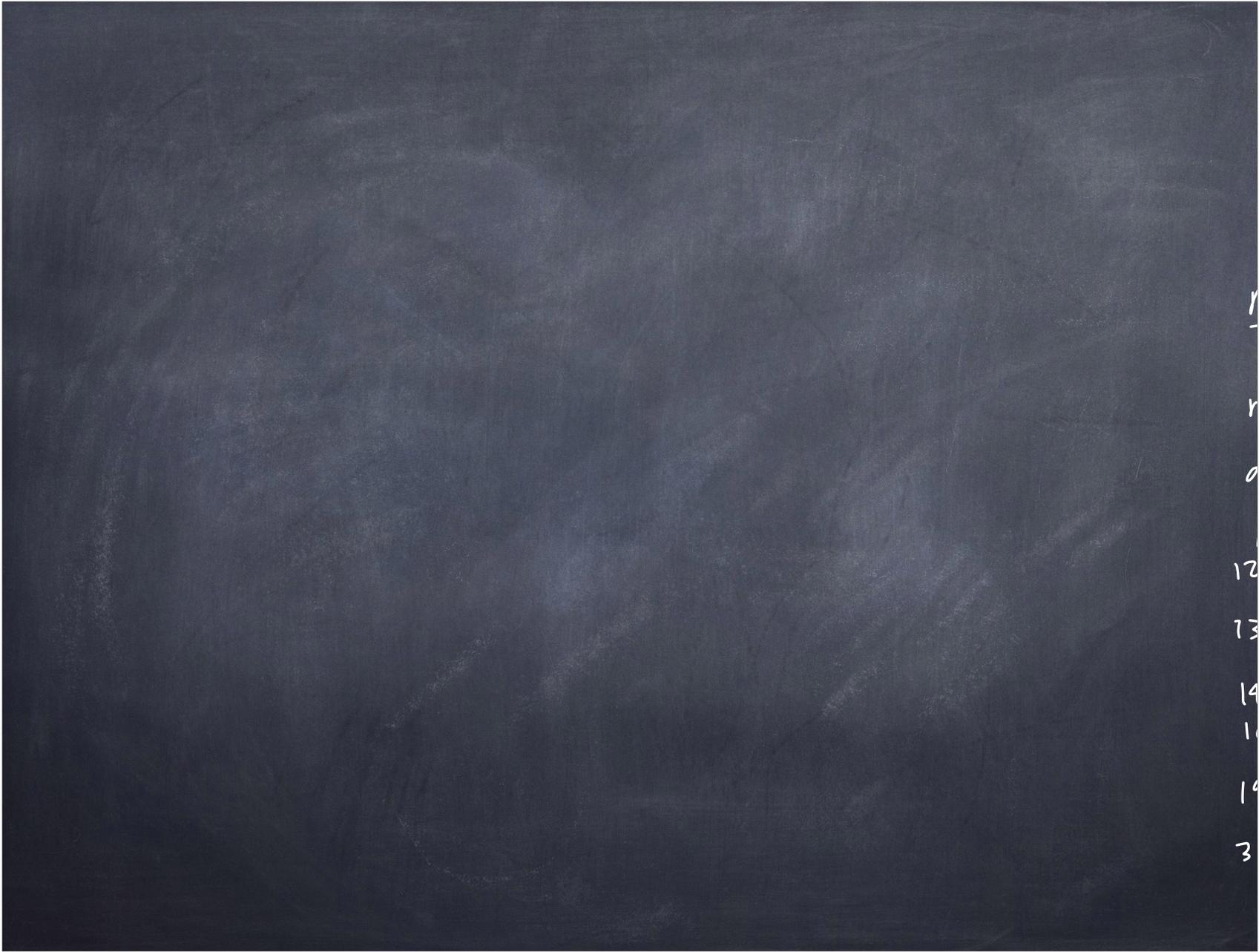


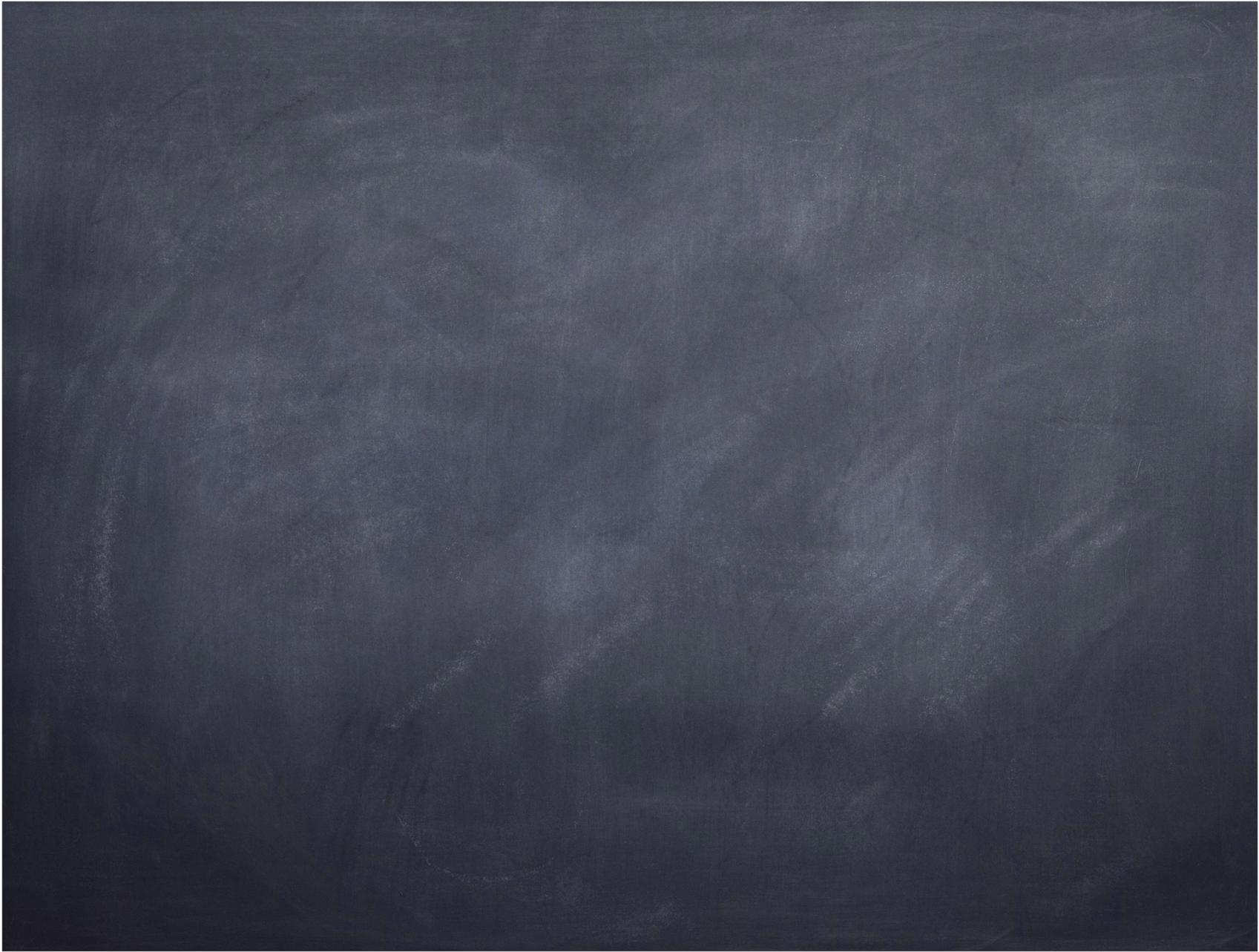
$$v = r \frac{d\theta}{dt} = r \omega_p$$

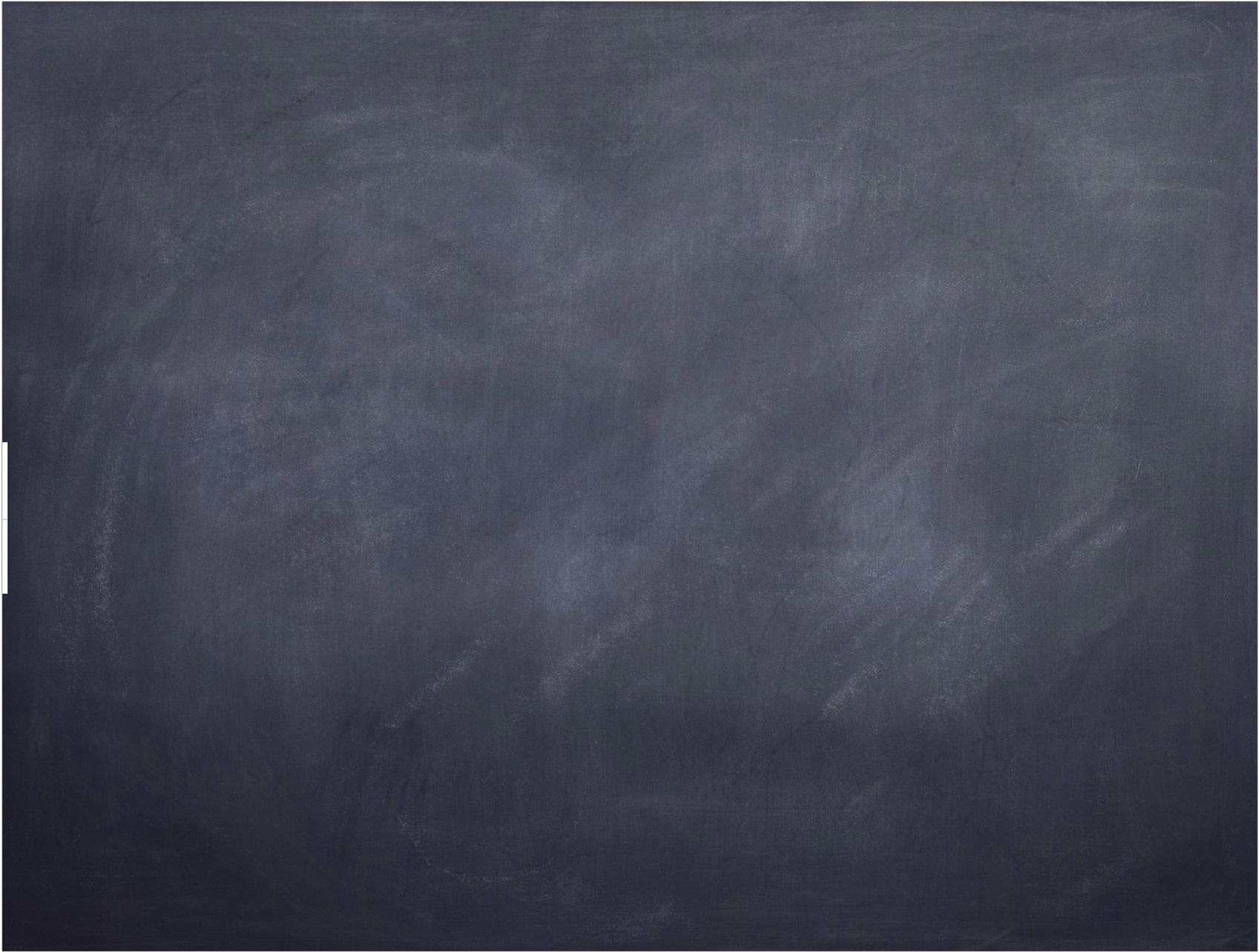


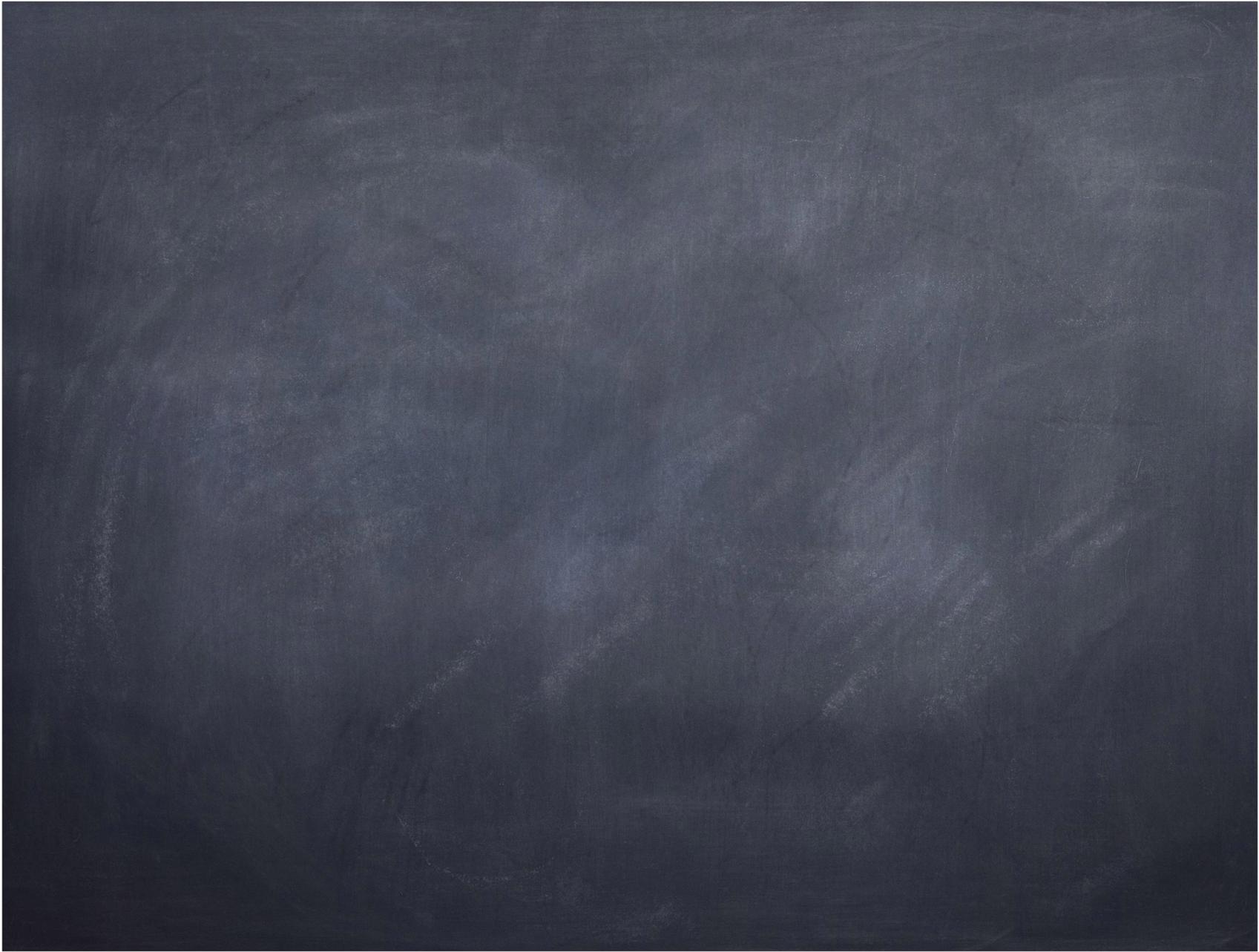


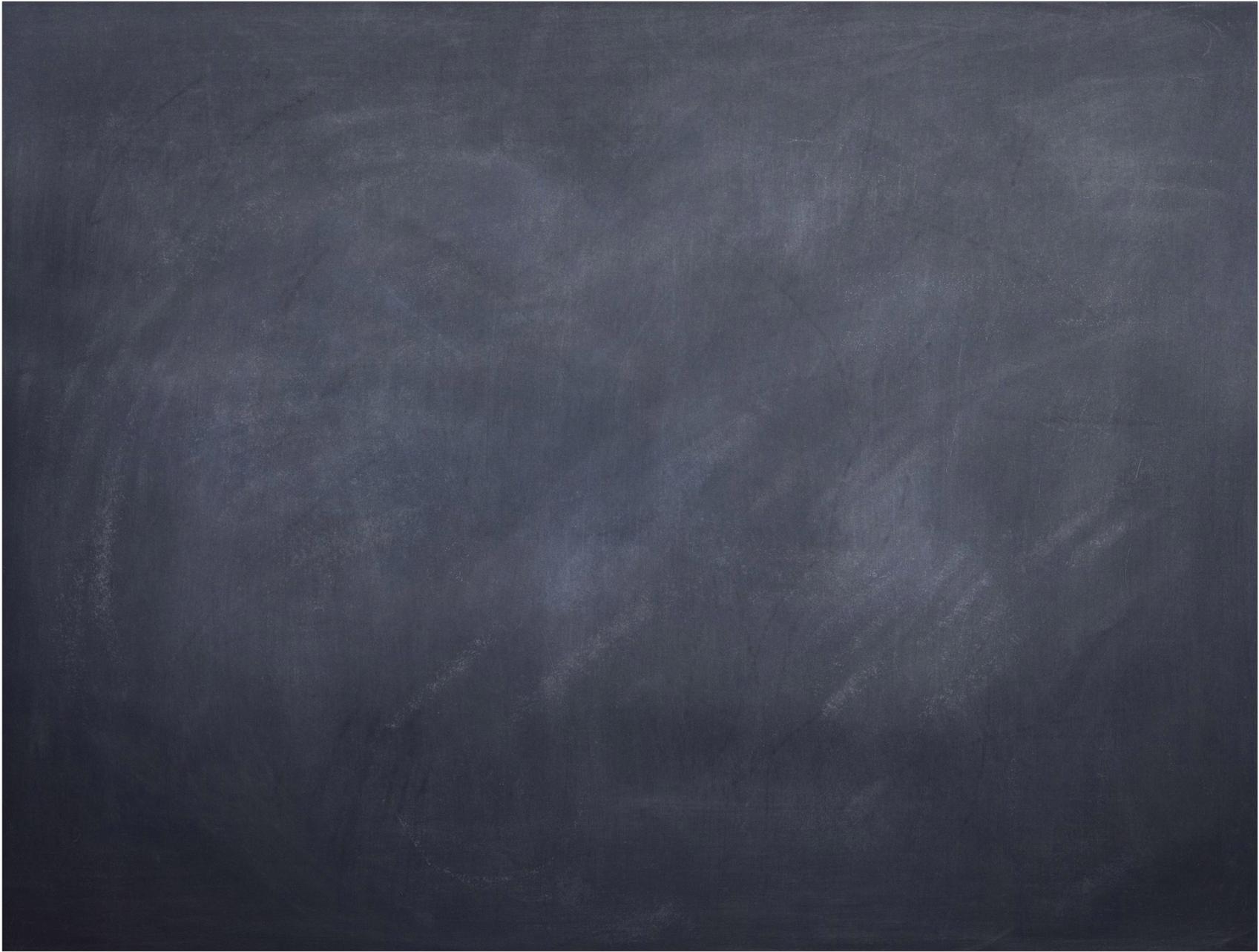


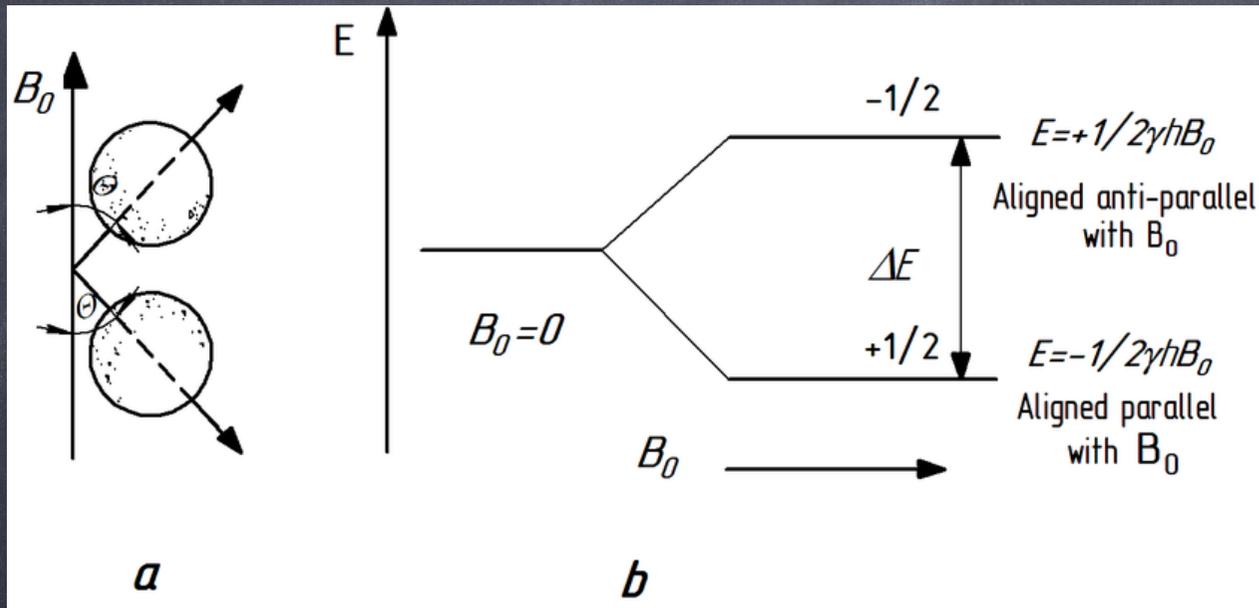


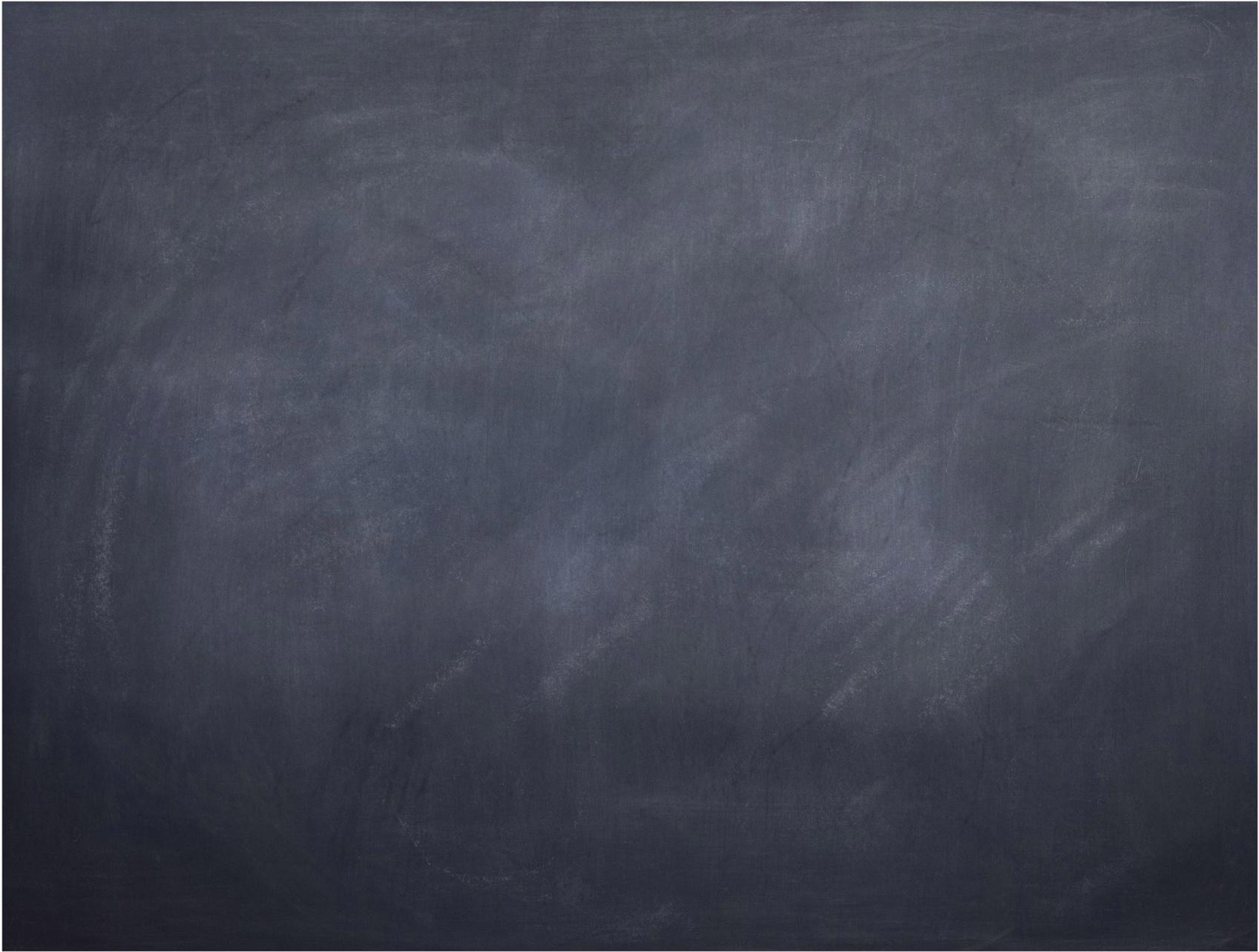


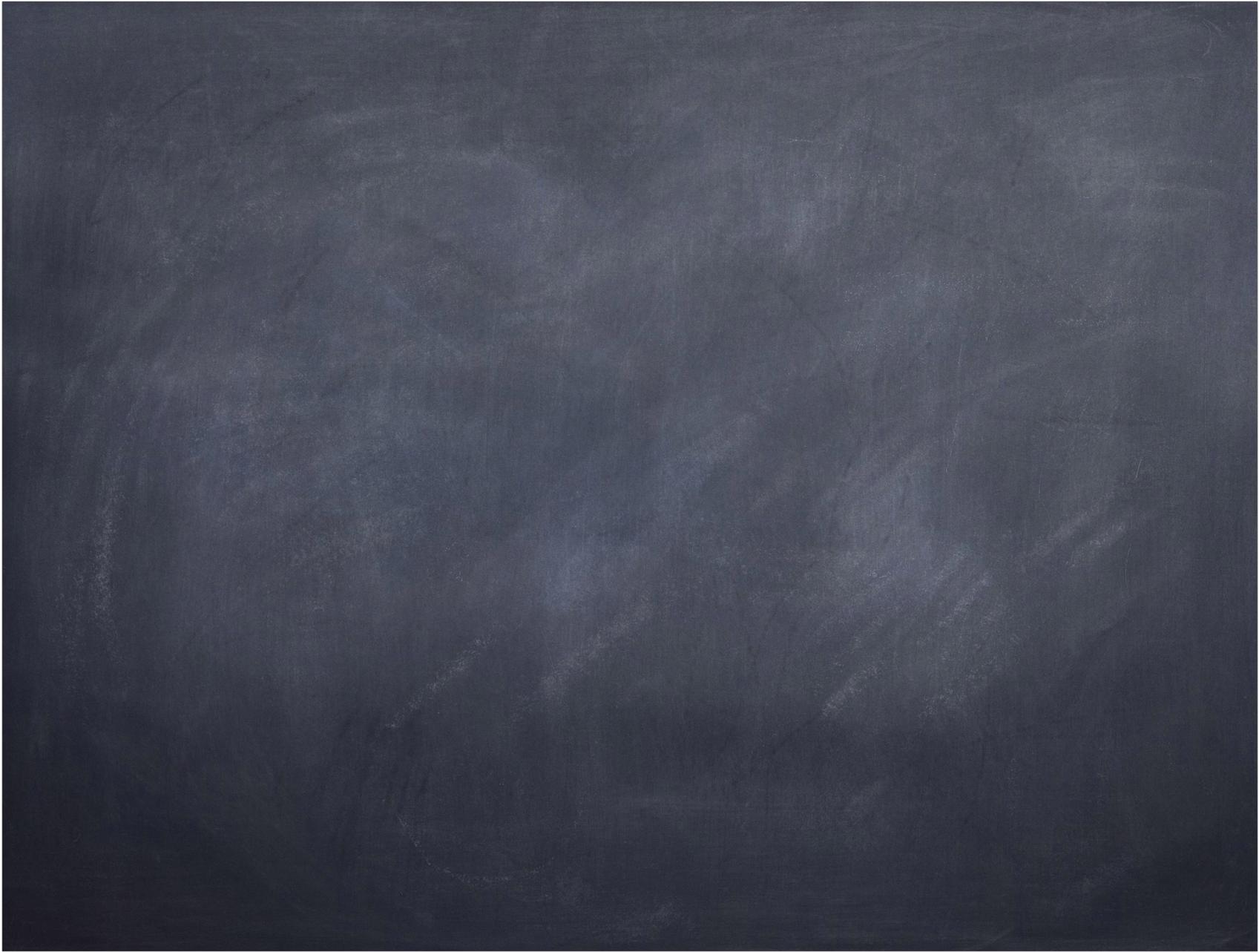










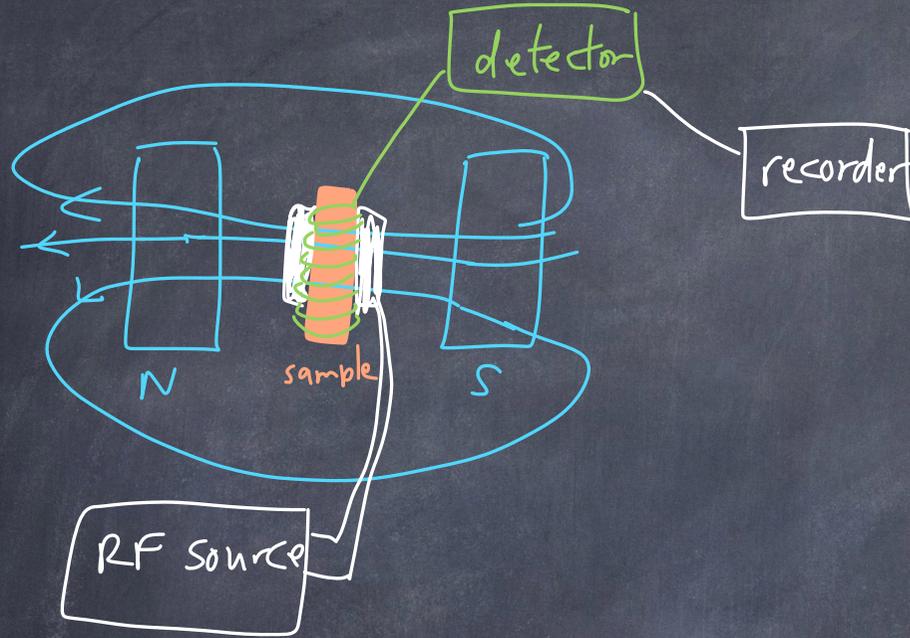


In NMR, RF (radio frequency) is fixed and \bar{B} is varied by small amounts while scanning through for resonance conditions. (see video on wikipedia page)

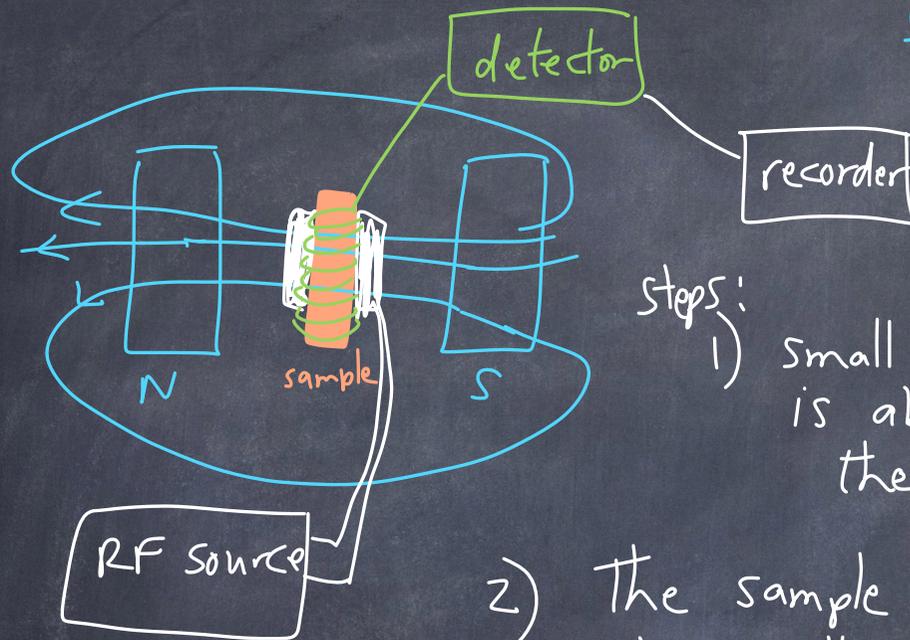
Einstein showed that the same RF photons that can be absorbed, flipping spins to a higher energy state, can with equal probability, flip the nuclear spin to a lower energy state, emitting a second RF photon with energy ΔE .

If $n_{up} + n_{down}$ were equal, there would be no net absorption. But, since there are slightly more nuclei in the n_{down} state than the n_{up} state, there is a slight net absorption of photons. This is our signal for NMR.

How to detect NMR radiation.



How to detect NMR radiation.



sample is placed in a magnetic field

detector is a solenoid that can measure changes in electric current

steps:

1) small amount of RF radiation is absorbed by our sample, then we turn off the RF.

2) The sample returns to equilibrium, by emitting RF energy.

The net magnetic moment of the sample changes, and this can be detected in the solenoidal coil. (This comes from PHY 117 (script 2))

The changing magnetism of the sample induces a electric current in the solenoid. (Faraday's Law)

Next time: how to use NMR to determine molecular structure

