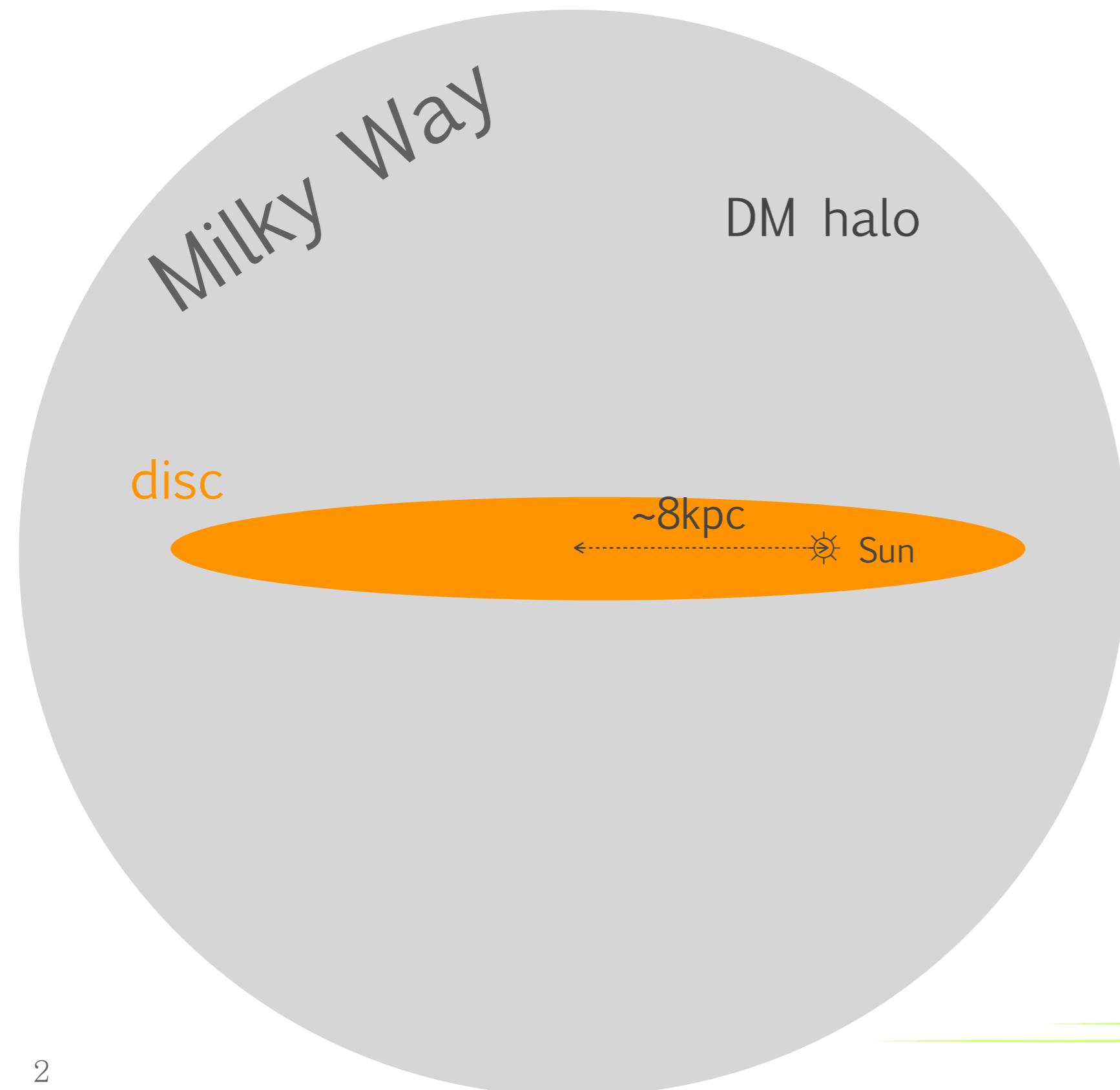




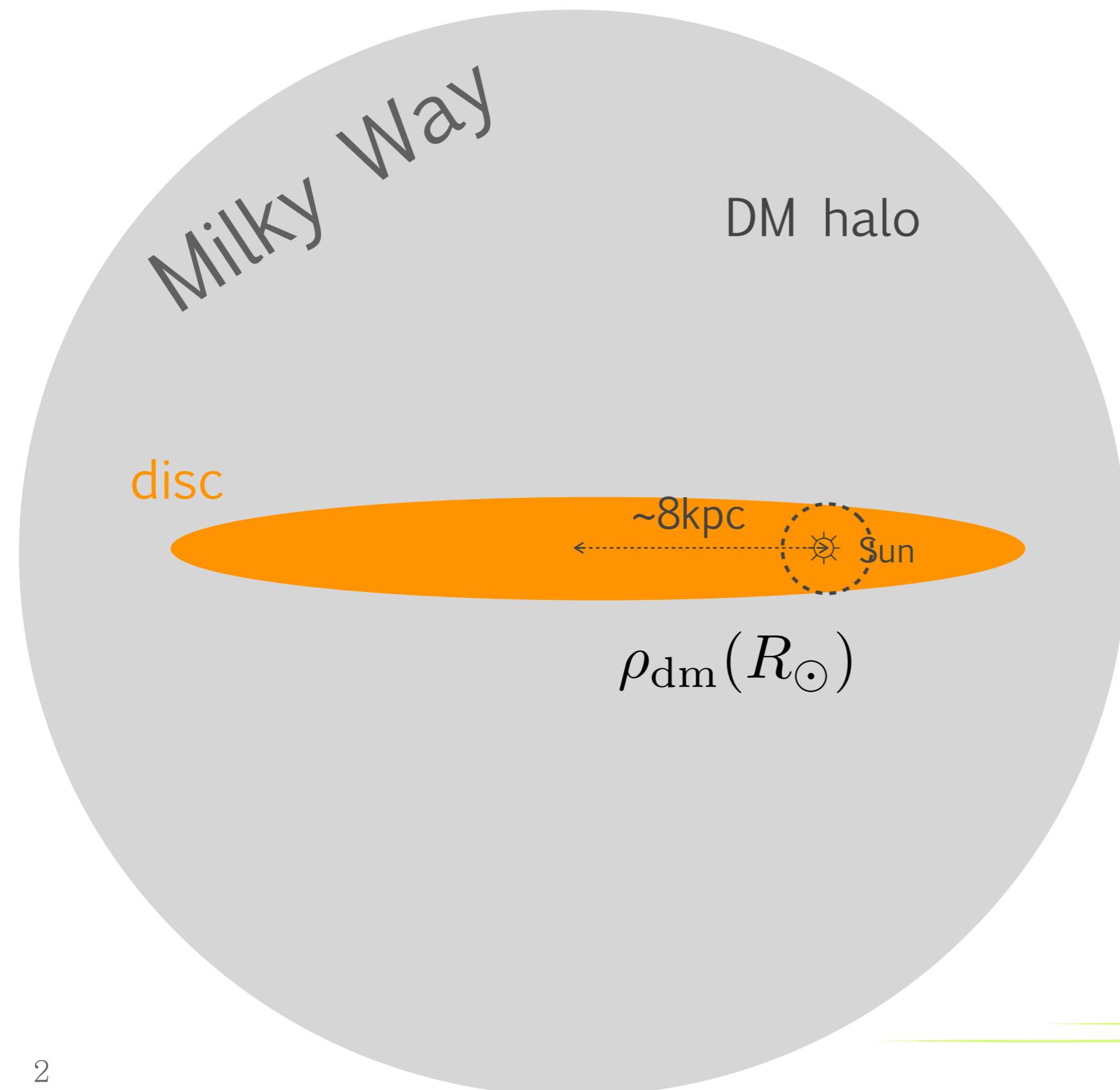
A new measurement of $\rho_{\text{DM}}(R_{\odot})$ from the kinematics of K dwarfs

Silvia Garbari
with Justin Read, George Lake and Chao Liu

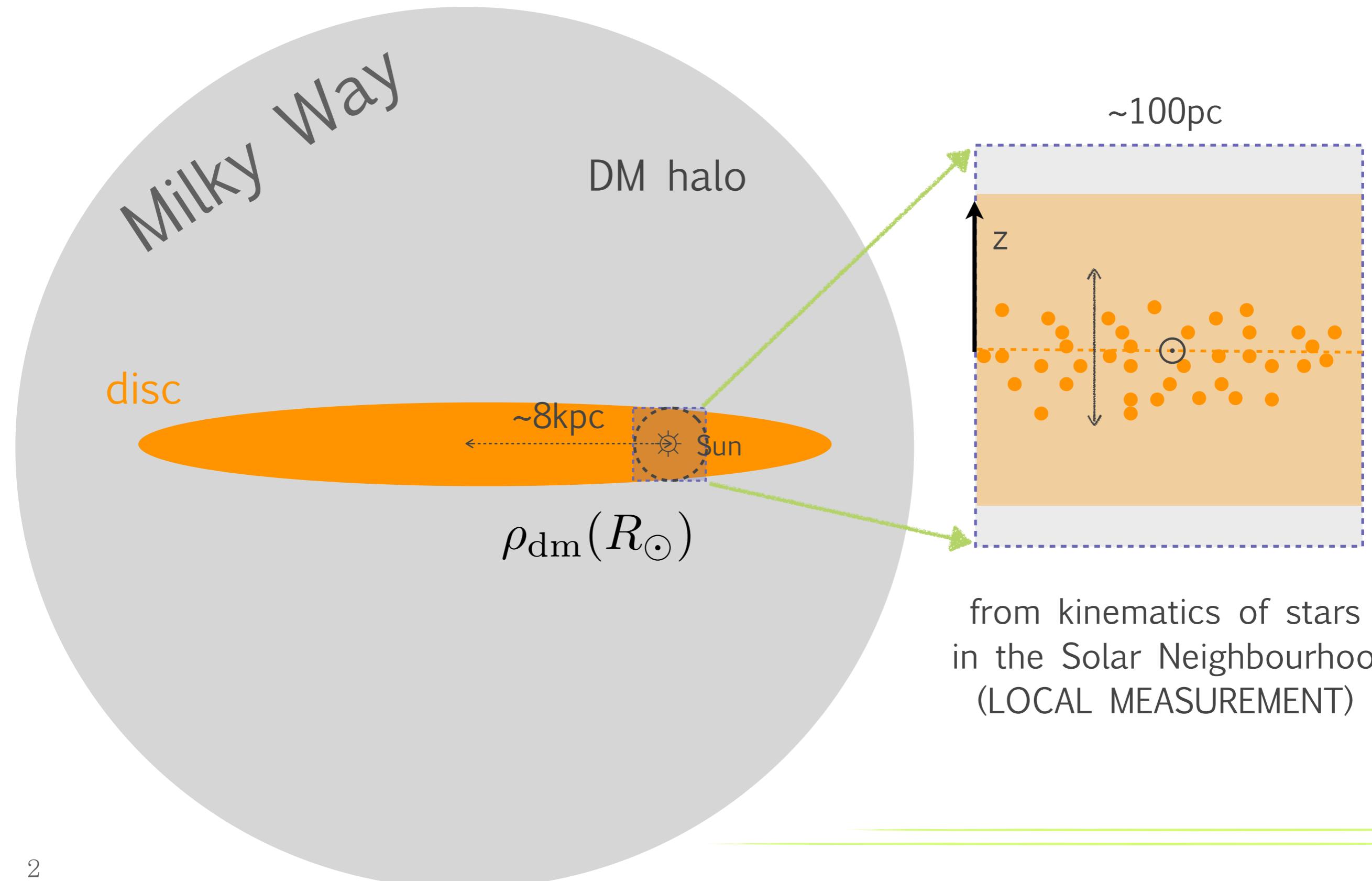
Measuring the local dark matter density $\rho_{\text{DM}}(R_\odot)$



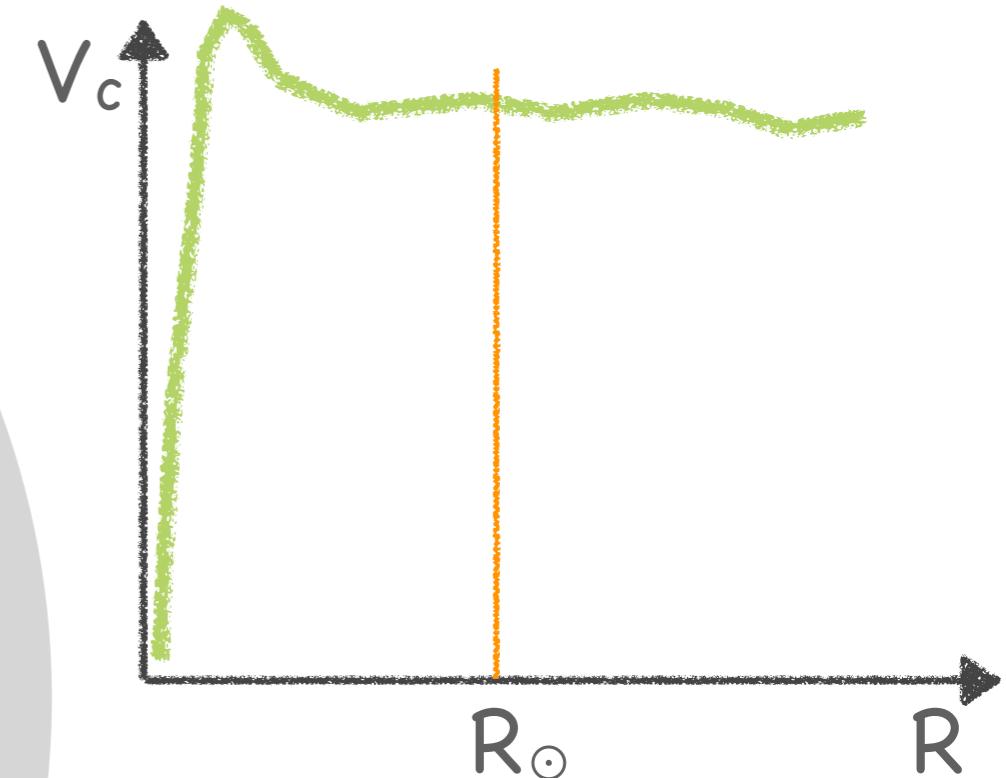
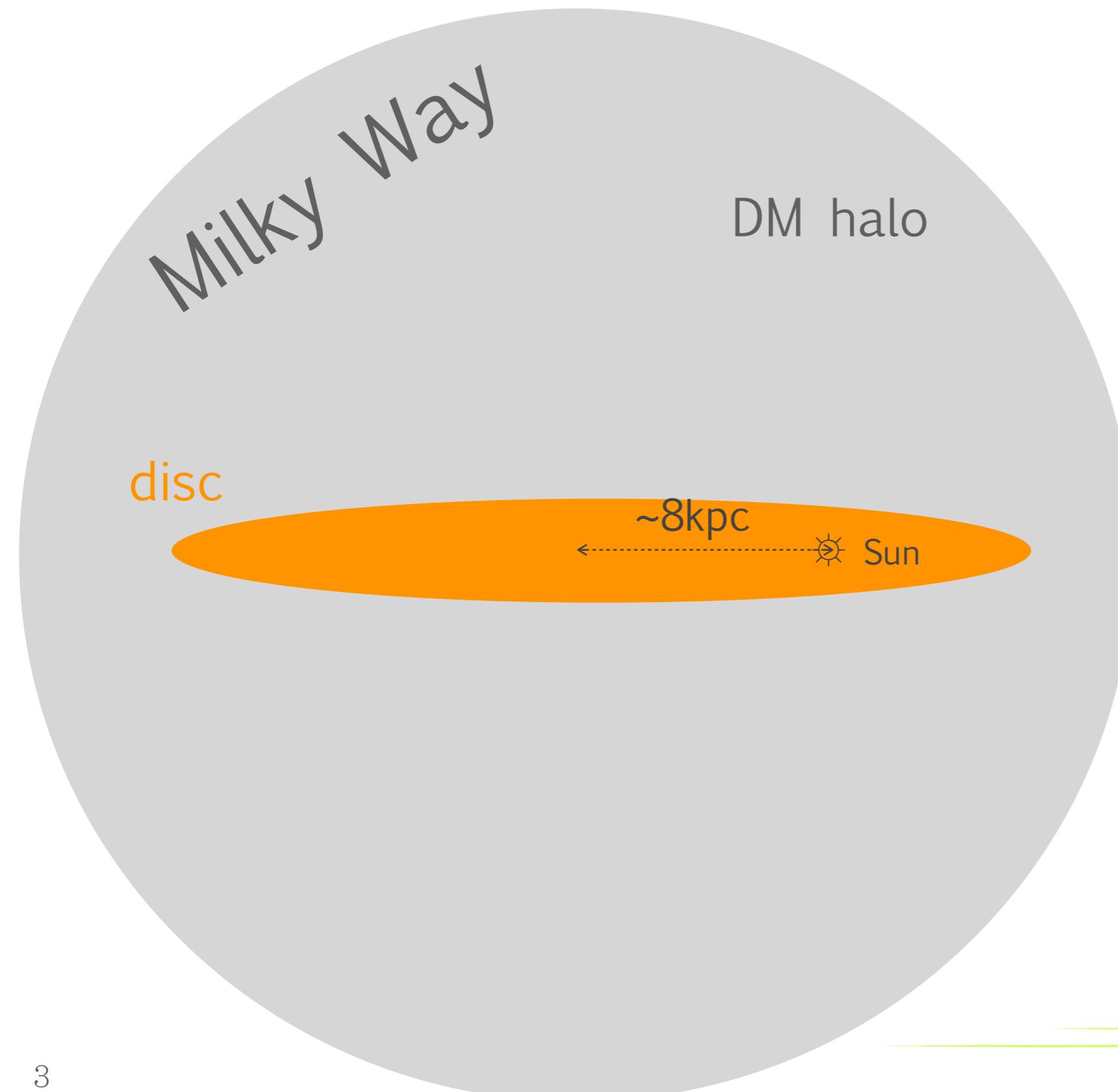
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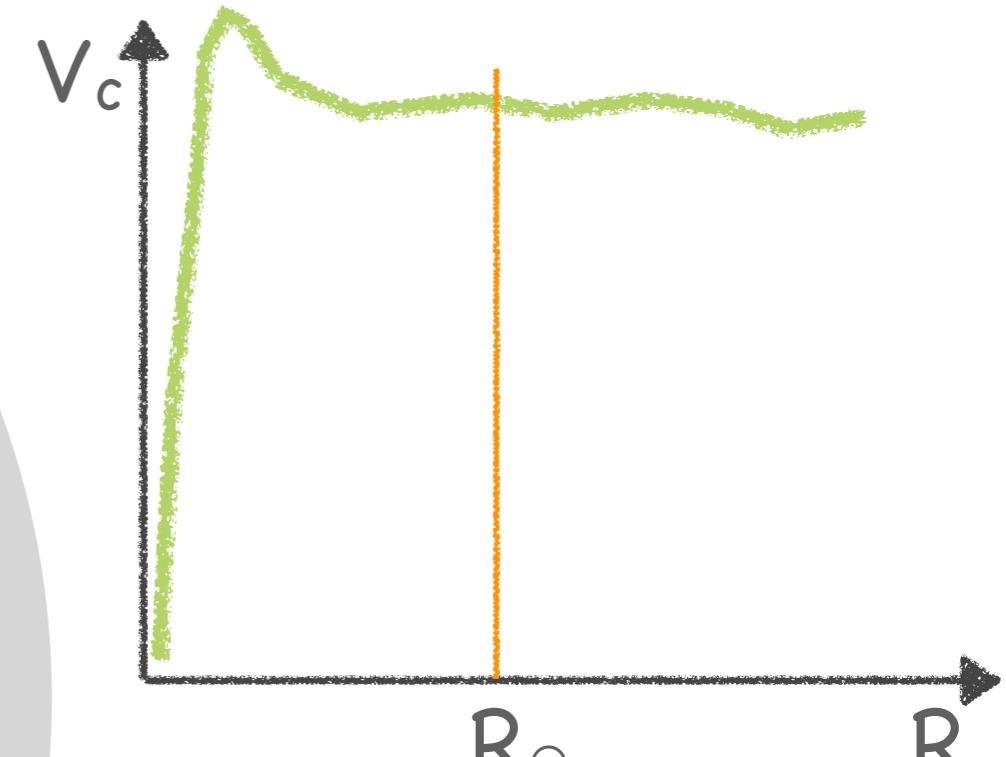
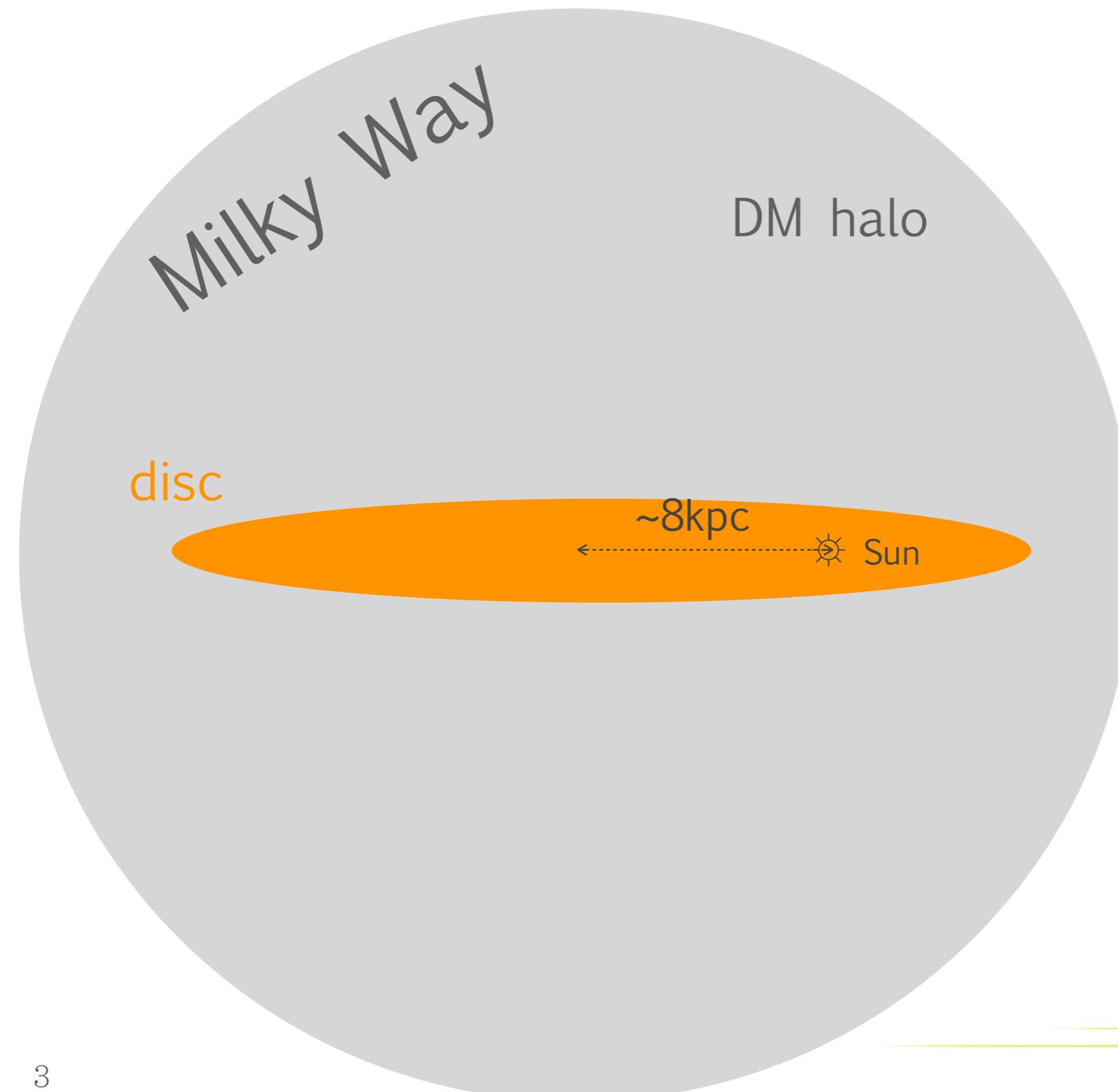
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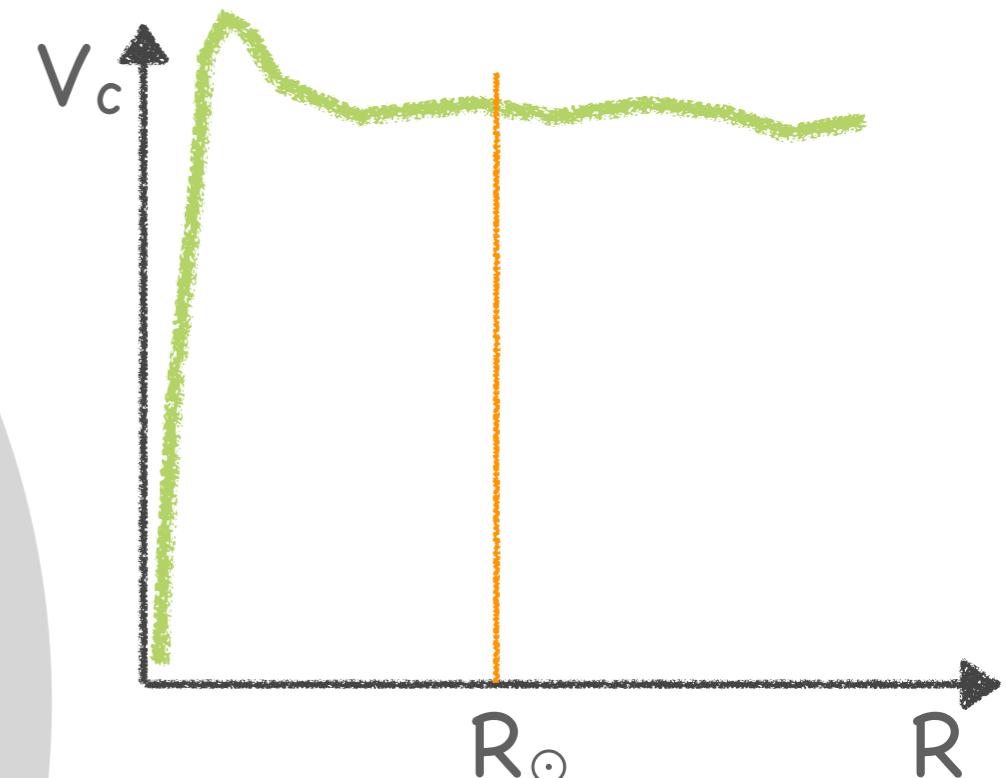
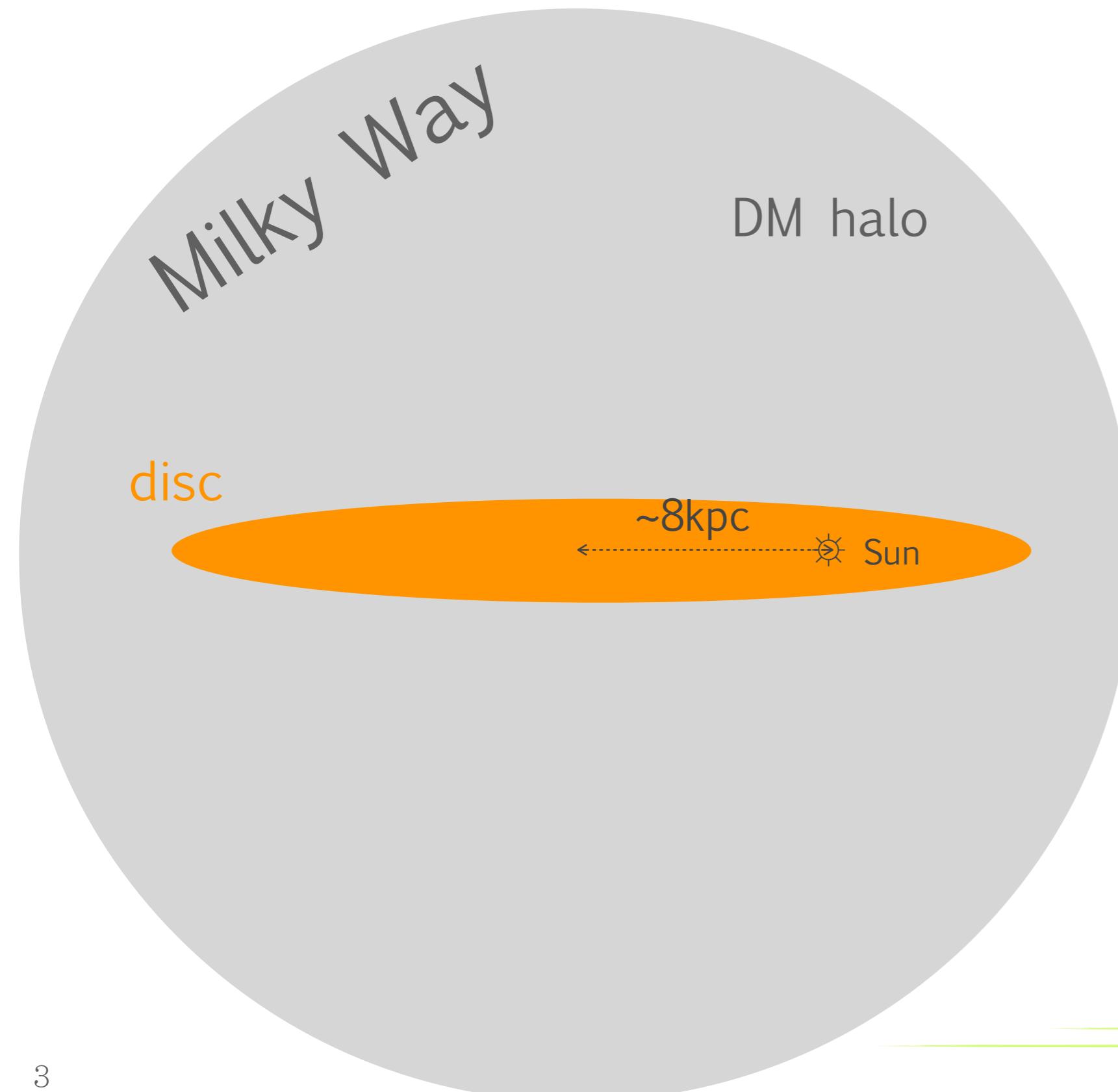
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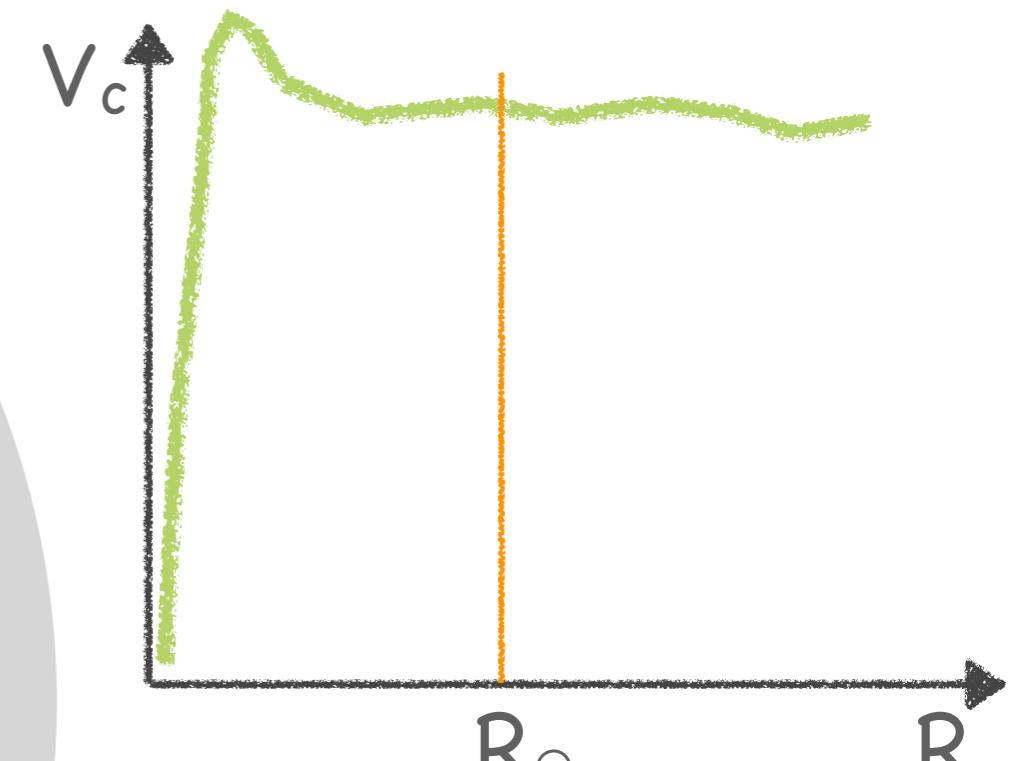
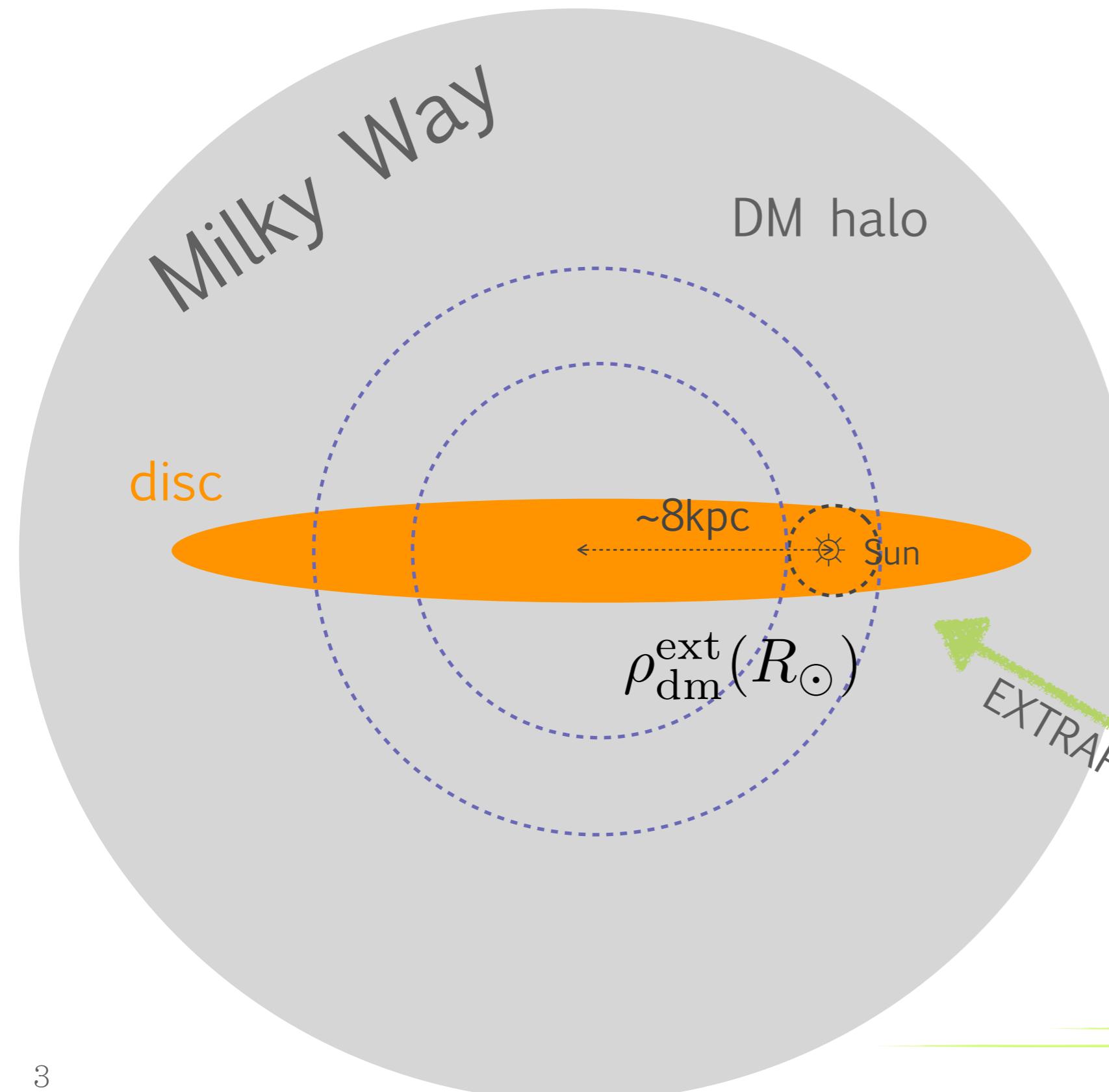


assumptions
on the halo shape

$$V_c^2(R) = \frac{GM}{R}$$

spherical

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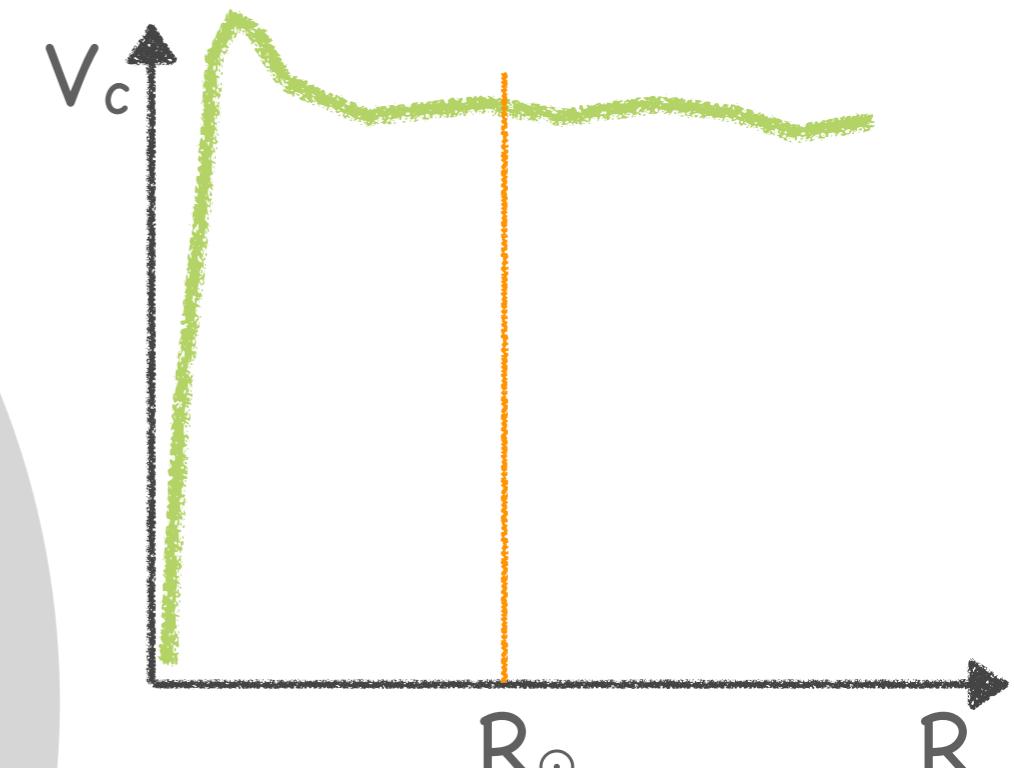
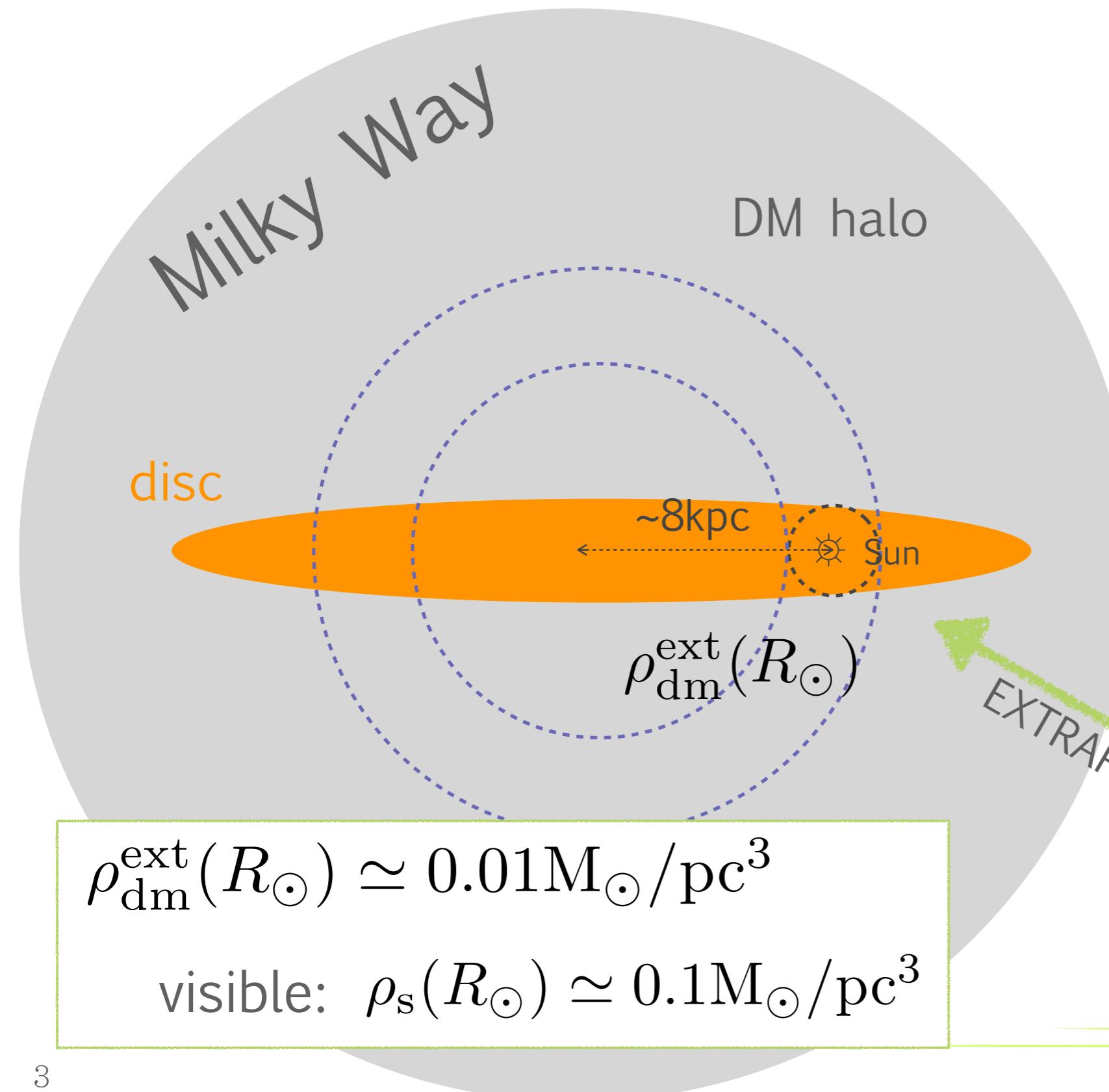


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Why is $\rho_{\text{DM}}(R_\odot)$ interesting?

1. Constraints on the shape of the DM Halo of the MW

spherical halo: $\rho_{\text{dm}}^{\text{ext}}(R_\odot) \simeq 0.01 M_\odot/\text{pc}^3$

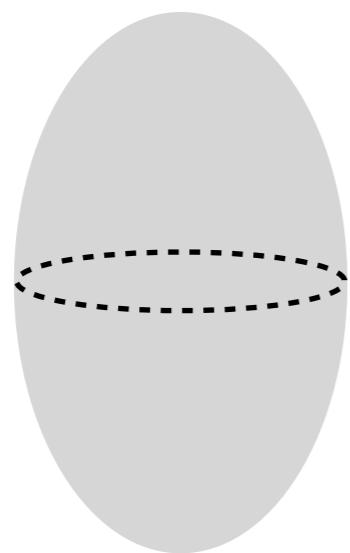
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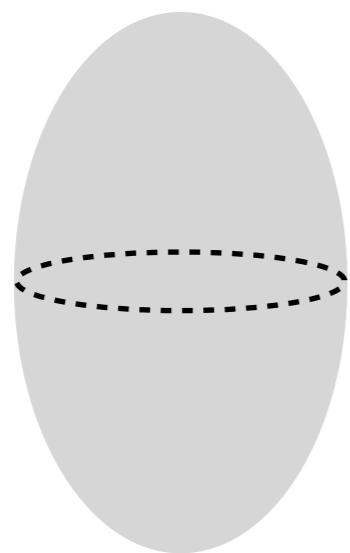
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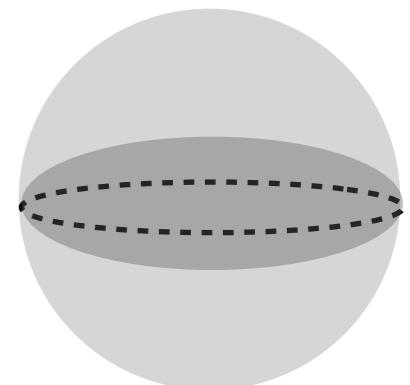
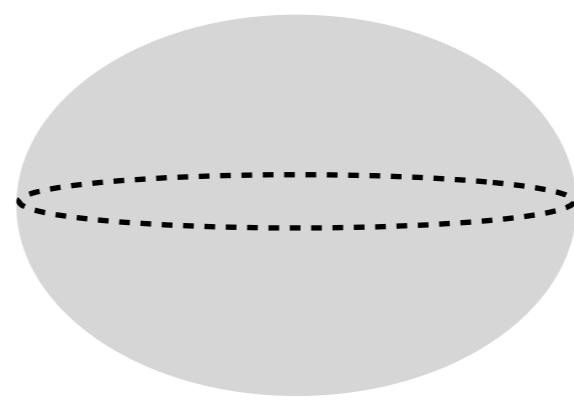
prolate halo



$$\rho_{\text{dm}}(R_\odot) > \rho_{\text{dm}}^{\text{ext}}(R_\odot)$$

oblate halo

(or/and dark disc [Read 2008,2009])



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if DM=WIMP (Weakly Interacting Massive Particles)

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nuclear recoil caused by a WIMP scattering within the detector

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what we want to measure

Minimal Assumption Method

$$\frac{df}{dt} = 0 = \frac{\partial f}{\partial t} + \mathbf{v} \cdot \frac{\partial f}{\partial \mathbf{r}} - \nabla \Phi \cdot \frac{\partial f}{\partial \mathbf{v}}$$

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Moments =
Jeans equations

$$\frac{1}{R} \frac{\partial}{\partial R} (R \nu_i \bar{v}_R \bar{v}_z) + \frac{\partial}{\partial z} \left(\nu_i \bar{v}_z^2 \right) + \nu_i \frac{\partial \Phi}{\partial z} = 0$$

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hyp. 2: tilt term is negligible

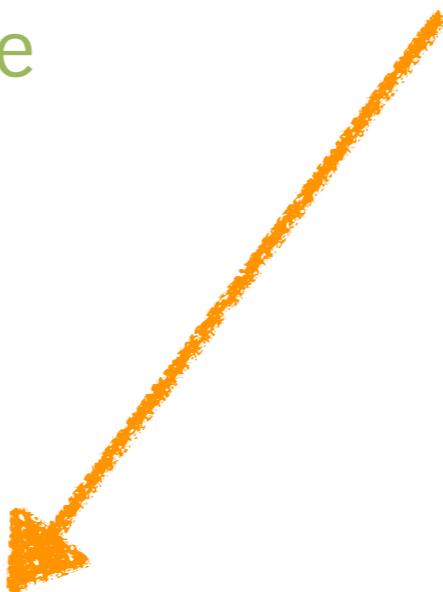
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negligible

$$\frac{1}{R} \frac{\partial}{\partial R} \left(R \frac{\partial \Phi}{\partial R} \right) = \frac{1}{R} \frac{\partial V_c^2}{\partial R} = 2(B^2 - A^2)$$

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hyp. 5: the distribution function is separable

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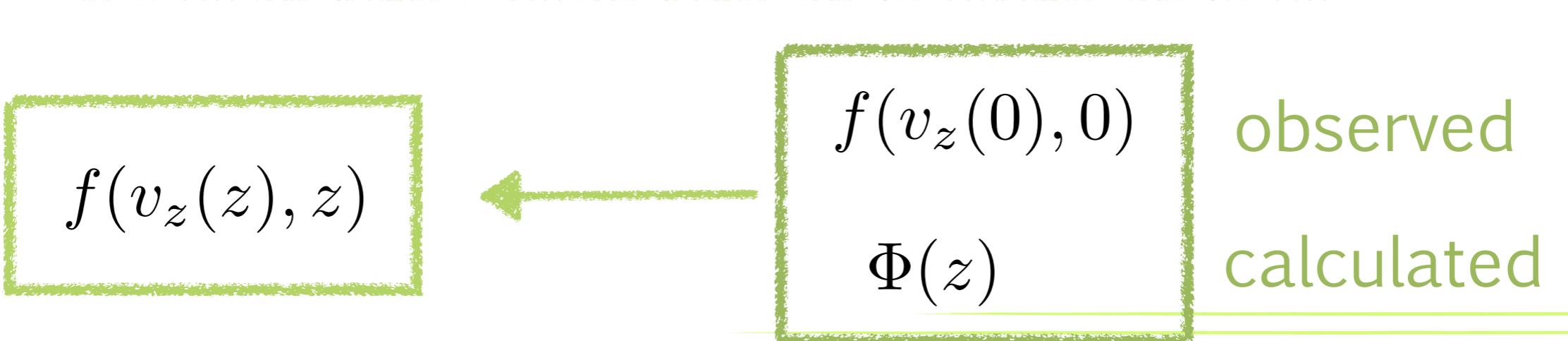
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Testing the methods with simulations

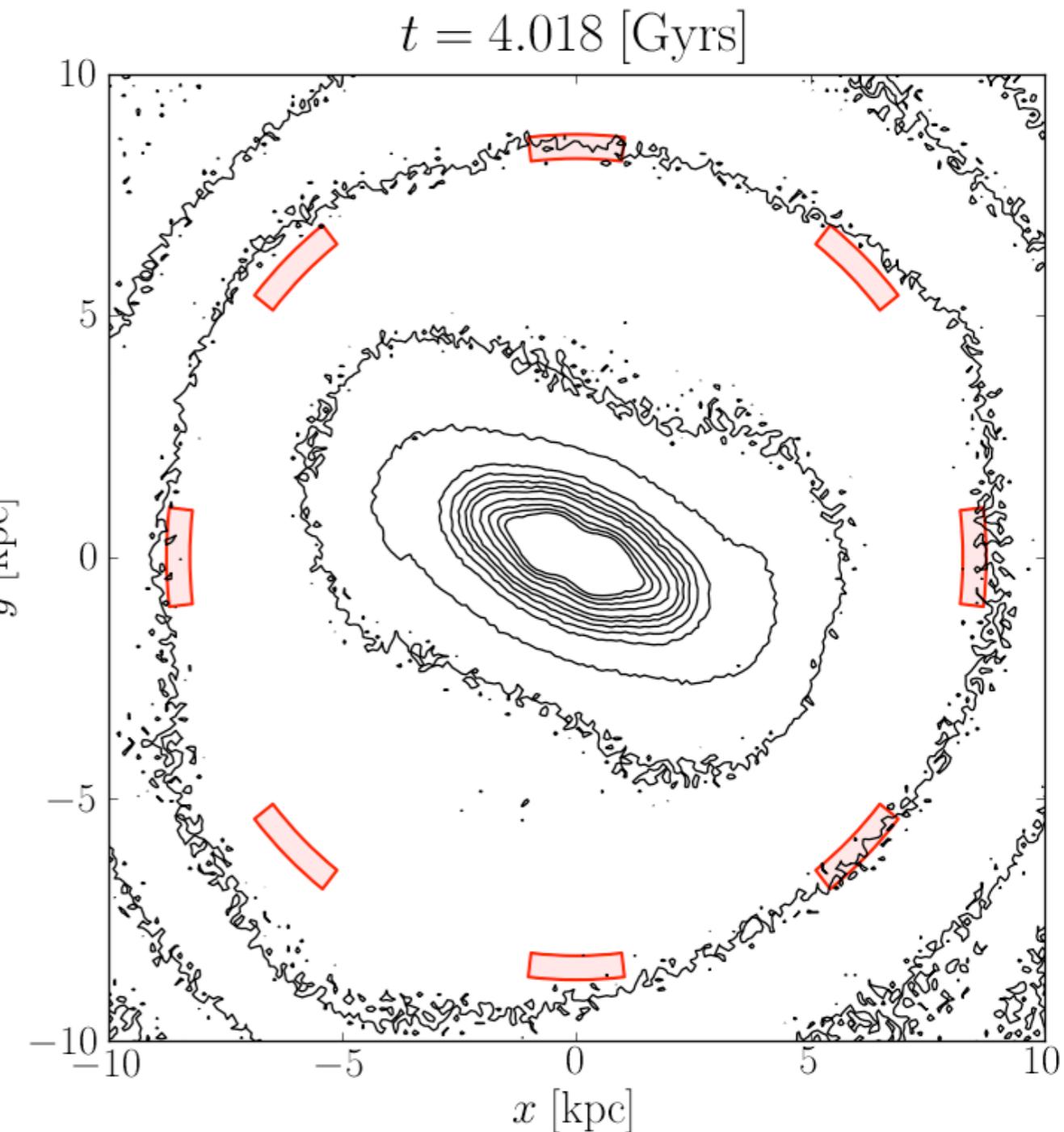
simulation

	N (10^6)	M ($10^{10} M_\odot$)	ε (kpc)	$R_{1/2}$ (kpc)	$z_{1/2}$ (kpc)
Disc	30	5.30	0.015	4.99	0.17
Bulge	0.5	0.83	0.012	–	–
Halo	15	45.40	0.045	–	–

Milky Way

	M ($10^{10} M_\odot$)	$R_{1/2}$ (kpc)	$z_{1/2}$ (kpc)
Thin disc	3.5–5.5 ^a	3.35–9.24	~0.14–0.18
Thick disc	–	5.04–7.56	0.49–0.84
Bulge	~1	–	–
Halo	~40–200	–	–

^aTotal disc mass.



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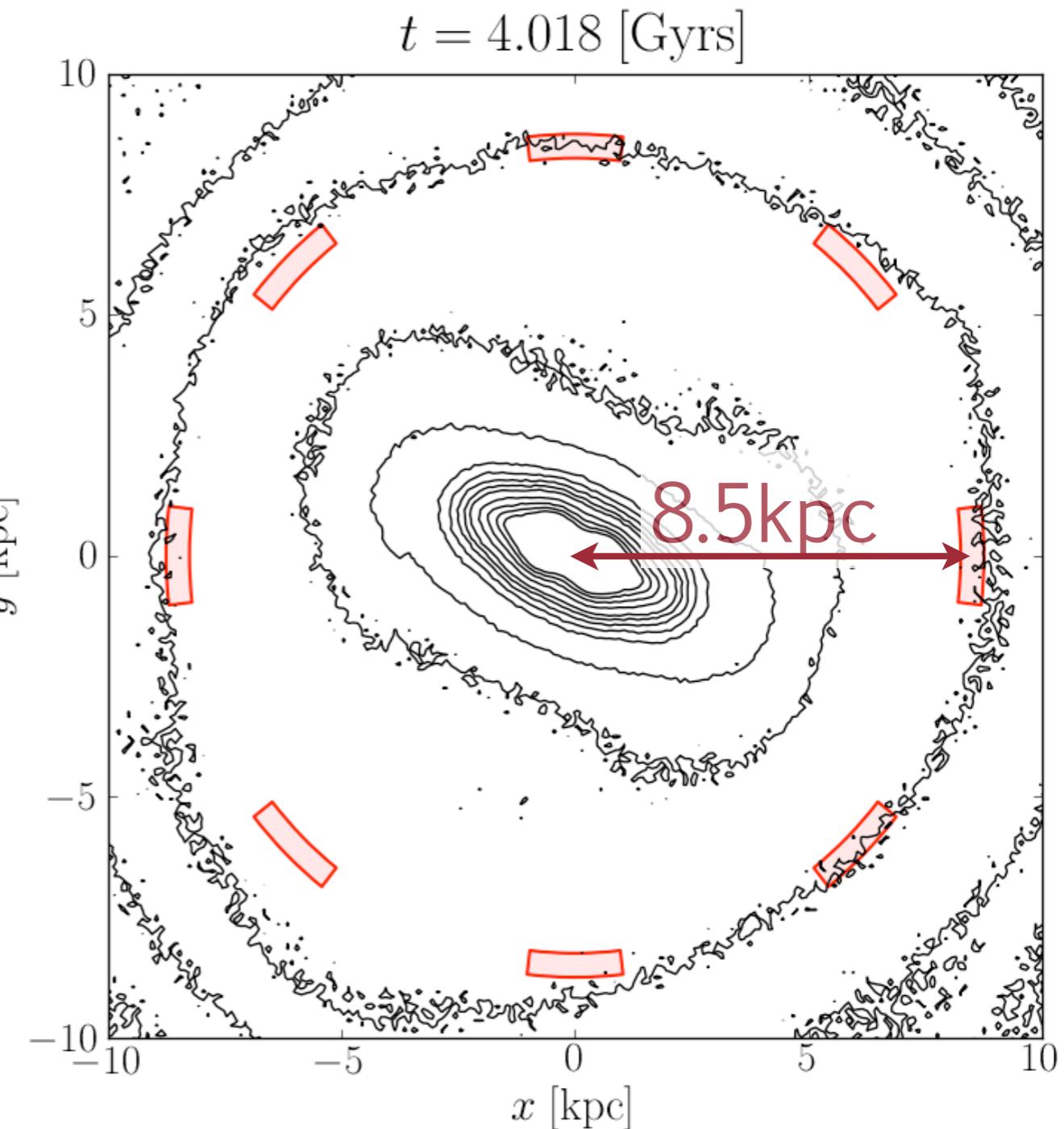
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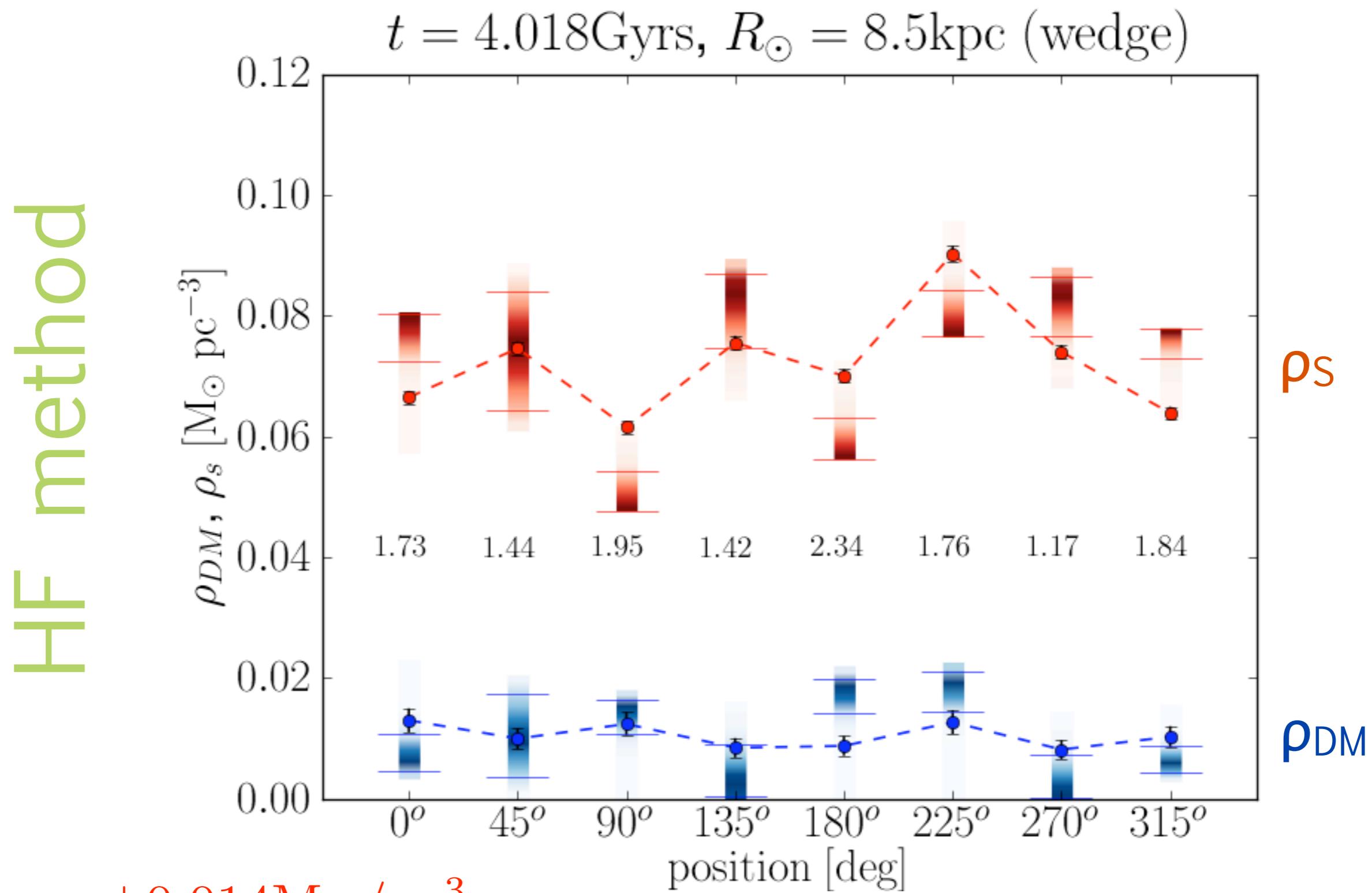
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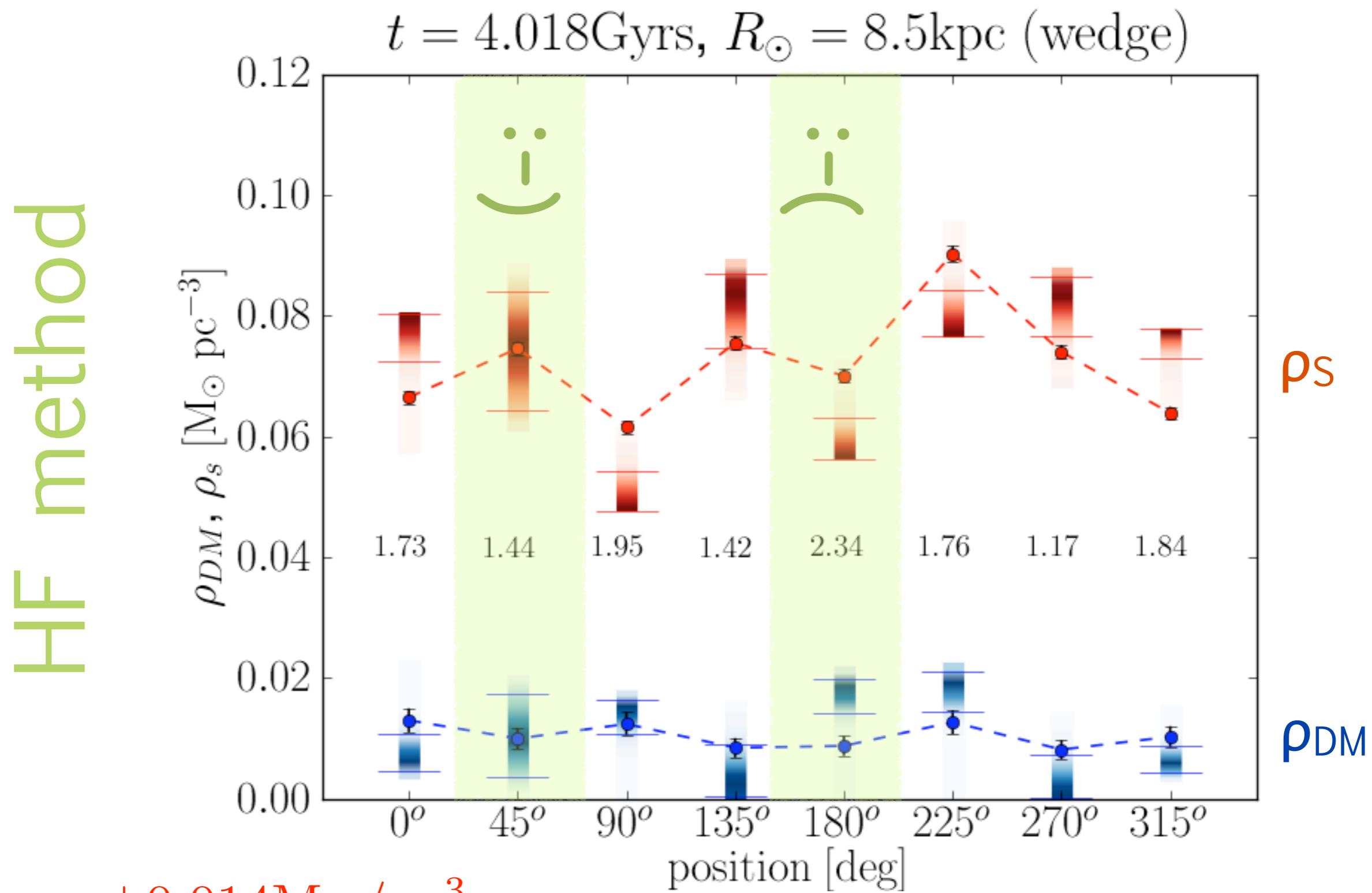
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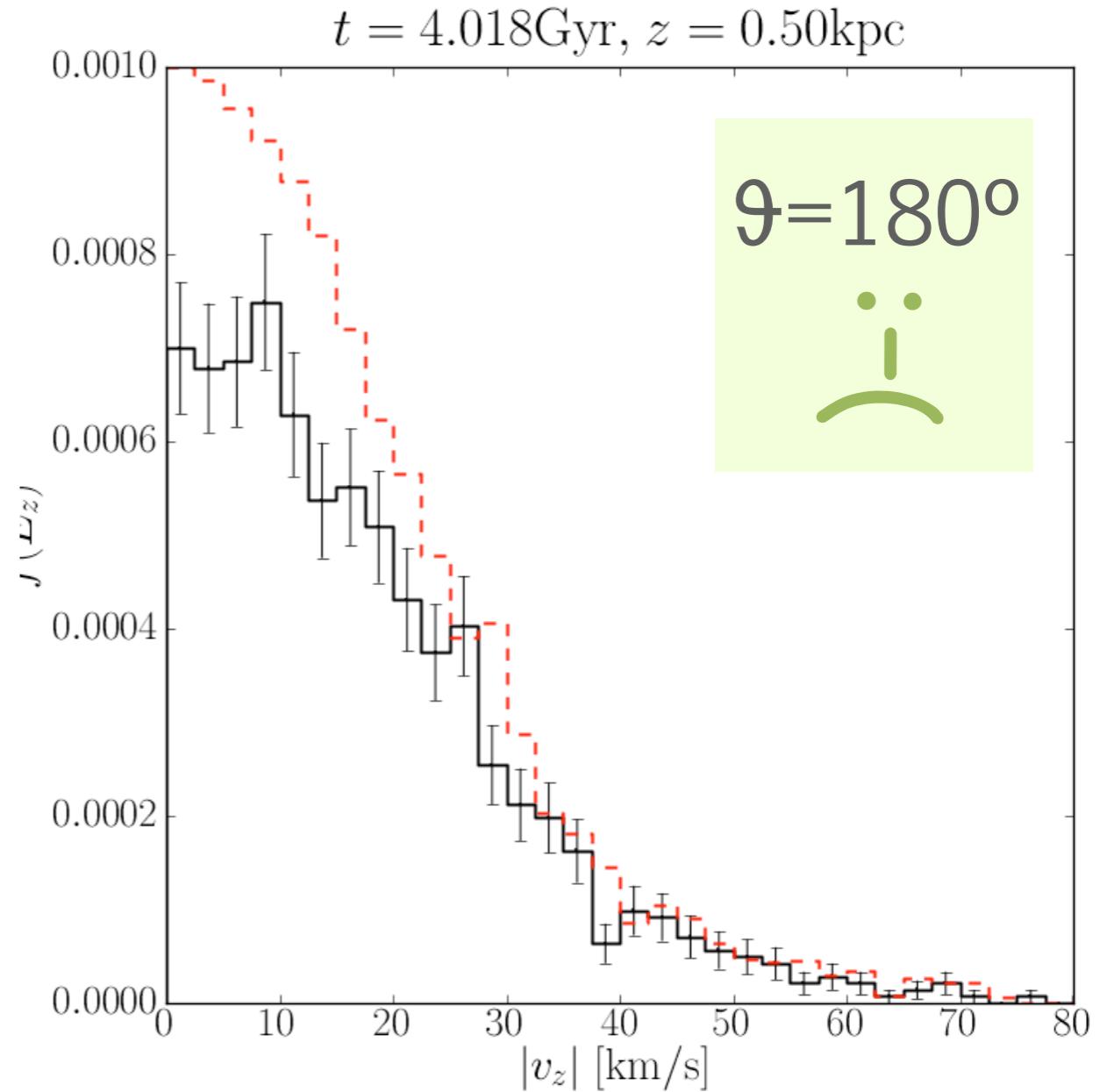
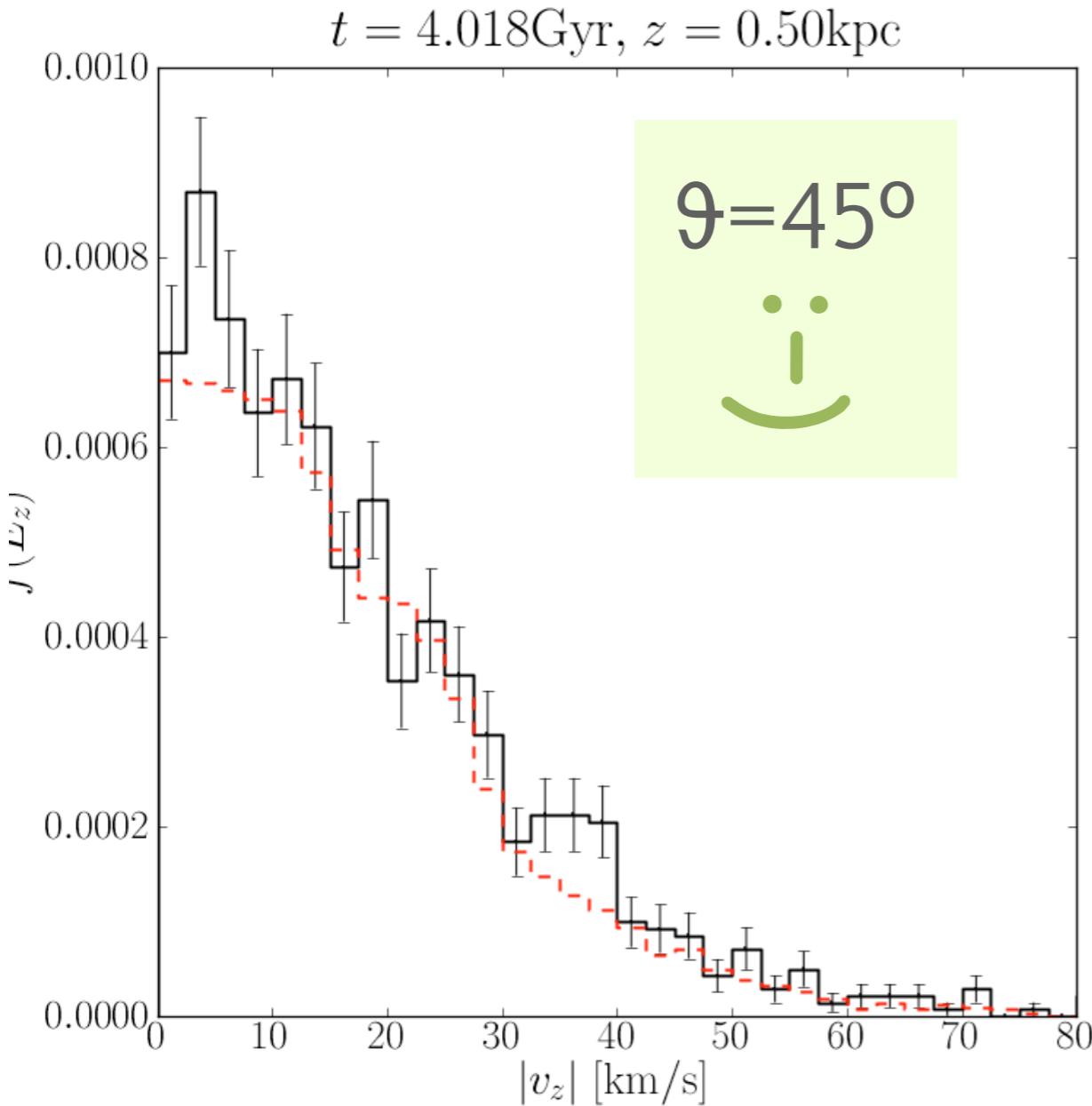
Evolved sim: HF vs MA method



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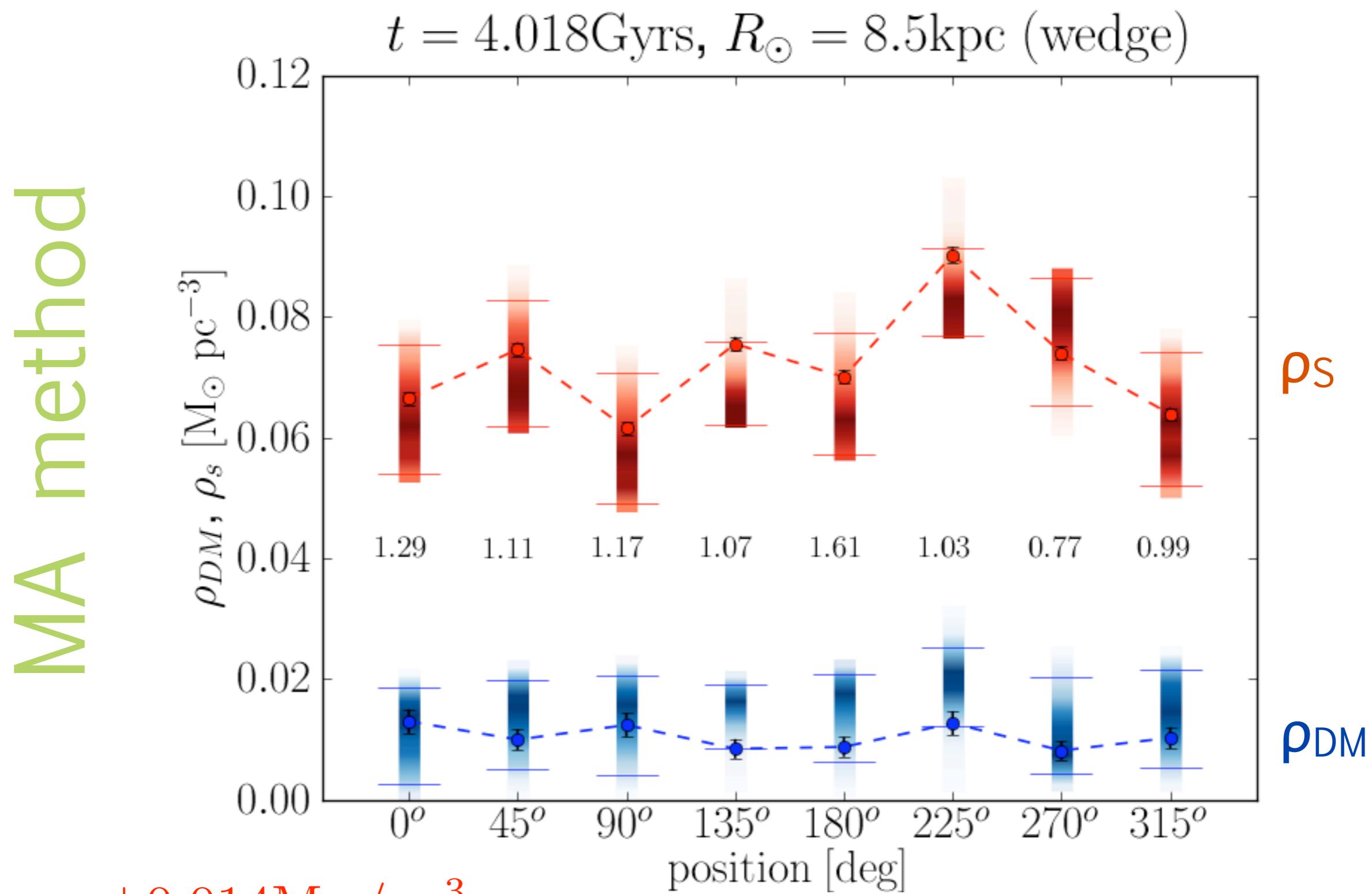


Evolved sim: distribution functions



Evolved simulation

Evolved sim: HF vs MA method



Tracer population

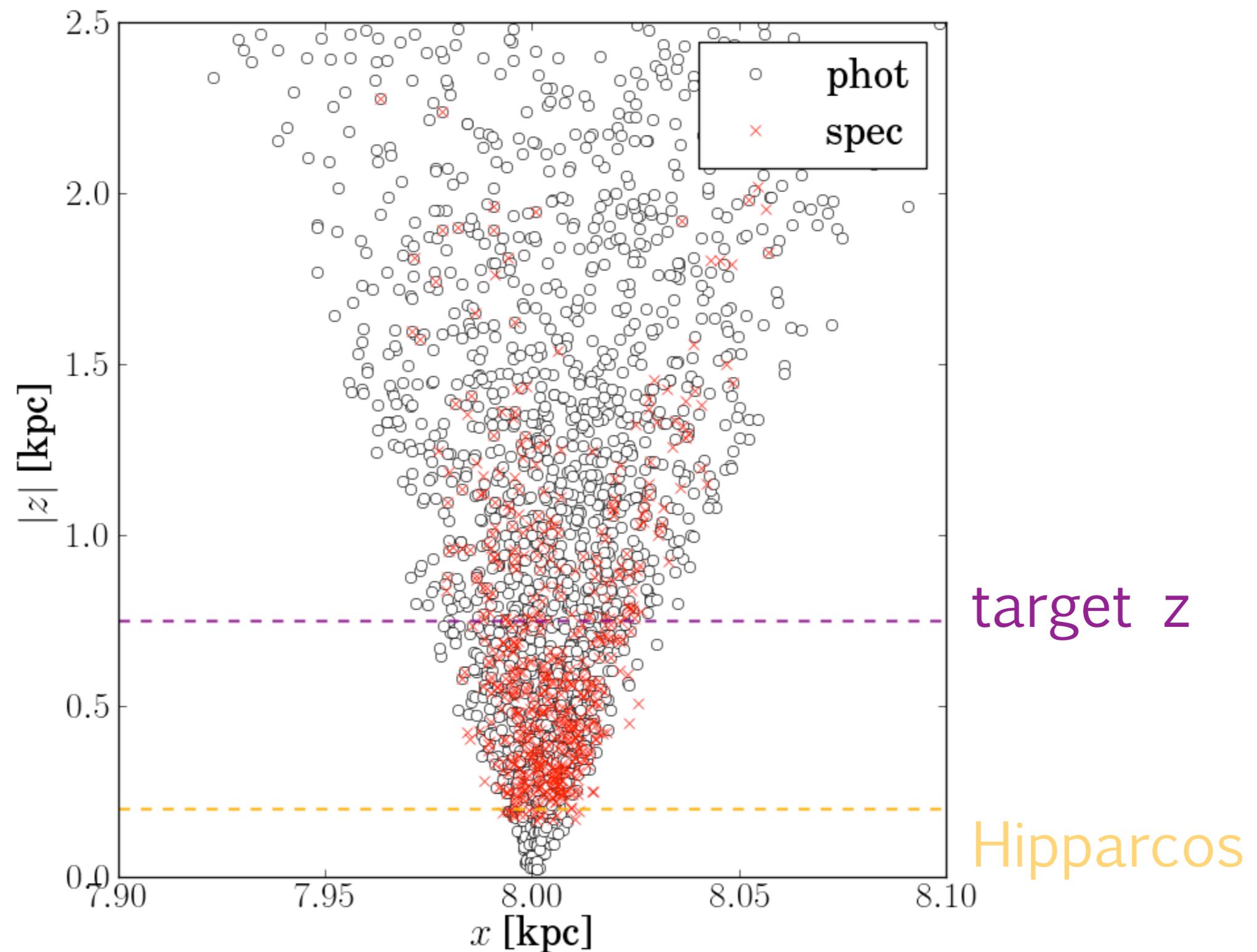
MUST BE:

- * in dynamical equilibrium with the Galactic potential.
- * common stars (to allow useful statistical precision in the result).
- * in a volume complete sample.
- * with reliable distances and vertical velocity available.

DATA: from Kuijken & Gilmore 1989 - K dwarfs

photometric
sample
~2000 stars

spectroscopic
sample ~600
stars

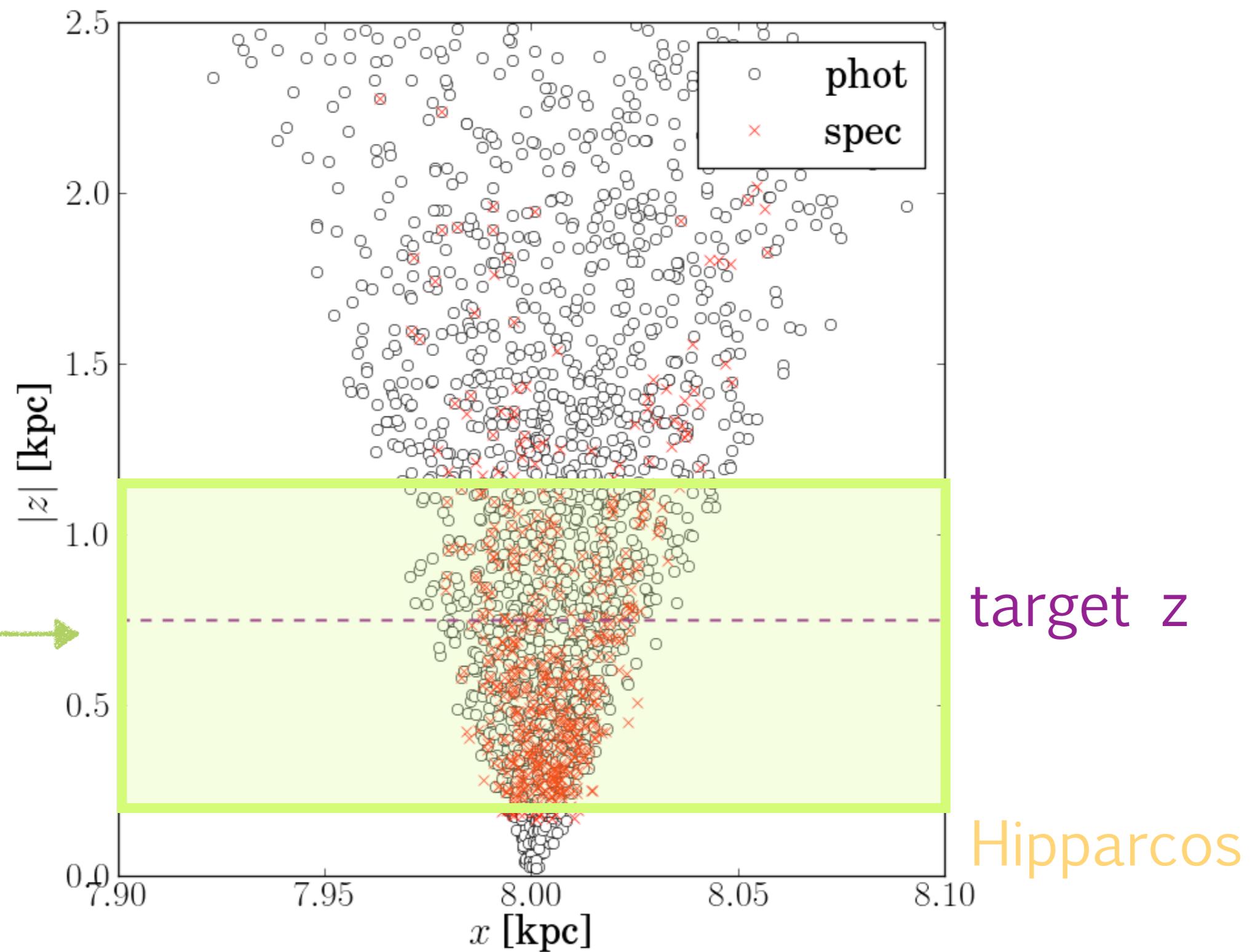


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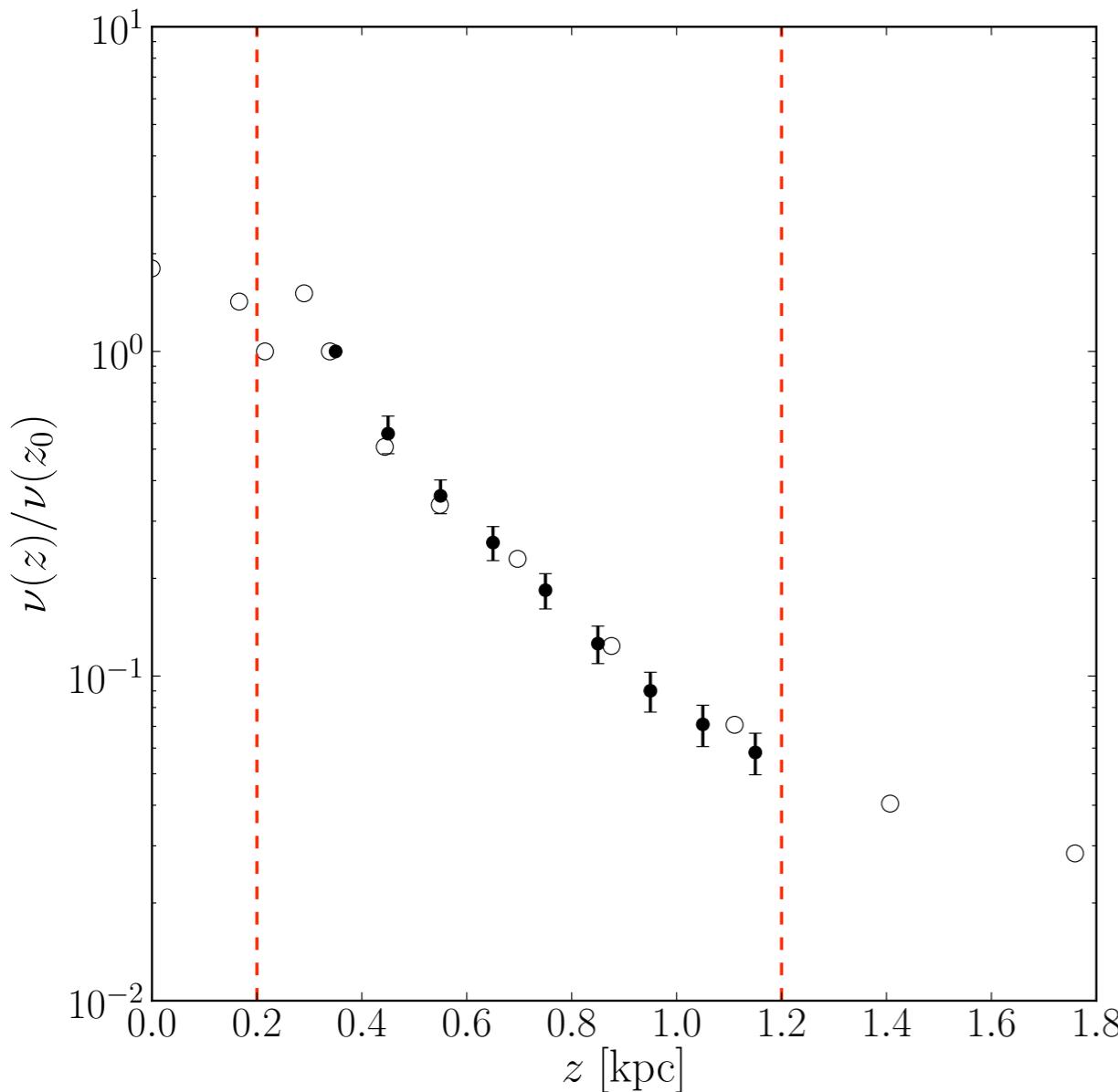
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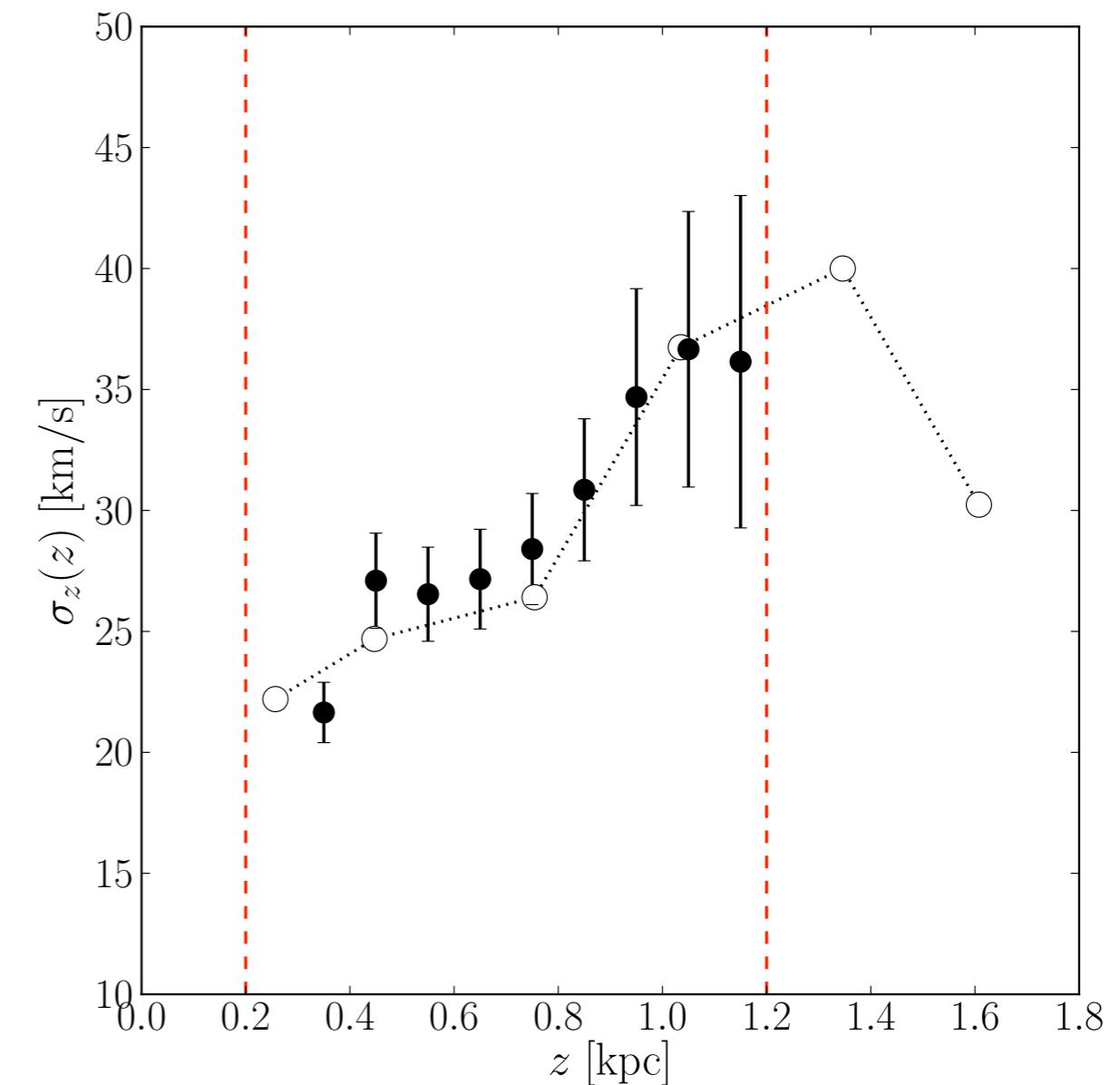
Volume
complete
photometric
sample



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Visible mass model by Flynn et al 2006

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density errors:
 Stars: 10-20%;
 Gas*: 50%

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HI(1)*	0.016	7.0 \pm 1.0
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Warm gas*	0.0009	40.0 \pm 1.0
Giants	0.0006	20.0 \pm 2.0
$M_V < 2.5$	0.0031	7.5 \pm 2.0
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$3.0 < M_V < 4.0$	0.0020	14.0 \pm 2.0
$4.0 < M_V < 5.0$	0.0022	18.0 \pm 2.0
$5.0 < M_V < 8.0$	0.007	18.5 \pm 2.0
$M_V > 8.0$	0.0135	18.5 \pm 2.0
White dwarfs	0.006	20.0 \pm 5.0
Brown dwarfs	0.002	20.0 \pm 5.0
Thick disc	0.0035	37.0 \pm 5.0
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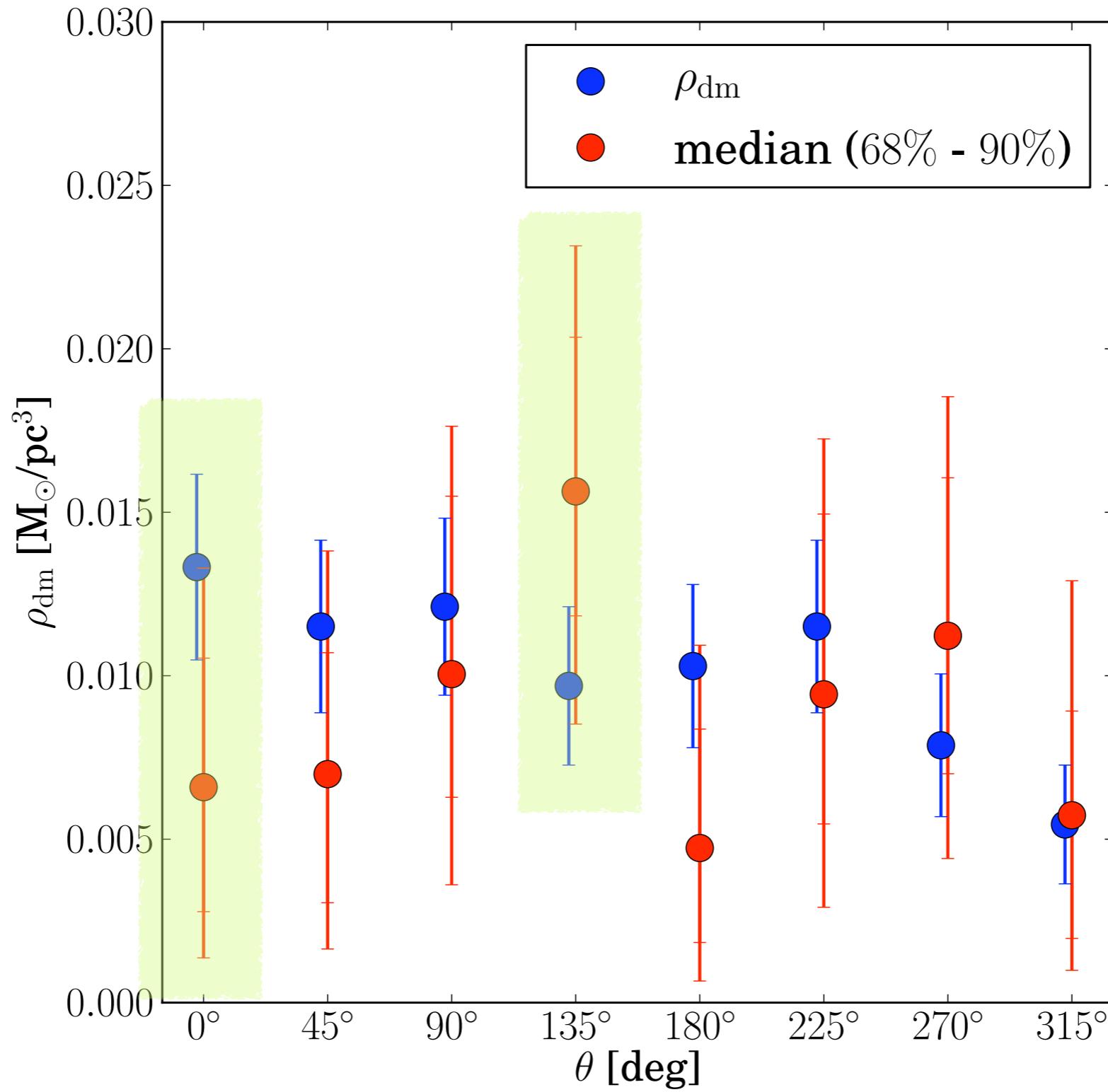
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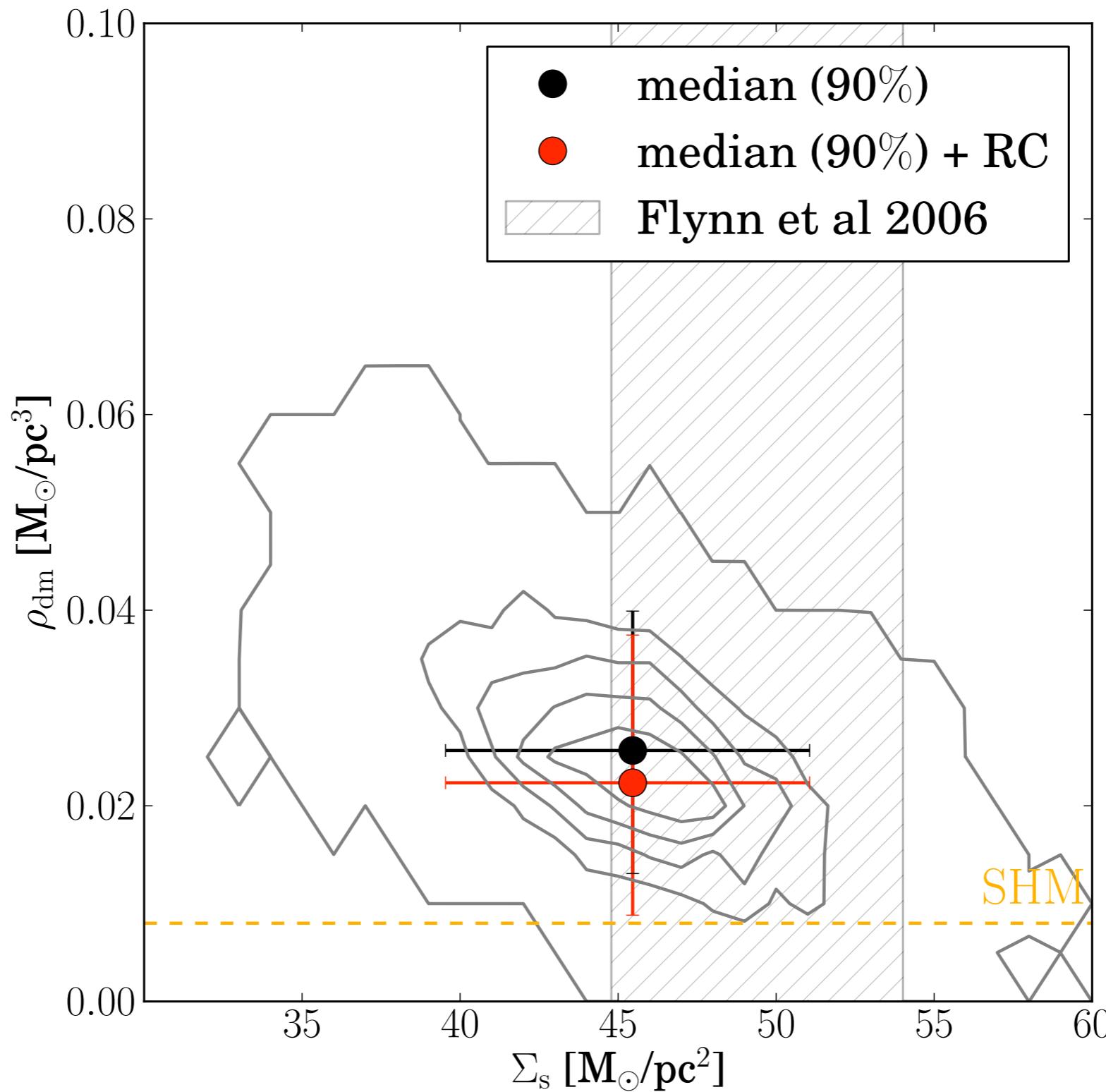
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$2.5 < M_V < 3.0$	0.0015	10.5 \pm 2.0
$3.0 < M_V < 4.0$	0.0020	14.0 \pm 2.0
$4.0 < M_V < 5.0$	0.0022	18.0 \pm 2.0
$5.0 < M_V < 8.0$	0.007	18.5 \pm 2.0
$M_V > 8.0$	0.0135	18.5 \pm 2.0
White dwarfs	0.006	20.0 \pm 5.0
Brown dwarfs	0.002	20.0 \pm 5.0
Thick disc	0.0035	37.0 \pm 5.0
Stellar halo	0.0001	100.0 \pm 10.0

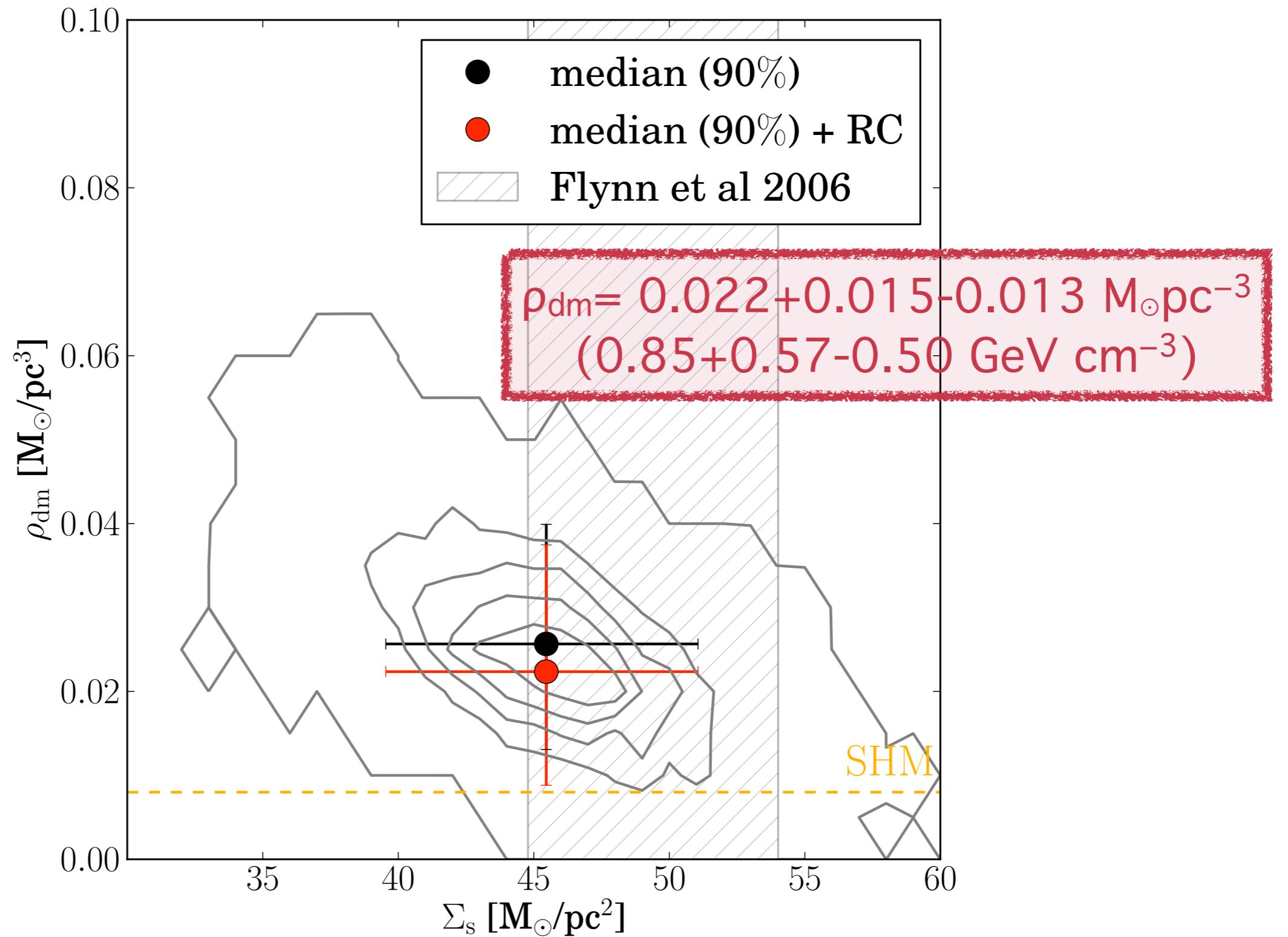
Test on the simulation: MA method



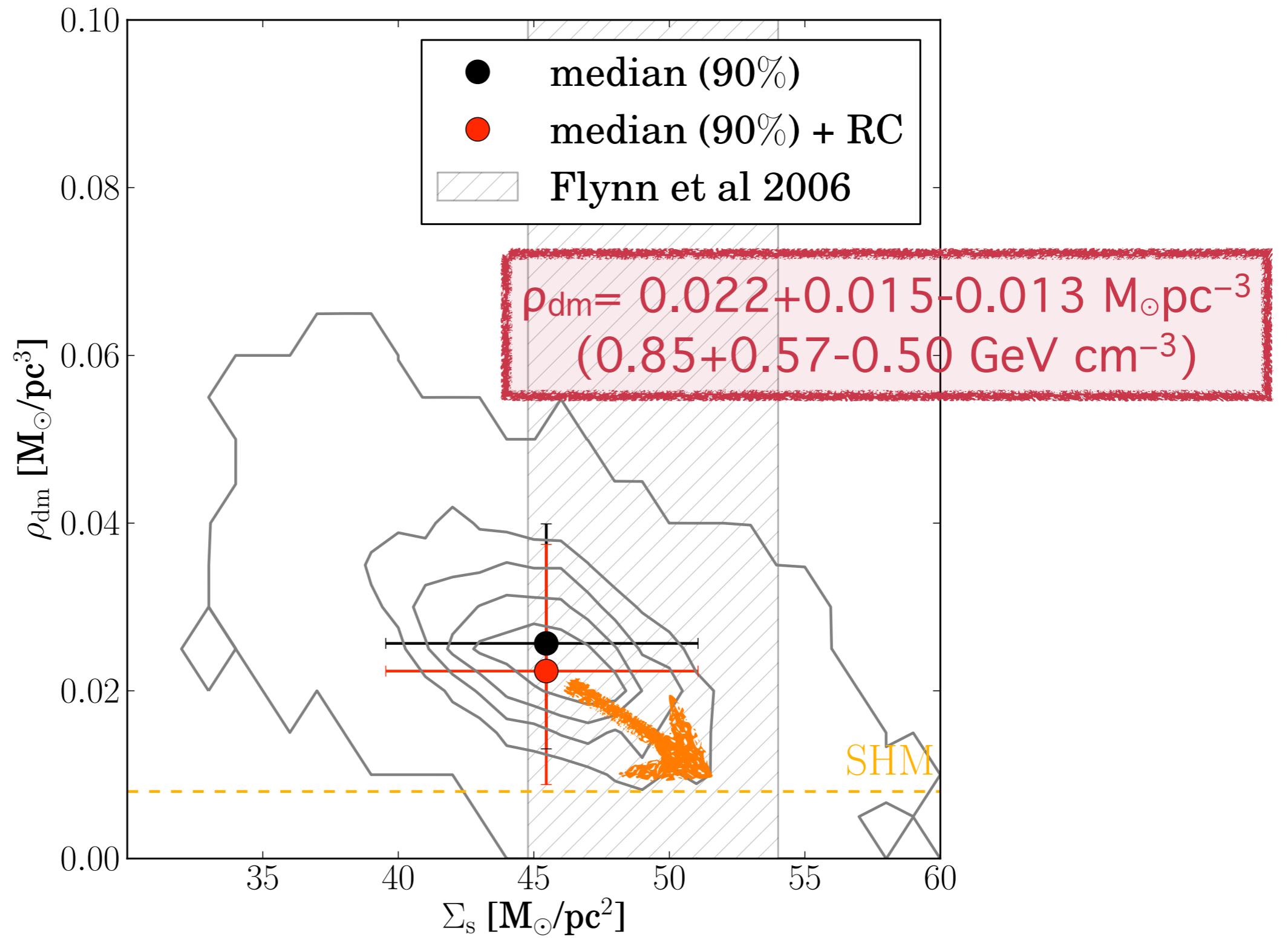
data from Kuijken & Gilmore 1989 - K dwarfs



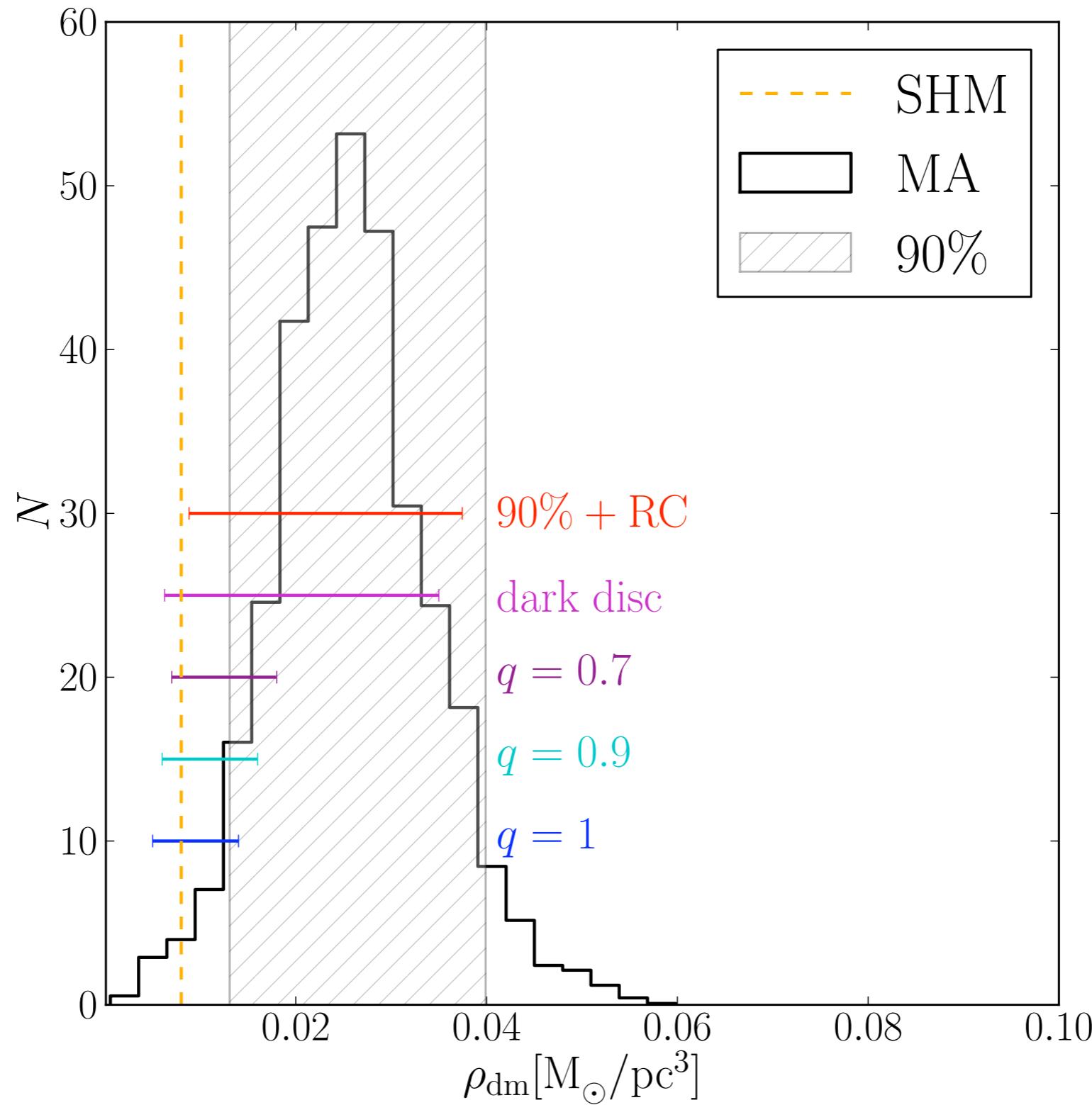
data from Kuijken & Gilmore 1989 - K dwarfs



data from Kuijken & Gilmore 1989 - K dwarfs



data from Kuijken & Gilmore 1989 - K dwarfs



Conclusion

* We present a new method to measure ρ_{dm} from the vertical kinematics local tracers. It relies on a minimal set of assumptions and

- uses a MCMC to marginalise over the uncertainties
- does not require any prior on the MW rotation curve
- does not require any assumption on the tracers' distribution function

* We use hi-res simulations as a mock data set to test our method.

* We obtain a new measurement of the local dark matter density: $\rho_{\text{dm}} = 0.022+0.015-0.013 \text{ M}_\odot \text{ pc}^{-3} (0.85+0.57-0.50 \text{ GeV cm}^{-3})$.

* Our median value of the local dark matter density is larger at 90% confidence than the Standard Halo Model value of $\rho^{\text{SHM}}_{\text{dm}} = 0.008 \text{ M}_\odot \text{ pc}^{-3} (0.30 \text{ GeV cm}^{-3})$. If confirmed by future data (GAIA), it has interesting implications:

- for direct detection experiments: it implies a larger flux of dark matter particles and therefore a greater chance of detection.
- it suggests that the halo of our Galaxy is oblate and/or that we have a disc of dark matter.