

# Flavour Physics

## Olaf Steinkamp

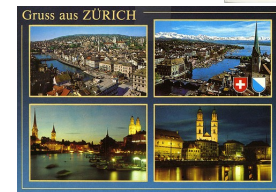
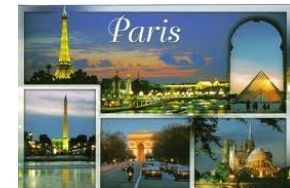
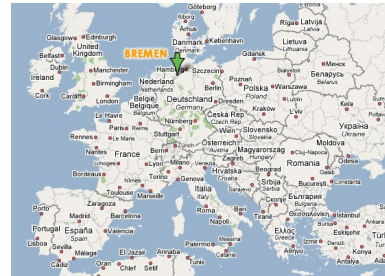


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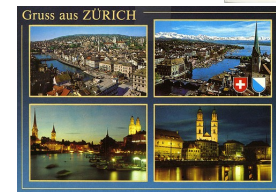
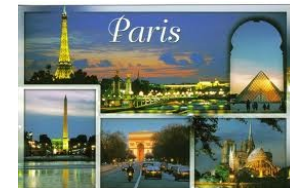
# Your Lecturer

- born in Bremen, Germany
- studied physics in Bonn
- PhD work at CERN
  - on a small experiment you will never have heard of
- 1<sup>st</sup> PostDoc at Saclay
  - working on the construction of the NA48 detector
  - observation of direct CP violation in neutral kaon decays
- 2<sup>nd</sup> PostDoc at NIKHEF
  - working on the construction of the HERA-B detector
  - (failed) attempt to search for CP violation in the  $B^0\bar{B}^0$  system
- “Wissenschaftlicher Mitarbeiter” at Universität Zürich
  - working on the LHCb experiment
  - indirect search for “New Physics” ( = physics beyond the Standard Model )  
via precision measurements of CP violation and rare heavy quark decays



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- **Part I: Introduction**

- what is (quark) flavour physics and why is it so exciting?
- how we got here: brief history of flavour physics in the 20<sup>th</sup> century

- **Part II: Particle-Antiparticle Mixing**

- a short summary of the formalism (don't worry, I'm an experimentalist ... )
- introduce experimental facilities and techniques

- **Part III: Precision tests of the Standard Model**

- CP violating observables:  $\sin 2\beta$ , CKM angle  $\gamma$ ,  $B_s^0 \bar{B}_s^0$  mixing phase  $\phi_s$
- rare decays: search for  $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ , angular observables in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

[ selected topics, no attempt at giving a comprehensive overview of the field ! ]

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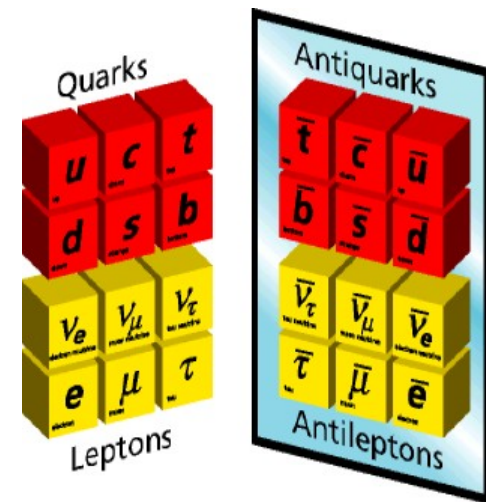
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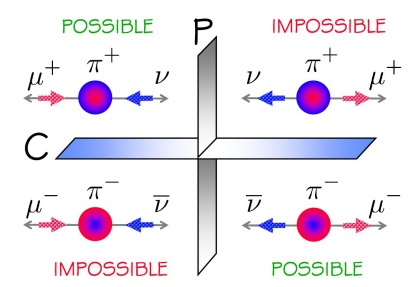
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- study properties of the three fermion families and their interactions
  - masses, lifetimes, ...
  - couplings, amplitudes, phases, ...
- it's all about the weak interaction
  - flavour conserved in strong and electromagnetic interactions
- three distinct sectors (theoretical questions and experimental approaches)
  - **quarks**: measure mixing parameters, test Standard Model predictions
  - **charged leptons**: test lepton number conservation
  - **neutrinos**: measure oscillation parameters, masses, Dirac  $\leftrightarrow$  Majorana ?
- guiding principle: symmetries and their violation
  - Parity (P), Charge Conjugation (C), Time reversal (T), combined CP symmetry, all violated in weak interactions



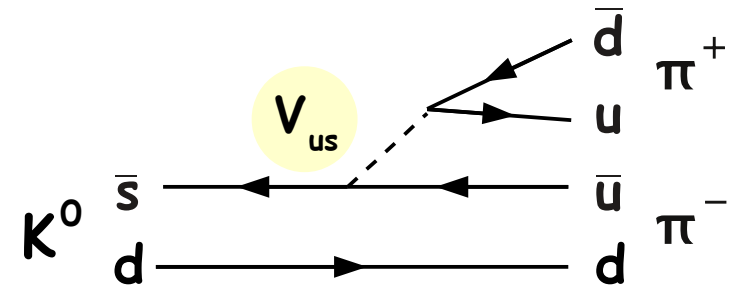
this course



## Observe mixing between quark families in charged-current interactions

- e.g. kaons and B mesons would otherwise be stable particles
- described by quark mixing matrix  $V_{ij}$  (Cabibbo-Kobayashi-Maskawa = CKM) in the charged current Lagrangian

$$-L_{cc} = \frac{g}{\sqrt{2}} \bar{u}_i \gamma^\mu (1 - \gamma_5) V_{ij} d_j W_\mu^+ + h.c.$$



$$V_{ij} = V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

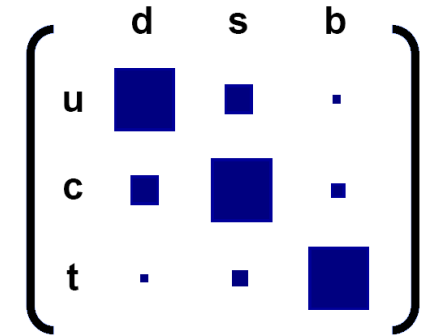
- studying the parameters of the CKM matrix is one of the main goals of quark flavour physics
- 3 quark families: 4 free parameters = 3 rotation angles + complex phase
- this complex phase is the only source of CP violation in the Standard Model

# Wolfenstein Parametrization

## Values of the CKM matrix elements not predicted by theory

- measured magnitudes show clear hierarchy [PDG 2012]

$$V_{\text{CKM}} = \begin{pmatrix} 0.97425 \pm 0.00022 & 0.2252 \pm 0.0009 & 0.00389 \pm 0.00044 \\ 0.2230 \pm 0.0011 & 1.023 \pm 0.036 & 0.0406 \pm 0.0013 \\ 0.0084 \pm 0.0006 & 0.0387 \pm 0.0021 & 0.88 \pm 0.07 \end{pmatrix}$$



- is there some deeper meaning hidden in this?

## This hierarchy reflected in Wolfenstein parametrisation

- expand all CKM elements in terms of  $\lambda = \sin \theta_c \approx 0.23$
- approximate to order  $\lambda^3$
- assign the complex phase to the smallest elements,  $V_{td}$  and  $V_{ub}$

L. Wolfenstein,

[PRL 51 (1983) 1945]

$$V_{\text{CKM}} \approx \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A \cdot \lambda^3 (\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A \cdot \lambda^2 \\ A \cdot \lambda^3 (1 - \rho - i\eta) & -A \cdot \lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$



# Unitarity Triangles

## Unitarity of CKM matrix $\rightarrow$ 6 orthogonality relations

$$V_{ud} V_{cd}^* + V_{us} V_{cs}^* + V_{ub} V_{cb}^* = 0 \quad (\lambda, \lambda, \lambda^5)$$

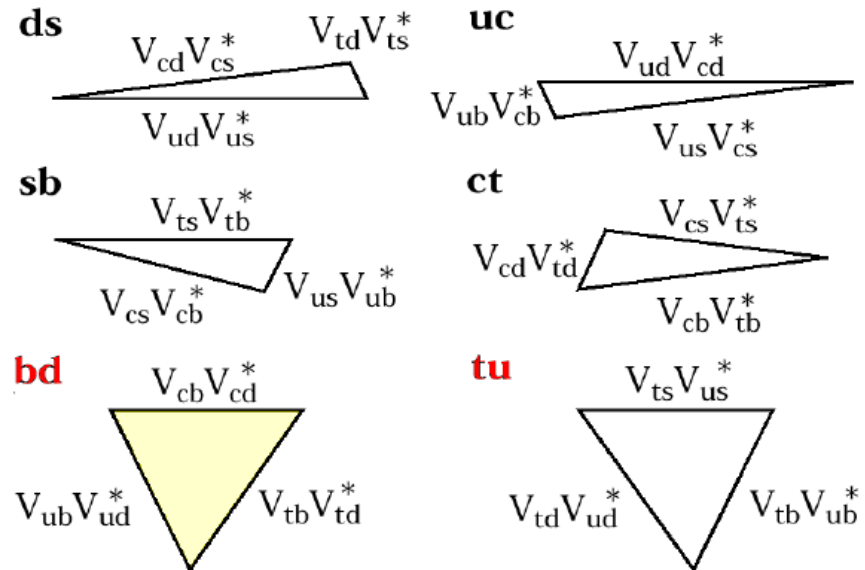
$$V_{ud} V_{td}^* + V_{us} V_{ts}^* + V_{ub} V_{tb}^* = 0 \quad (\lambda^3, \lambda^3, \lambda^3)$$

$$V_{cd} V_{td}^* + V_{cs} V_{ts}^* + V_{cb} V_{tb}^* = 0 \quad (\lambda^4, \lambda^2, \lambda^2)$$

$$V_{ud} V_{us}^* + V_{cd} V_{cs}^* + V_{td} V_{ts}^* = 0 \quad (\lambda, \lambda, \lambda^5)$$

$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0 \quad (\lambda^3, \lambda^3, \lambda^3)$$

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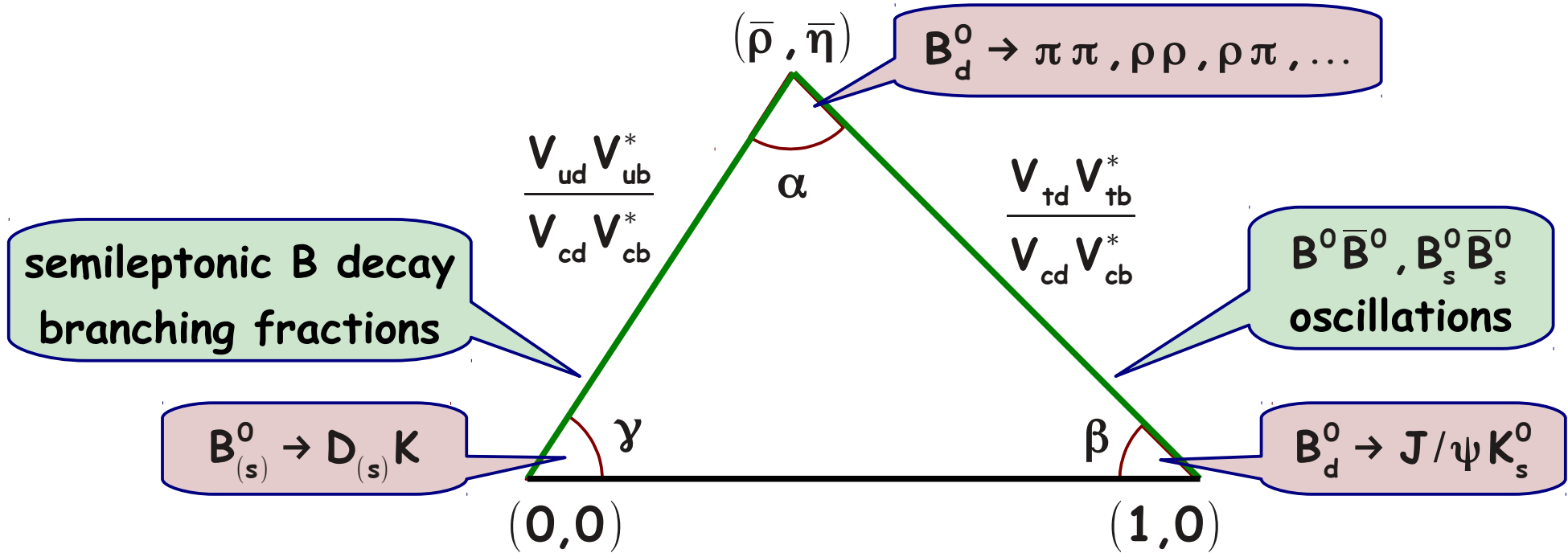
- can be visualized as triangles in the complex plane
  - all six triangles have the same surface area  $\propto$  CP violation
  - but four of them are "squashed"
- the two non-squashed triangles are identical in Wolfenstein approximation
  - differences appear at higher orders of  $\lambda \rightarrow$  become relevant at LHCb

C. Jarlskog,  
[PRL 55 (1985) 1039]

angles and sides of these triangles are related to measurable quantities

# "The" Unitarity Triangle

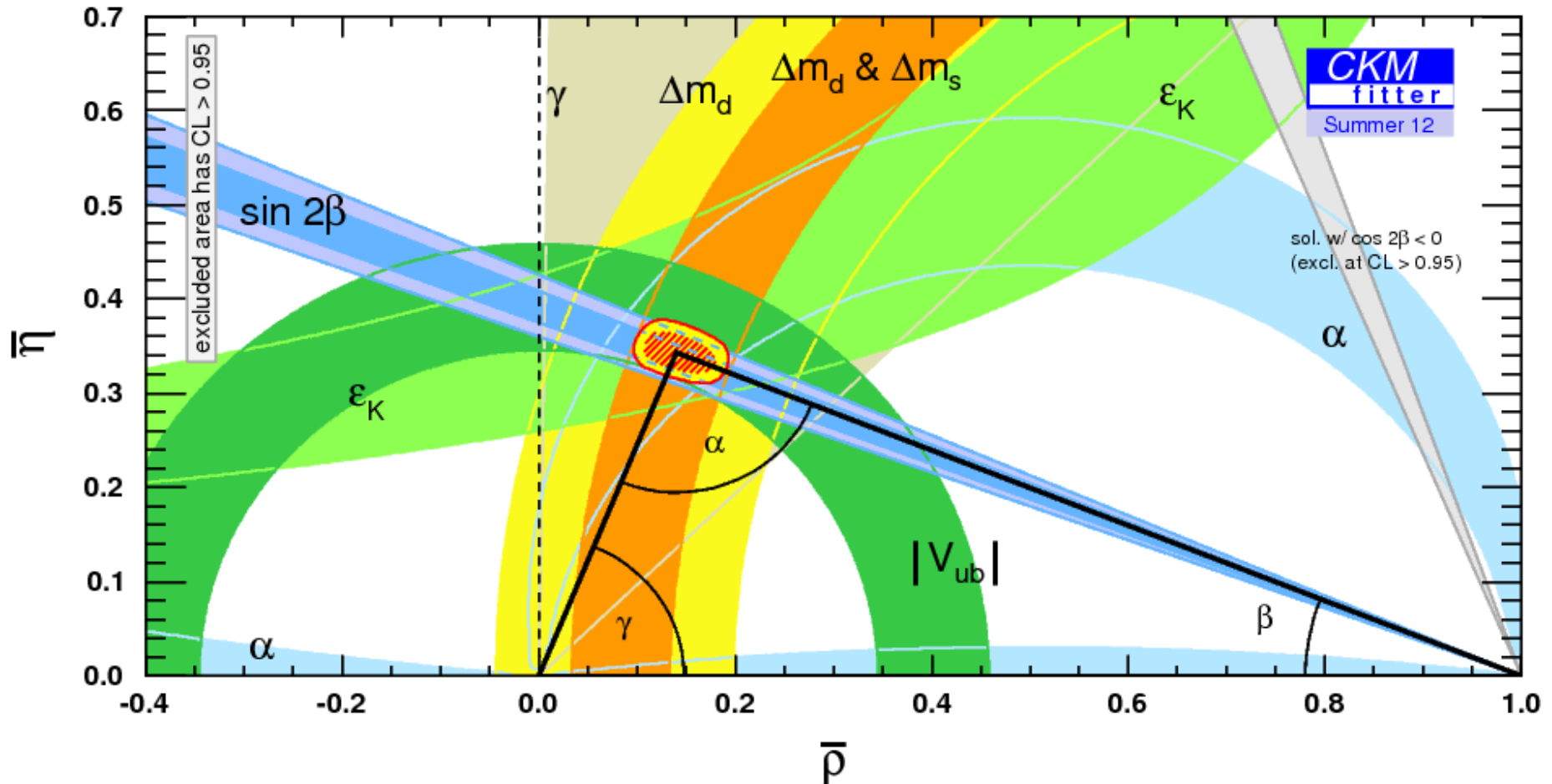
Use  $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$  and normalize to  $V_{cd}V_{cb}^*$



- measure the lengths of the two sides: CP conserving quantities
- measure all three angles: CP violating quantities (angles = phases !)
- many observables  $\rightarrow$  overconstraint determination of triangle

consistency check of Standard Model !

# "The" Unitarity Triangle 2012



- so far a huge success story for the Standard Model
- current measurement precision permits  $\sim 20\%$  contribution from New Physics

need more precise measurements: this is the goal of LHCb !

## Why do we expect New Physics to show up in these observables?

- many processes involve loop diagrams:

- box diagrams (mixing)

- Penguin diagrams (decays)

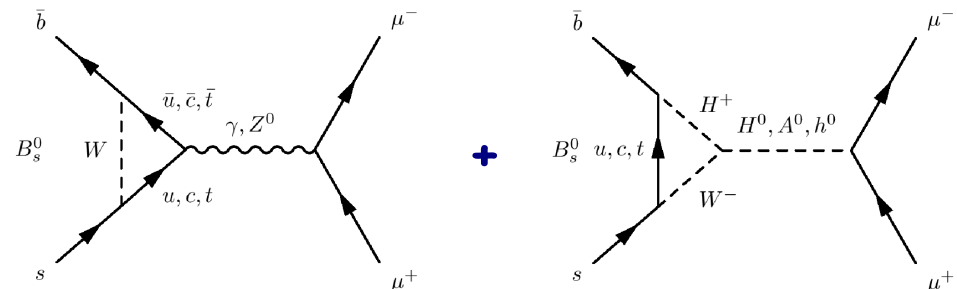
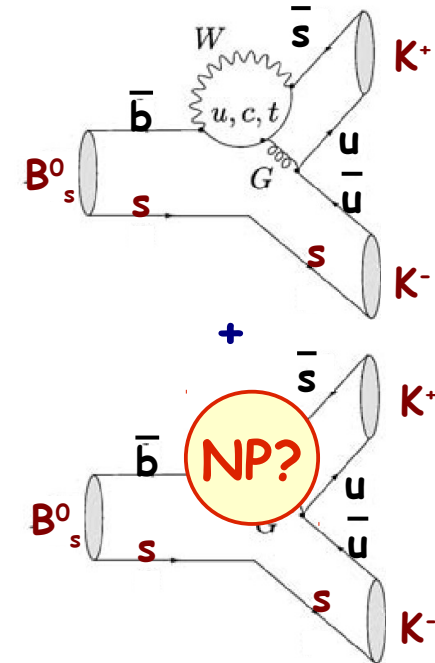
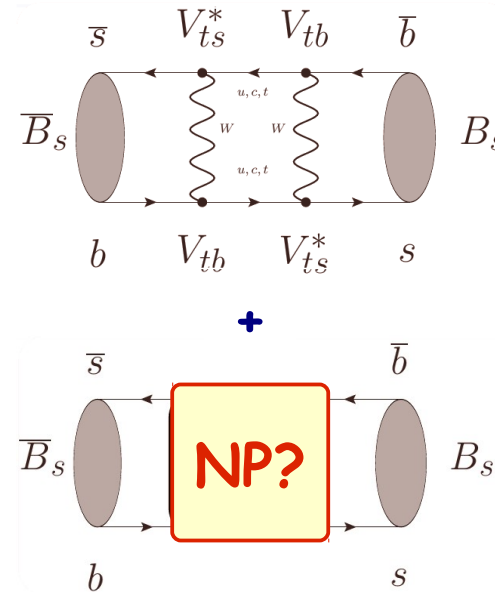
- New Physics models usually predict new, heavy particles (e.g. SUSY)

- these particles can appear in the loops and affect magnitudes and phases

- searches are sensitive to the appearance of virtual particles in loops

- test much higher mass scales than direct searches for new particles (limited by center-of-mass energy)

- another promising hunting ground: rare heavy quark decays



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## Observe similar behaviour of proton/neutron

- different charge but similar masses, same couplings in nuclear interactions

## Heisenberg (1932): p/n form an Isospin doublet

ZfP 77 (1932) 1

- nuclear interaction invariant under global  $SU(2)$  rotation in Isospin space

$$p : (\mathbf{I}, I_z) = (1/2, +1/2) \quad ; \quad n : (\mathbf{I}, I_z) = (1/2, -1/2)$$

- similarly:  $\pi^+/\pi^0/\pi^-$  form an Isospin triplet

$$\pi^+ : (\mathbf{I}, I_z) = (1, +1) \quad ; \quad \pi^0 : (\mathbf{I}, I_z) = (1, 0) \quad ; \quad \pi^- : (\mathbf{I}, I_z) = (1, -1)$$

## In today's language: $I_z = +1/2 \rightarrow u$ quark, $I_z = -1/2 \rightarrow d$ quark

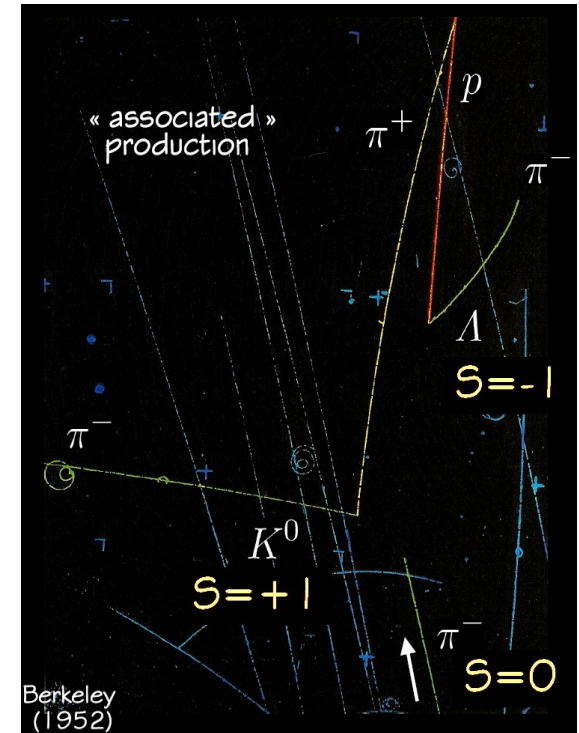
$$p = (uud), \quad n = (udd) \quad \pi^+ = (u\bar{d}), \quad \pi^0 = 1/\sqrt{2} (u\bar{u} + d\bar{d}), \quad \pi^- = (\bar{u}d)$$

- Isospin is not an exact symmetry but rather successful as a concept

- works so well because  $m_u \sim m_d$  and  $m_u, m_d \ll \Lambda_{QCD} \approx 200 \text{ MeV}$

## Observe “strangely behaved” particles

- large production cross sections
  - typical for strong interaction
- but long lifetimes of order  $10^{-10}$ s
  - typical for weak decays
- always produced in pairs: “associated production”



## Gell-Mann (1953) / Nishijima (1955): “strangeness” quantum number

- conserved in production (strong interaction)
- not conserved in decay (weak interaction)

PR 92 (1953) 833

PTP 13 (1955) 285

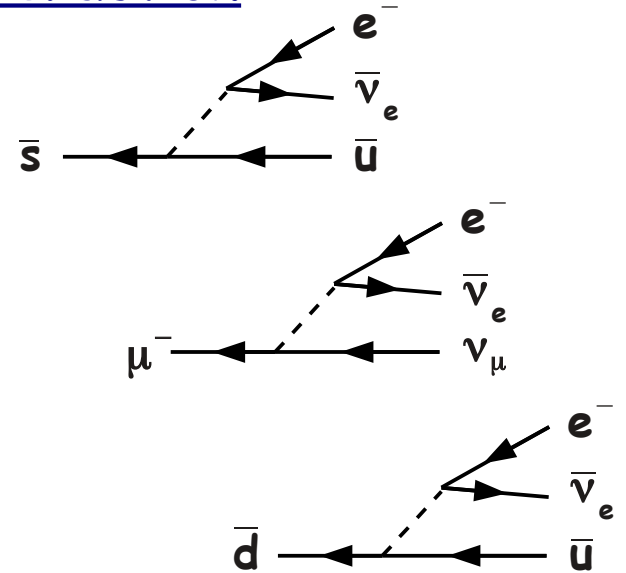
## In today's language: strangeness $\rightarrow$ s quark

- associated production: creation of an  $s\bar{s}$ -pair in strong interaction

# Cabibbo Angle

## Observe different coupling strengths of weak interaction

- weak coupling constant should be universal if weak interactions are a fundamental force, but:
- coupling in decays of strange particles seems about a factor 20 smaller than in muon decay
- coupling in neutron decay about 4% smaller than in muon decay



## Cabibbo (1963): weak interaction couples to a linear combination

[PRL 10 (1963) 531]

$$d' = \cos \theta_c \cdot d + \sin \theta_c \cdot s \quad \text{with} \quad \lambda = \sin \theta_c \approx 0.22$$

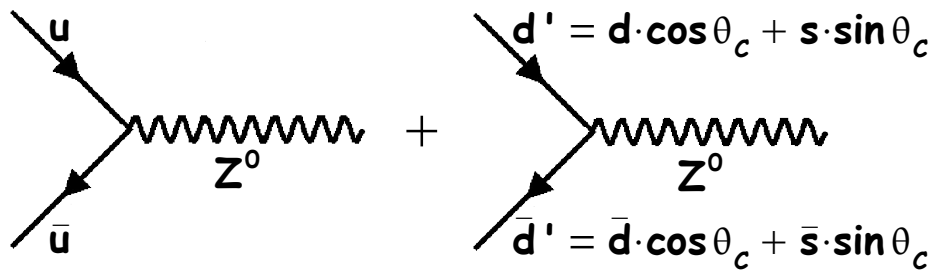
- coupling strengths in hadronic decays are then (using today's language)

$$\frac{d \rightarrow u W^-}{\mu^- \rightarrow \nu_\mu W^-} = \cos^2 \theta_c \approx 0.96 \qquad \frac{s \rightarrow u W^-}{d \rightarrow u W^-} = \frac{\sin^2 \theta_c}{\cos^2 \theta_c} \approx \frac{1}{20}$$



## Observe strong suppression of Flavour-Changing Neutral Currents

- for example:  $\text{BF}(K^+ \rightarrow \mu^+ \nu_\mu) \approx 63.5\%$  but  $\text{BF}(K_L^0 \rightarrow \mu^+ \mu^-) \approx 7 \times 10^{-9}$
- but would expect sizeable amplitude if weak interaction couples to  $u$  and  $d'$



$$\Rightarrow u\bar{u} + d\bar{d} \cos^2 \theta_c + s\bar{s} \sin^2 \theta_c + \dots + (d\bar{s} + \bar{d}s) \cos \theta_c \sin \theta_c$$

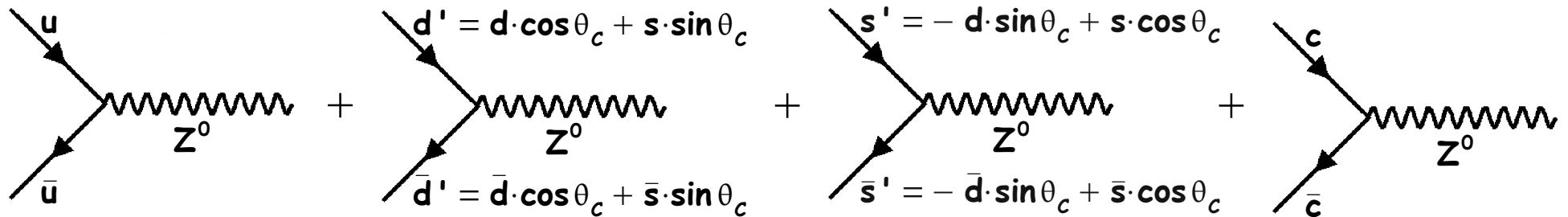
## Glashow, Ilioupolis, Maiani (1970): quark doublets

[PRD 2 (1970) 1285]

$$\begin{pmatrix} u \\ d' \end{pmatrix} \quad \begin{pmatrix} c \\ s' \end{pmatrix} \quad \text{with} \quad \begin{pmatrix} d' \\ s' \end{pmatrix} = \begin{pmatrix} \cos \theta_c & \sin \theta_c \\ -\sin \theta_c & \cos \theta_c \end{pmatrix} \cdot \begin{pmatrix} d \\ s \end{pmatrix}$$

- leads to cancellation of FCNC amplitudes at tree level ( $\rightarrow$  next slide)
- requires an additional, not yet observed quark ( $c$  quark discovered in 1974)

## Quark doublets → suppression of FCNC at tree level



$$u\bar{u} + c\bar{c} + (d\bar{d} + s\bar{s}) \cdot \cos^2 \theta_c + (d\bar{d} + s\bar{s}) \cdot \sin^2 \theta_c$$

$$\dots + (d\bar{s} + \bar{d}s) \cdot \cos \theta_c \sin \theta_c - (d\bar{s} + \bar{d}s) \cdot \sin \theta_c \cos \theta_c = u\bar{u} + c\bar{c} + d\bar{d} + s\bar{s}$$

- cancellation only exact if all quark masses are the same
  - valid to very good approximation, because quark masses  $\ll Z^0$  mass
- FCNC can proceed through 2<sup>nd</sup> order processes (e.g. double W-exchange)
  - but strongly suppressed because of smallness of weak coupling constant

# Parity Violation

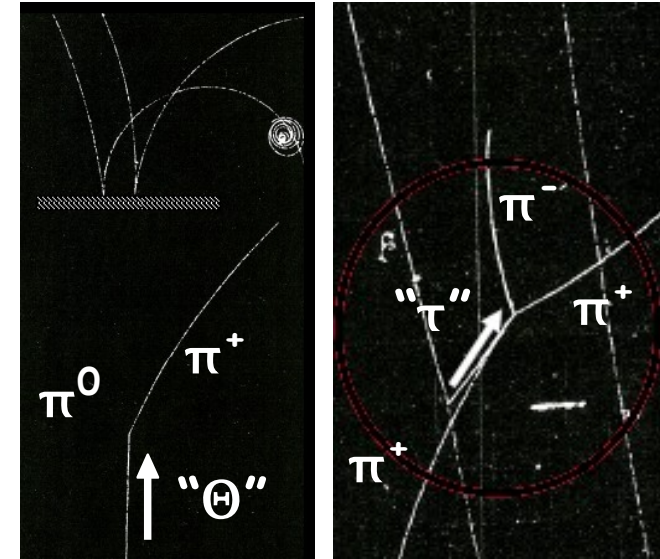
" $\Theta$ / $\tau$ -puzzle": observe two charged, strange, spin-0 mesons

- same mass ( $\sim 500$  MeV) and same lifetime, but:
- one (" $\Theta$ ") decays into  $\pi^+\pi^0$  (even parity)
- the other (" $\tau$ ") decays into  $\pi^+\pi^+\pi^-$  (odd parity)

Yang, Lee (1956): V-A theory of weak interactions

[PR 104 (1956) 254]

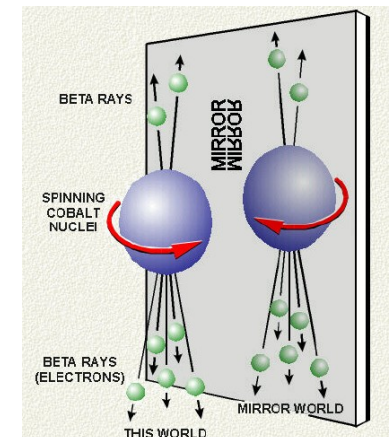
- parity is not conserved in weak interactions
- " $\Theta$ " and " $\tau$ " are in fact the same particle ( $K^+$ )



Wu et al. (1957): experimental proof of parity violation

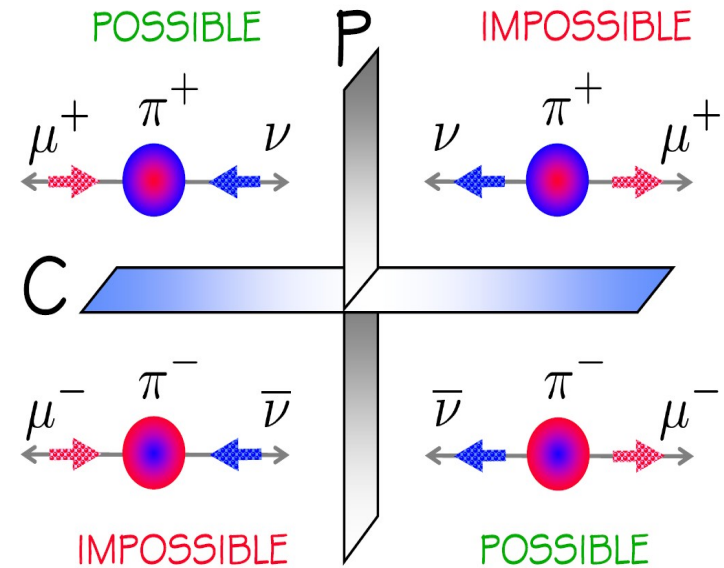
[PR 105 (1957) 1413]

- measure angular distribution of electrons from  $\beta$ -decay of polarized  $^{60}\text{Co}$  (spin= $5^+$ ) to  $^{60}\text{Ni}^*$  (spin= $4^+$ )
- must be up-down symmetric if parity is conserved
- observation: electrons are emitted predominantly opposite to  $^{60}\text{Co}$ -spin  $\rightarrow$  parity is maximally violated!



## Parity violation in semi-leptonic pion decays

- muons from  $\pi^\pm$  decays are polarized:
  - $\mu^-$  from  $\pi^-$ -decays are left-handed
  - $\mu^+$  from  $\pi^+$ -decays are right-handed
- parity is maximally violated, as expected
- charge conjugation is also maximally violated
- but: decay rates for  $\pi^-$  to left-handed  $\mu^-$  and for  $\pi^+$  to right-handed  $\mu^+$  are the same !



## Landau, Okun (1957): relevant symmetry in weak interactions is CP

- CP = Charge conjugation × Parity
- Richard Feynman in *Symmetries in Physical Laws*, 1963:

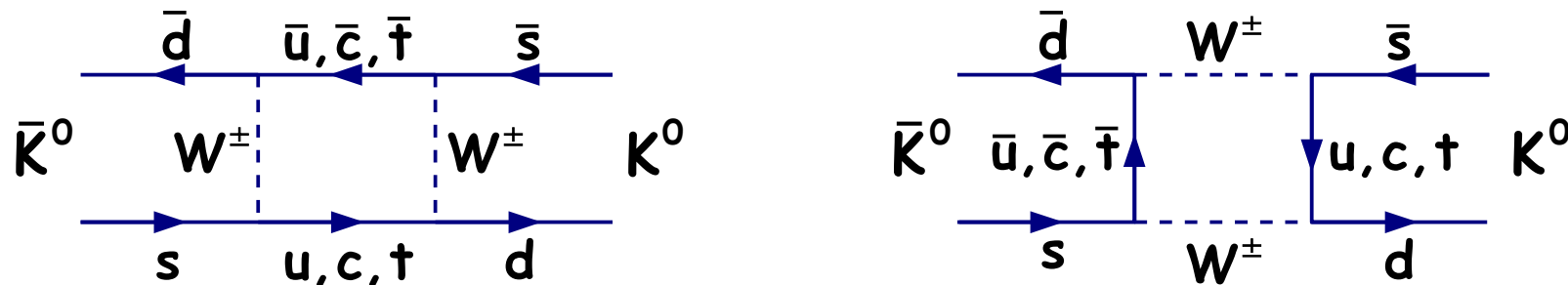
[Nucl Phys 3 (1957) 127]

[Zh Eksp Teor Fiz 32 (1957) 1587]

“it is really true that right and left symmetry is still maintained ... the right-handed matter behaves the same way as the left-handed antimatter”

## Short excursion: $K^0\bar{K}^0$ mixing

- strangeness is the only quantum number that distinguishes  $K^0$  from  $\bar{K}^0$
- strangeness is not conserved in weak interactions: transitions  $K^0 \leftrightarrow \bar{K}^0$
- in today's language: transitions via double  $W$  exchange ("box diagrams")



- pure state  $|K^0\rangle$  produced at time  $t=0$  will evolve into a mixed state at  $t>0$

$$|\psi(t)\rangle = a(t) \cdot |K^0\rangle + b(t) \cdot |\bar{K}^0\rangle$$

- define Eigenstates of  $CP$  operator:

$$|K_1\rangle = \frac{1}{\sqrt{2}} \cdot \{ |K^0\rangle + |\bar{K}^0\rangle \} \Rightarrow CP |K_1\rangle = + |K_1\rangle$$

$$|K_2\rangle = \frac{1}{\sqrt{2}} \cdot \{ |K^0\rangle - |\bar{K}^0\rangle \} \Rightarrow CP |K_2\rangle = - |K_2\rangle$$

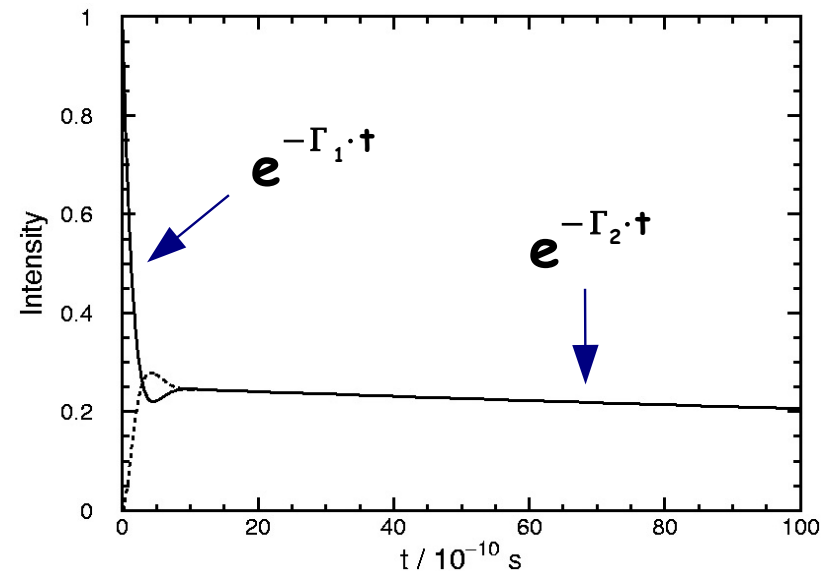
## Gell-Mann, Pais (1955): two $K^0$ states with different lifetimes

[PR 97 (1955) 1387]

- if  $CP$  conserved in weak interactions, then
  - $K_1$  and  $K_2$  are also eigenstates of weak interaction
  - $K_1$  can decay into 2 pions
  - $K_2$  cannot decay into 2 pions
- all possible decay channels for  $K_2$  suppressed:
  - decays to 3 pions by phase space
  - semi-leptonic decays by parity violation
- $K_2$  must have much longer lifetime than  $K_1$
- measured lifetimes:

$$\begin{aligned}
 J_K = J_\pi = 0 &\Rightarrow L_{\pi\pi} = 0 \\
 &\Rightarrow CP_{\pi\pi} = -1^{L_{\pi\pi}} = +1
 \end{aligned}$$

$$\tau(K_2) \approx 500 \times \tau(K_1)$$

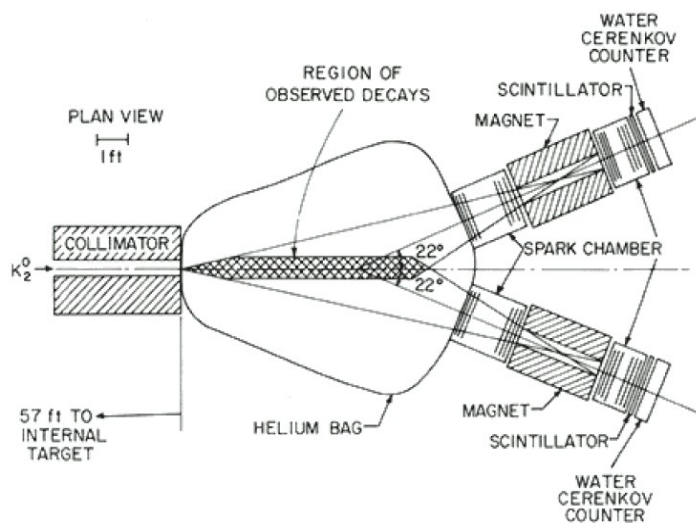


# CP Violation

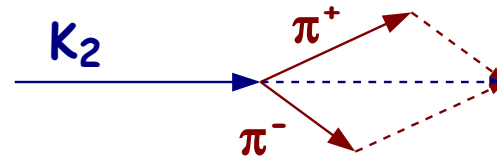
## Christenson, Cronin, Fitch, Turlay (1964): observation of $K_2 \rightarrow \pi^+ \pi^-$

[PRL 13 (1964) 138]

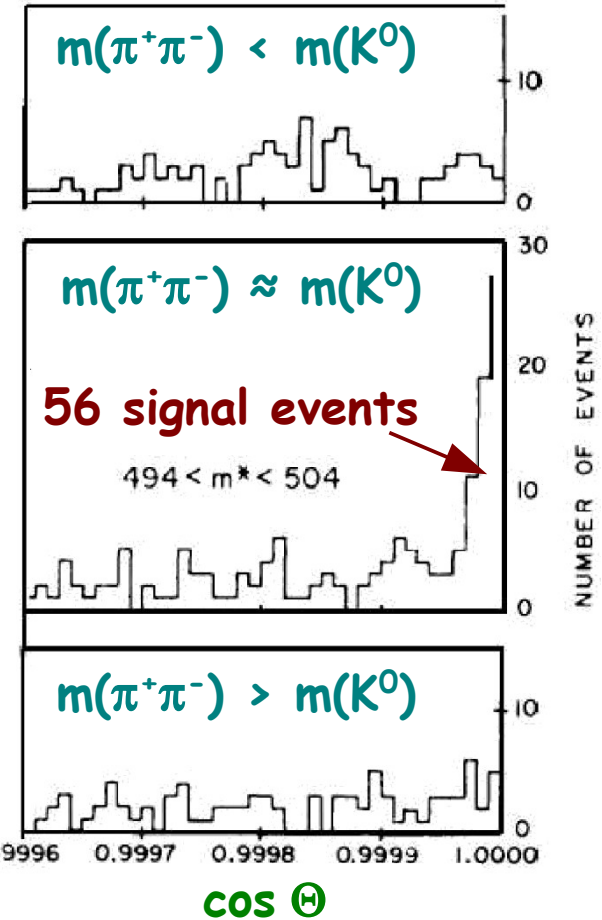
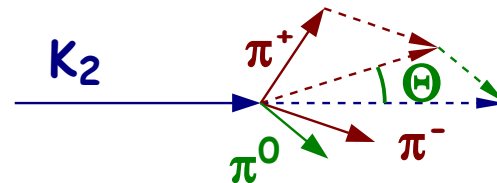
- shoot protons into fixed target, produce  $K^0$  and  $\bar{K}^0$
- let them propagate in a vacuum tube
- $K_1$  component decays away  $\rightarrow$  obtain pure  $K_2$  beam
- search for  $\pi^+ \pi^-$  decays in this  $K_2$  beam
- energy conservation: invariant mass of  $\pi^+ \pi^-$  pair
- momentum conservation: momentum balance



### 2-body decays:



### 3-body decays:



- observe excess of 56 events in signal region  $\Rightarrow$

$$\text{BR}(K_2 \rightarrow \pi^+ \pi^-) \approx 2 \times 10^{-3}$$

# Sakharov Conditions

## Sakharov (1967): CP violation required to create a matter/antimatter asymmetry in the Universe

[JETP Lett 5 (1967) 24]

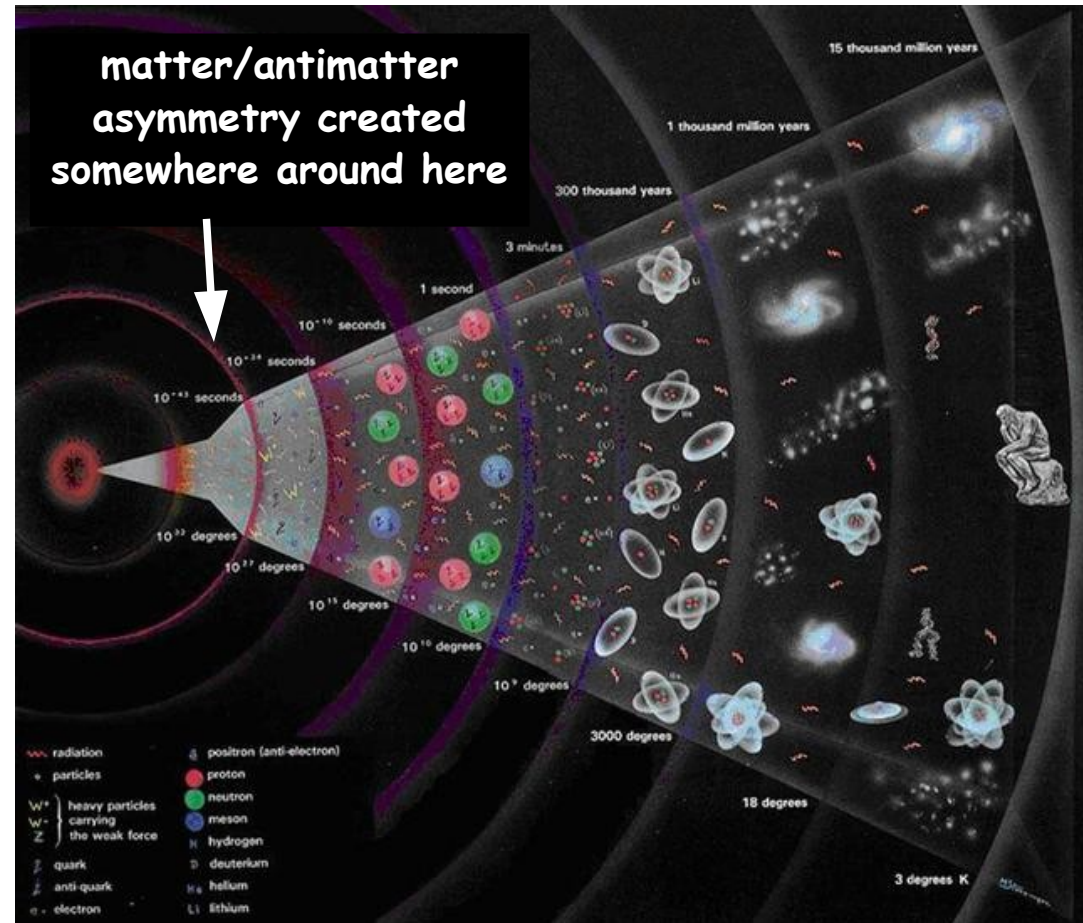
- Sakharov's three conditions:
  - Baryon-number violation
  - C violation and CP violation
  - thermal non-equilibrium
- but: baryon asymmetry observed in the universe is

$$\eta = \frac{n_B - n_{\bar{B}}}{n_\gamma} \approx 6 \times 10^{-10}$$

- CKM-induced CP violation gives

$$\eta \approx 10^{-18}$$

- need additional sources of CP violation





# CKM Mechanism

## Kobayashi, Maskawa (1972): CP violation if three quark doublets

[PTP 49 (1973) 652]

$$\begin{pmatrix} u \\ d' \end{pmatrix} \quad \begin{pmatrix} c \\ s' \end{pmatrix} \quad \begin{pmatrix} t \\ b' \end{pmatrix} \quad \text{with} \quad \begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \cdot \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

- 9 complex numbers = 18 parameters
  - 9 unitarity constraints ( $V^\dagger V = VV^\dagger = 1$ )
  - 5 arbitrary (“unphysical”) phases
- = 4 free parameters: 3 rotation angles **+ 1 complex phase**
- CP violation due to interference if diagrams with different weak phase contribute to the same process
- “prediction” of third quark family before even charm quark was discovered

$$\left. \begin{array}{l} u_i \rightarrow e^{i\phi_i} u_i \\ d_j \rightarrow e^{i\phi_j} d_j \end{array} \right\} \Leftrightarrow V_{ij} \rightarrow e^{i(\phi_j - \phi_i)} V_{ij}$$

## Various other models proposed at the time to explain CP violation

- most prominent: new “superweak” force that acts only in kaon mixing

## "November revolution" (1974)

[PRL 33 (1974) 1404]

[PRL 33 (1974) 1406]

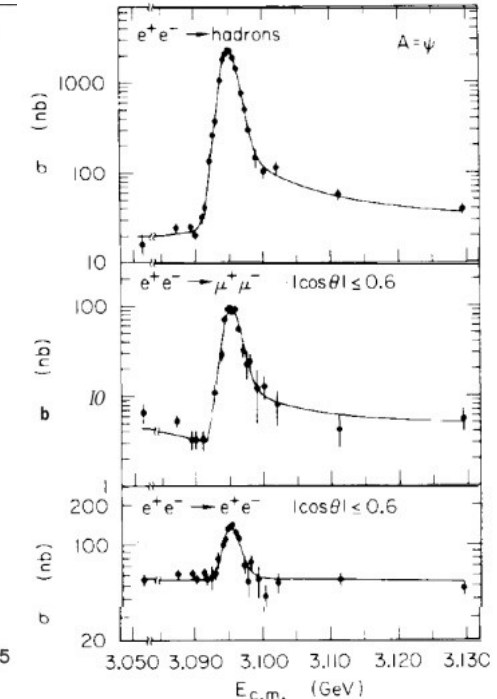
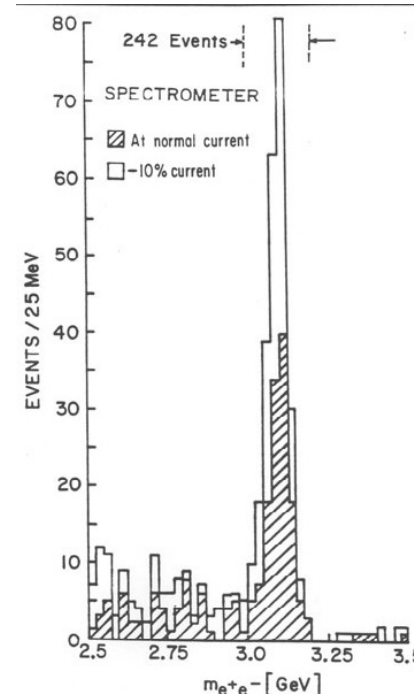
- observation of a narrow resonance at a mass of 3.1 GeV, simultaneously
  - in  $p + Be \rightarrow e^+ e^- + X$  at BNL (Ting et al.)  $\rightarrow$  "J"
  - in  $e^+ e^- \rightarrow e^+ e^-, \mu^+ \mu^-, \text{hadrons}$  at SLAC (Richter et al.)  $\rightarrow$  "ψ" } J/ψ
- in both cases, measured width dominated by the detector resolution

- narrow width  $\rightarrow$  long lifetime  
 $\rightarrow$  cannot be an excited u,d,s state

- interpretation: bound  $c\bar{c}$  state

$$m(c) \sim 1.5 \text{ GeV}$$

- soon confirmed by observation of other  $c\bar{c}$  states and of open charm (D mesons)

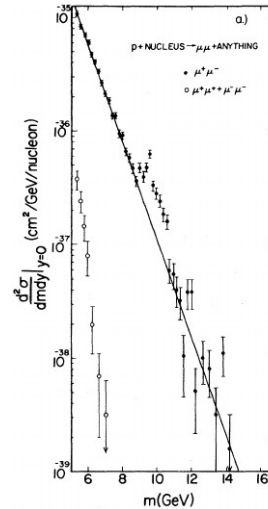


# Bottom and Top Quarks

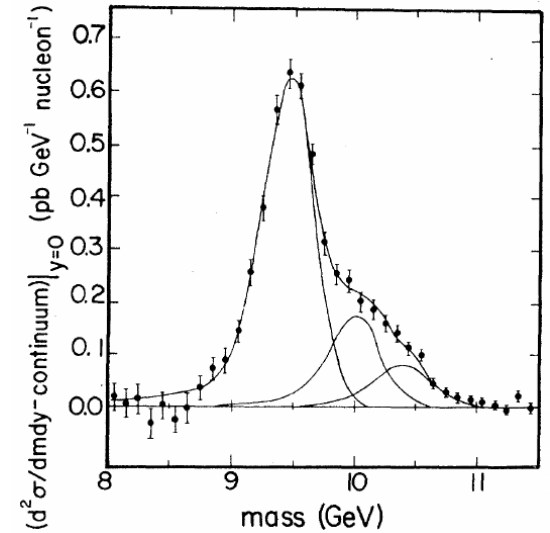
## Lederman et al. (1977): search for $b\bar{b}$ resonances in $p + \text{Cu} \rightarrow \mu^+ \mu^- + X$

- observe excess of  $\mu^+ \mu^-$  pairs around an invariant mass of 9.4-10.4 GeV
- resolved into three resonances, interpreted as bound  $b\bar{b}$  states

$$m(b) \sim 4.5 \text{ GeV}$$



[PRL 39 (1977) 252]



[PRL 42 (1979) 486]

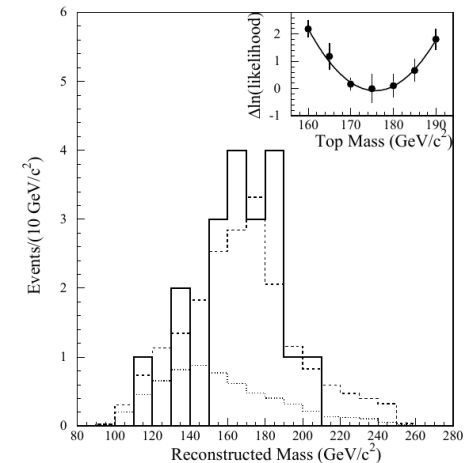
## CDF/D0 (1995): first observation of top quark

- existence of top quark taken for granted after discovery of b quark
- mass around 170 GeV predicted from fits to electroweak precision measurements at LEP and SLC
- production in 1.8 TeV  $p\bar{p}$  collisions at Tevatron
- detection in  $t \rightarrow W b$  decays

$$m(t) \sim 176 \text{ GeV}$$

[PRL 74 (1995) 2626]

[PRL 74 (1995) 2632]



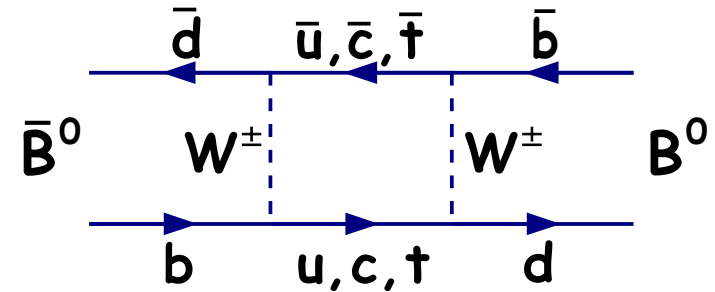
## Argus experiment at DESY (1987)

[PLB192 (1987) 245]

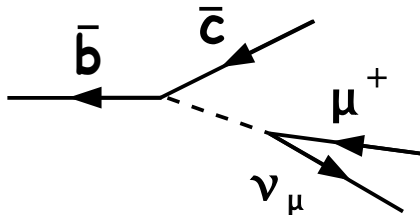
- $e^+e^-$  collider operating at  $\Upsilon(4s)$  resonance
- produce  $B^0\bar{B}^0$  pairs through

$$e^+e^- \rightarrow \Upsilon(4s) \rightarrow B^0\bar{B}^0$$

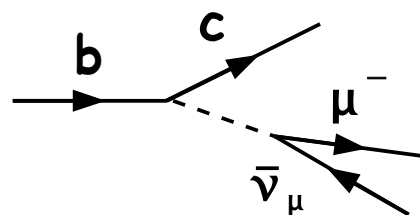
- $B^0\bar{B}^0$  mixing through box diagrams
- can be observed in semi-leptonic decays



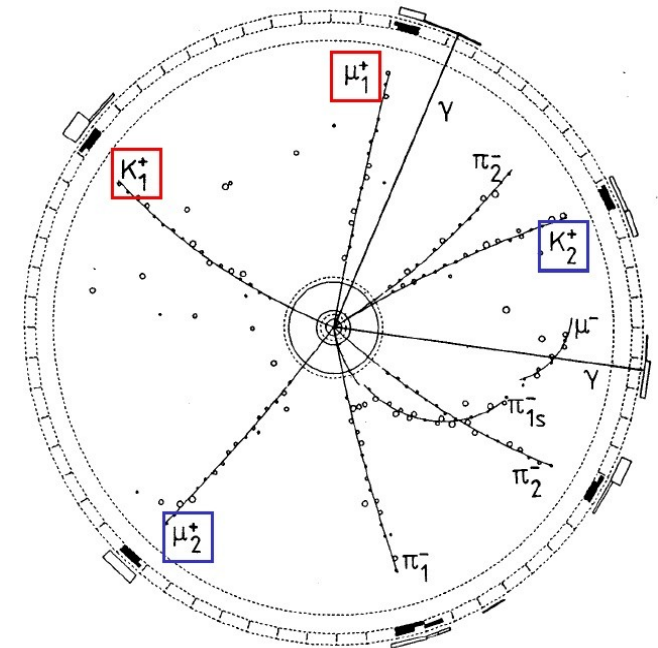
$$B^0 \rightarrow D^{*-} \mu^+ \nu_\mu$$



$$\bar{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu$$



- observe "like-sign event" with two  $\mu^-$  or two  $\mu^+$   
 $\rightarrow B^0$  or  $\bar{B}^0$  must have mixed

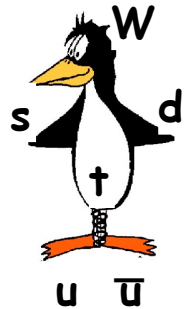
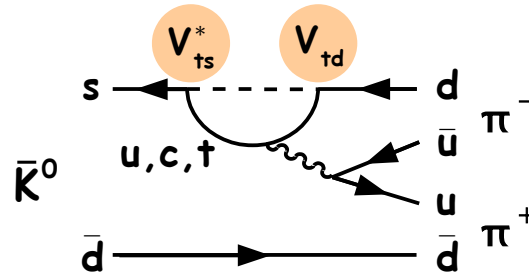
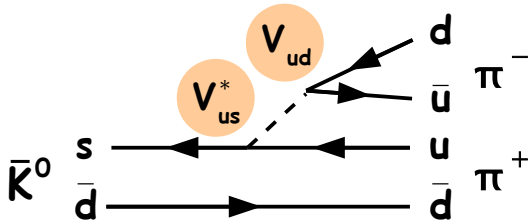
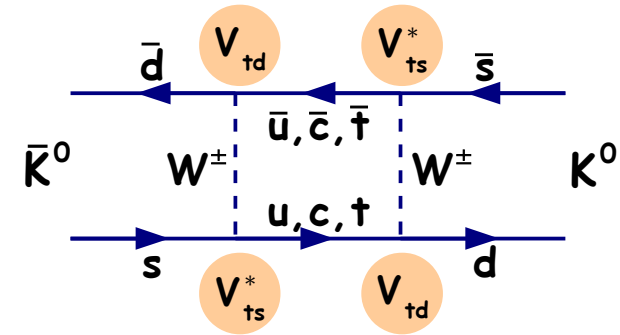


- strong mixing observed  $\rightarrow$  predict large top quark mass

# Direct CP Violation

## CKM: CP violation from interference of diagrams with different phase

- interference of box diagrams with different internal quarks: "indirect" CP violation in K mixing
- interference of tree and penguin decay diagrams with different phases: "direct" CP violation in decay



- can be tested by comparing CP violation in  $\pi^+\pi^-$  and  $\pi^0\pi^0$  decays: different decay diagrams  $\rightarrow$  expect CP violation to be slightly different

$$\eta_{+-} = \frac{\Gamma(K_L \rightarrow \pi^+\pi^-)}{\Gamma(K_S \rightarrow \pi^+\pi^-)} = \varepsilon + \varepsilon' \quad ; \quad \eta_{00} = \frac{\Gamma(K_L \rightarrow \pi^0\pi^0)}{\Gamma(K_S \rightarrow \pi^0\pi^0)} = \varepsilon - 2\varepsilon'$$

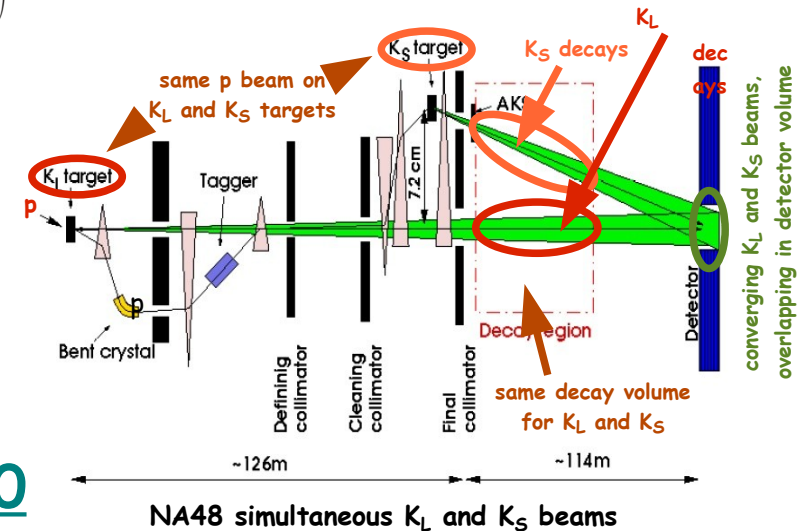
- in Standard Model expect  $\varepsilon'/\varepsilon \approx 10^{-3}$
- if CP violation only in K mixing (superweak interaction):  $\eta_{+-} = \eta_{00}$ ,  $\varepsilon' = 0$

# Direct CP Violation

## Experimental approach: measure the "double ratio"

$$R = \left| \frac{\eta_{00}}{\eta_{+-}} \right|^2 = \frac{\Gamma(K_L \rightarrow \pi^0 \pi^0) / \Gamma(K_S \rightarrow \pi^0 \pi^0)}{\Gamma(K_L \rightarrow \pi^+ \pi^-) / \Gamma(K_S \rightarrow \pi^+ \pi^-)} \approx 1 - 6 \cdot \text{Re} \left( \frac{\varepsilon'}{\varepsilon} \right)$$

- challenge: control systematics to  $O(10^{-4})$
- many systematic effects cancel to first order if all four decay rates are measured simultaneously (same beam, same detector)



## NA48/KTeV (2001): observation of $\varepsilon'/\varepsilon \neq 0$

- end of a decades long competition CERN  $\leftrightarrow$  FNAL

NA48@CERN:

$$\text{Re} \left( \frac{\varepsilon'}{\varepsilon} \right) = (14.7 \pm 2.2) \times 10^{-4}$$

[PLB 544 (2002) 97]

KTeV@FNAL:

$$\text{Re} \left( \frac{\varepsilon'}{\varepsilon} \right) = (19.2 \pm 2.1) \times 10^{-4}$$

[PRD 83 (2011) 092001]

- vindication of CKM model of CP violation
- but large hadronic uncertainties, do not learn much about CKM parameters

# CP Violation in The $B^0\bar{B}^0$ System

## Many advantages over $K^0\bar{K}^0$ system

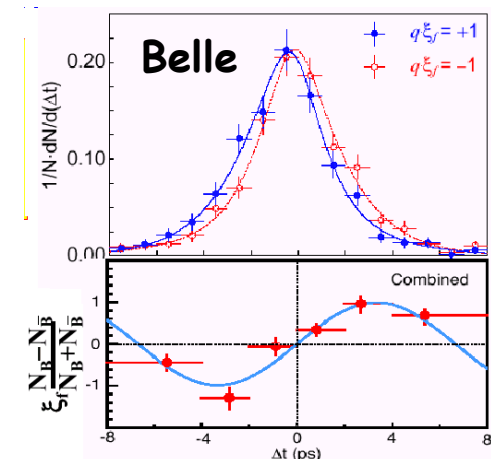
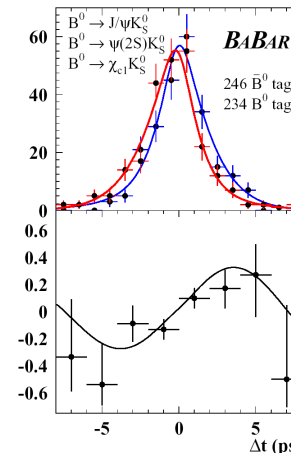
- many decay channels and observables, large CP asymmetries, theoretically “clean” predictions, ...

## But experimental challenges

- B mesons heavy  $\rightarrow$  small production cross section
  - many decay channels  $\rightarrow$  small branching ratios
  - short lifetime and fast oscillation frequency
- } need high-luminosity accelerators and very precise detectors
- dedicated “B factories” constructed especially for CP measurement:

BaBar at PEP-II, Belle at KEKB

- 2001: both observe CP asymmetry in “golden decay channel”  $B^0 \rightarrow J/\psi K^0_s$
- measured values in good agreement with CKM prediction



## Many more and much more precise results

- BaBar/Belle, CDF/D0 at Tevatron, now LHCb
  - results so far in very good agreement with CKM predictions ( 2-3 $\sigma$  deviations came and went)
- } remainder of this lecture
- Babar and Belle stopped data taking, Belle collected  $\sim 1 \text{ ab}^{-1}$
  - Tevatron stopped in autumn 2011  $\rightarrow$  CDF/D0 collected  $\sim 9 \text{ fb}^{-1}$
  - LHCb collected  $\sim 1 \text{ fb}^{-1}$  at 7 TeV in 2011 and  $\sim 2 \text{ fb}^{-1}$  at 8 TeV in 2012
    - $b\bar{b}$  production cross section  $\sim 5 \times$  Tevatron,  $\sim 500'000 \times$  Babar/Belle
    - many analyses ongoing, already  $\sim 80$  papers published
  - LHC shutdown in 2013/2014, resume at  $\geq 13 \text{ TeV}$  in 2015
    - another factor two in  $b\bar{b}$  production cross section
  - “Belle II” under construction; goal: collect  $\sim 50 \times$  Belle luminosity by 2022



- **Part I: Introduction**
  - what is (quark) flavour physics and why is it so exciting?
  - how we got here: brief history of flavour physics in the 20<sup>th</sup> century
- **Part II: Particle-Antiparticle Mixing**
  - a short summary of the formalism (don't worry, I'm an experimentalist ... )
  - introduce experimental facilities and techniques
- **Part III: Precision tests of the Standard Model**
  - CP violating observables:  $\sin 2\beta$ , CKM angle  $\gamma$ ,  $B_s^0 \bar{B}_s^0$  mixing phase  $\phi_s$
  - rare decays: search for  $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ , angular observables in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

Applies for all neutral meson systems ( $K^0\bar{K}^0$ ,  $D^0\bar{D}^0$ ,  $B^0\bar{B}^0$ ,  $B_s^0\bar{B}_s^0$ )

- different phenomenologies due to different mass and lifetime differences
- flavour mixing through box diagrams  $\rightarrow$  coupled system

$$|\psi(t)\rangle = a(t)|P^0\rangle + b(t)|\bar{P}^0\rangle$$

- time evolution described by two-component Schrödinger equation

$$-i \frac{\partial}{\partial t} \begin{pmatrix} a(t) \\ b(t) \end{pmatrix} = H \begin{pmatrix} a(t) \\ b(t) \end{pmatrix}$$

- with an effective Hamiltonian  $H$ 
  - $H$  is not Hermitian since it does not include decay products
- decompose  $H$  into Hermitian parts:

$$M \equiv \frac{1}{2} (H + H^\dagger) \quad ; \quad \frac{1}{2} \Gamma \equiv \frac{1}{2i} (H - H^\dagger)$$

$$H = M - \frac{i}{2} \Gamma = \begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix} - \frac{i}{2} \begin{pmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{21} & \Gamma_{22} \end{pmatrix}$$

- assume CPT is conserved: particle/antiparticle have same mass/lifetime

$$\left. \begin{aligned} M &\equiv M_{11} = M_{22} \\ \Gamma &\equiv \Gamma_{11} = \Gamma_{22} \end{aligned} \right\} \Rightarrow H = \begin{pmatrix} M - \frac{i}{2}\Gamma & M_{12} - \frac{i}{2}\Gamma_{12} \\ M_{12}^* - \frac{i}{2}\Gamma_{12}^* & M - \frac{i}{2}\Gamma \end{pmatrix}$$

- Eigenvalues

$$\omega_{H,L} = M - \frac{i}{2}\Gamma \pm \sqrt{\left(M_{12} - \frac{i}{2}\Gamma_{12}\right)\left(M_{12}^* - \frac{i}{2}\Gamma_{12}^*\right)} \equiv m_{H,L} - \frac{i}{2}\Gamma_{H,L}$$

- Eigenstates (labeled by their mass, H for "heavy", L for "light")

$$\left|P_{H,L}\right\rangle = p\left|P^0\right\rangle \mp q\left|\bar{P}^0\right\rangle \quad \text{with} \quad \frac{q}{p} = -\sqrt{\frac{H_{21}}{H_{12}}} = -\sqrt{\frac{M_{12}^* - \frac{i}{2}\Gamma_{12}^*}{M_{12} - \frac{i}{2}\Gamma_{12}}}$$

- these are states with well-defined mass and decay width

$$\left|P_H(t)\right\rangle = \left(p\cdot\left|P^0\right\rangle - q\cdot\left|\bar{P}^0\right\rangle\right) \cdot e^{-im_H t} \cdot e^{-\Gamma_H t/2}$$

$$\left|P_L(t)\right\rangle = \left(p\cdot\left|P^0\right\rangle + q\cdot\left|\bar{P}^0\right\rangle\right) \cdot e^{-im_L t} \cdot e^{-\Gamma_L t/2}$$

- time evolution of initially pure flavour states

$$\left| P^0_{(t=0)}(t) \right\rangle = g_+(t) \cdot |P^0\rangle + \frac{q}{p} \cdot g_-(t) \cdot |\bar{P}^0\rangle$$

$$\left| \bar{P}^0_{(t=0)}(t) \right\rangle = g_+(t) \cdot |\bar{P}^0\rangle + \frac{p}{q} \cdot g_-(t) \cdot |P^0\rangle$$

with:

$$\begin{aligned} g_{\pm}(t) &= \frac{1}{2} \left( e^{-\omega_L t} \pm e^{-\omega_H t} \right) \\ &= \frac{1}{2} e^{-iMt} e^{-\Gamma t/2} \left( e^{+i\Delta m t/2} e^{+\Delta\Gamma t/4} \pm e^{-i\Delta m t/2} e^{-\Delta\Gamma t/4} \right) \end{aligned}$$

$$\Delta m \equiv m_H - m_L > 0$$

$$\Delta\Gamma \equiv \Gamma_H - \Gamma_L$$

- mixing probabilities as a function of time  $t$ :

$$\text{Prob}_{(P^0 \rightarrow P^0)}(t) = \text{Prob}_{(\bar{P}^0 \rightarrow \bar{P}^0)}(t) = |g_+(t)|^2 = \frac{1}{2} e^{-\Gamma t} \left\{ \cosh\left(\frac{\Delta\Gamma}{2} \cdot t\right) + \cos(\Delta m \cdot t) \right\}$$

$$\text{Prob}_{(P^0 \rightarrow \bar{P}^0)}(t) = \left| \frac{q}{p} \right|^2 \cdot |g_-(t)|^2 = \frac{1}{2} \cdot \left| \frac{q}{p} \right|^2 \cdot e^{-\Gamma t} \cdot \left\{ \cosh\left(\frac{\Delta\Gamma}{2} \cdot t\right) - \cos(\Delta m \cdot t) \right\}$$

$$\text{Prob}_{(\bar{P}^0 \rightarrow P^0)}(t) = \left| \frac{p}{q} \right|^2 \cdot |g_-(t)|^2 = \frac{1}{2} \cdot \left| \frac{p}{q} \right|^2 \cdot e^{-\Gamma t} \cdot \left\{ \cosh\left(\frac{\Delta\Gamma}{2} \cdot t\right) - \cos(\Delta m \cdot t) \right\}$$

- observable time-dependent asymmetries

$$a_{\text{mix}}(t) \equiv \frac{N(P^0 \rightarrow P^0) - N(P^0 \rightarrow \bar{P}^0)}{N(P^0 \rightarrow P^0) + N(P^0 \rightarrow \bar{P}^0)} = \frac{\cos(\Delta m \cdot t) + \delta \cdot \cosh(\Delta \Gamma \cdot t/2)}{\cosh(\Delta \Gamma \cdot t/2) + \delta \cdot \cos(\Delta m \cdot t)}$$

$$\bar{a}_{\text{mix}}(t) \equiv \frac{N(\bar{P}^0 \rightarrow \bar{P}^0) - N(\bar{P}^0 \rightarrow P^0)}{N(\bar{P}^0 \rightarrow \bar{P}^0) + N(\bar{P}^0 \rightarrow P^0)} = \frac{\cos(\Delta m \cdot t) - \delta \cdot \cosh(\Delta \Gamma \cdot t/2)}{\cosh(\Delta \Gamma \cdot t/2) - \delta \cdot \cos(\Delta m \cdot t)}$$

with

$$\delta \equiv \frac{1 - |q/p|^2}{1 + |q/p|^2}$$

$\delta \neq 0 \Leftrightarrow$  CP violation in mixing

- assume for now that CP is conserved in mixing, i.e.  $\delta = 0$

$$a_{\text{mix}}(t) = \bar{a}_{\text{mix}}(t) = \frac{\cos(\Delta m \cdot t)}{\cosh(\Delta \Gamma \cdot t/2)} = \frac{\cos(x \cdot \Gamma \cdot t)}{\cosh(y \cdot \Gamma \cdot t)} \quad \text{with} \quad \left\{ \begin{array}{l} x = \Delta m / \Gamma \\ y = \Delta \Gamma / 2\Gamma \end{array} \right.$$

- oscillation frequency  $x$ : mass difference
  - damping parameter  $y$ : lifetime difference
- } between the two weak Eigenstates

# Mixing: $K^0\bar{K}^0$ and $D^0\bar{D}^0$

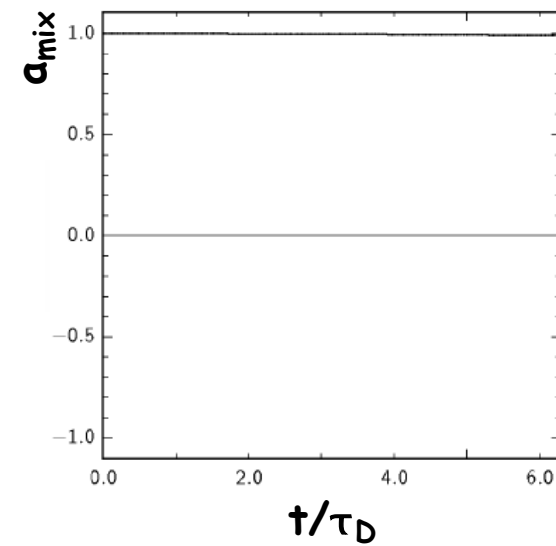
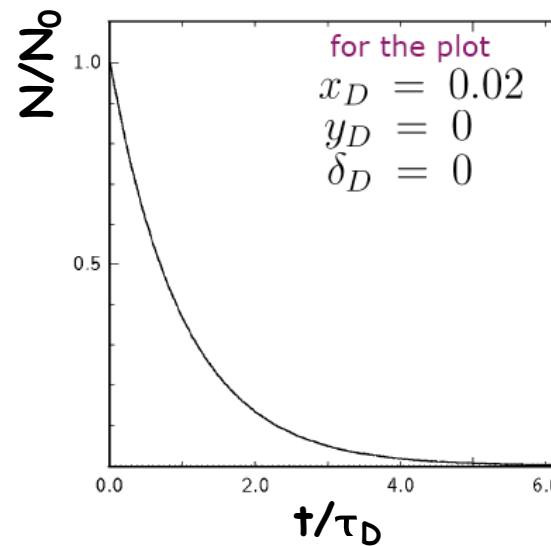
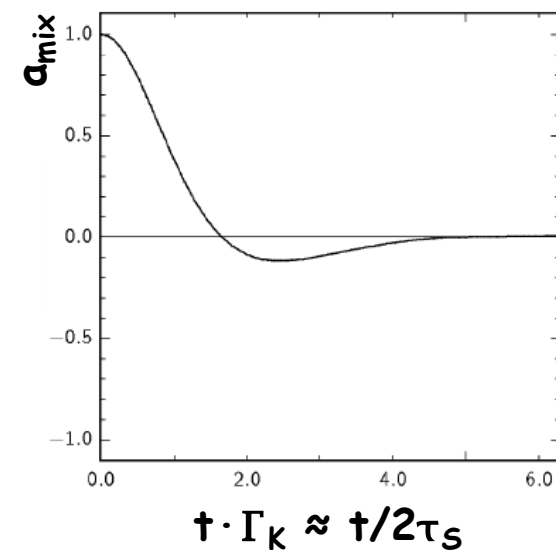
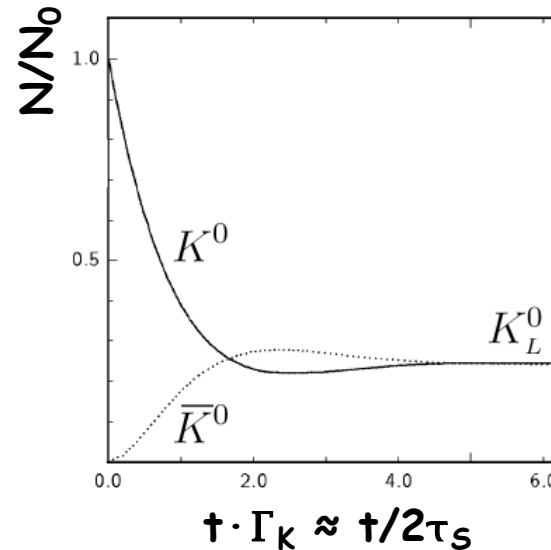
## $K^0\bar{K}^0$

- $x_K \approx 0.95$
- $y_K \approx -0.996$  ( $\tau_L \gg \tau_S$ )
- strong damping, only  $K_L$  left after about one oscillation

## $D^0\bar{D}^0$

- $x_D \approx 0.008$
- $y_D \approx 0.007$
- mixing very small, e.g. time-integrated probability

$$x_D = \frac{x_D^2 + y_D^2}{2(1 + x_D^2)} \approx 3 \times 10^{-5}$$



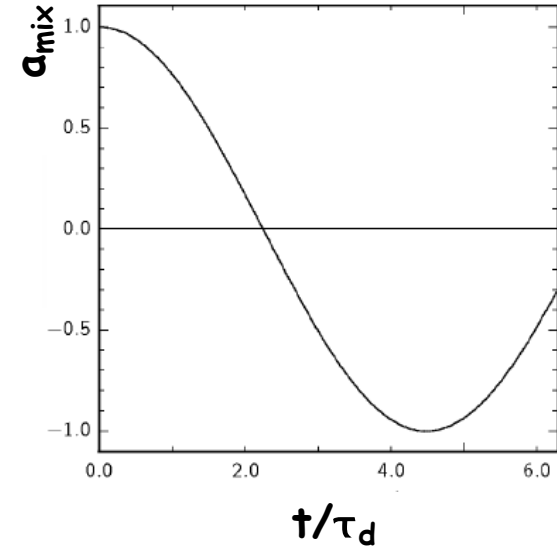
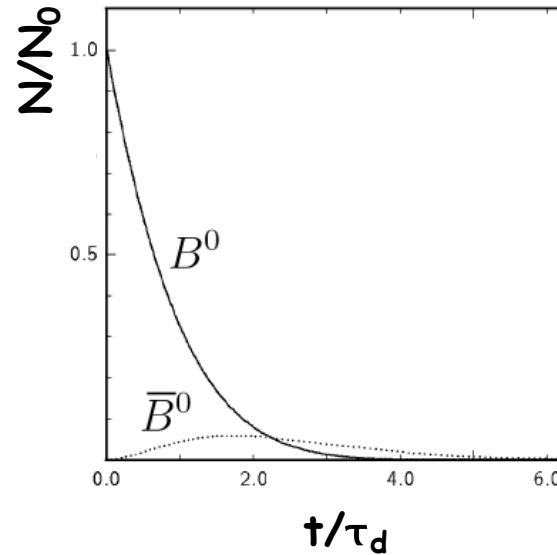
- 2007: first evidence @ B factories; 2012: first observation @ LHCb

# Mixing: $B^0\bar{B}^0$ and $B_s^0\bar{B}_s^0$

## $B^0\bar{B}^0$

- $x_d \approx 0.7$
- $y_d \approx 0$
- significant mixing:

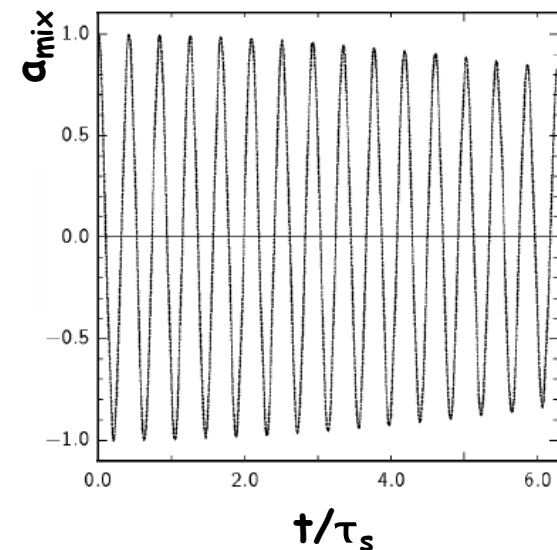
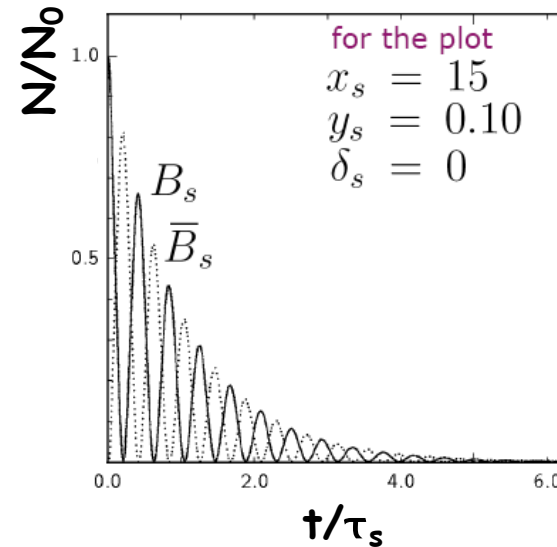
$$\chi_d = \frac{x_d^2}{2(1+x_d^2)} \approx 18\%$$



## $B_s^0\bar{B}_s^0$

- $x_s \approx 26$
- $y_s \approx 0.07$
- very fast oscillation, complete mixing:

$$\chi_s = \frac{x_s^2 + y_s^2}{2(1+x_s^2)} \approx 50\%$$



# $B^0\bar{B}^0$ Oscillations

$B^0\bar{B}^0$  oscillation frequency  $\rightarrow$  length of  $R_+$  side of the Unitarity Triangle

- $B^0\bar{B}^0$  transitions due to the off-diagonal elements of the effective Hamiltonian

$$H_{12} = M_{12} - (i/2) \Gamma_{12}$$

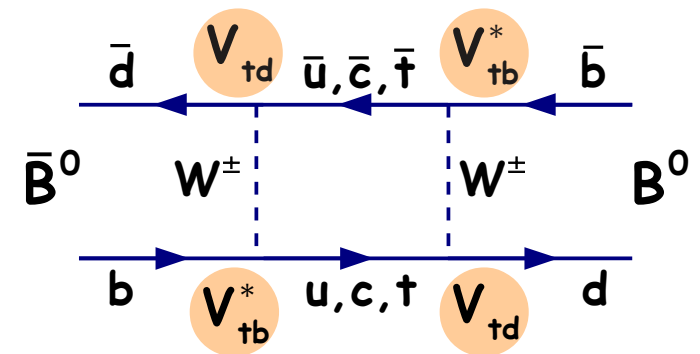
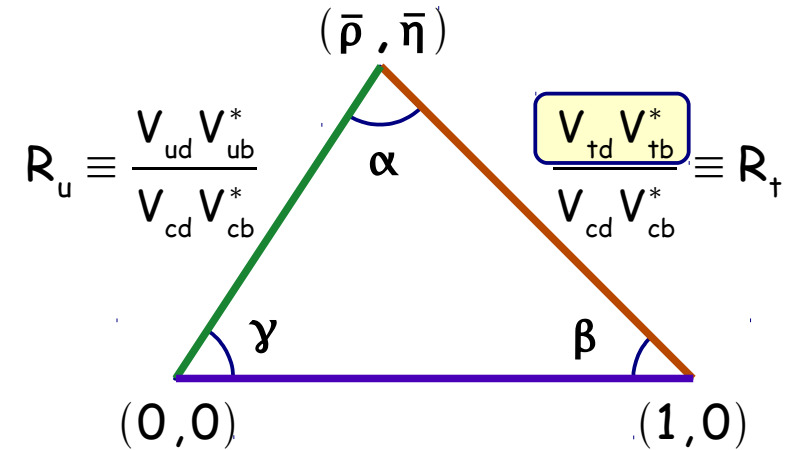
- $M_{12}$ : dispersive part of the amplitude, transitions via off-shell intermediate states

- dominated by t-box:  $M_{12} \propto (V_{td} V_{tb}^*)^2$

- $\Gamma_{12}$ : "absorptive part of the amplitude, transitions via on-shell intermediate states

- dominated by c-box:  $\Gamma_{12} \ll M_{12}$

$$\Rightarrow \Delta m = 2 |M_{12}| \propto |V_{td}|^2 \cdot |V_{tb}|^2$$

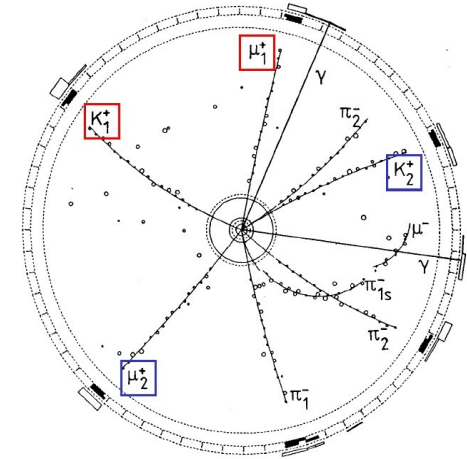




## First observation of time-integrated asymmetry by Argus (1987)

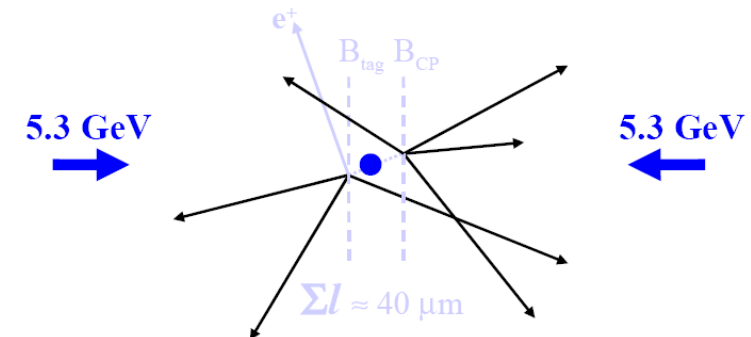
$$e^+ e^- \rightarrow \Upsilon(4s) \rightarrow B^0 \bar{B}^0$$

- look at semi-leptonic decays, count fraction of like-sign dimuon events  $\rightarrow$  gives integrated mixing probability



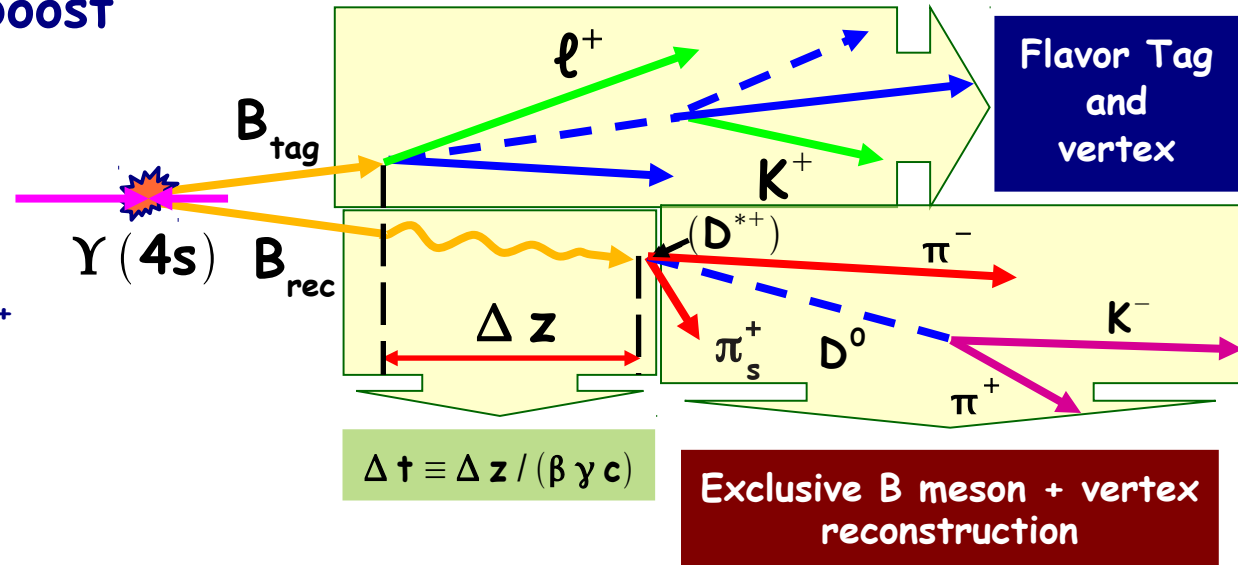
## But: impossible to observe oscillation pattern at Argus

- symmetric beam energies  $\rightarrow$  lab frame =  $\Upsilon(4s)$  rest frame
  - $m_{\Upsilon(4s)} = 10.58 \text{ GeV} \rightarrow p_B = 340 \text{ MeV} \rightarrow \beta\gamma = 0.064$
  - mean B decay length  $c\tau_B \cdot \beta\gamma \sim 30 \mu\text{m}$ , too small to resolve
- $B^0\bar{B}^0$  produced in coherent quantum state, oscillate in phase until one decays
  - need to measure difference of decay times to observe oscillation pattern
  - but  $B^0\bar{B}^0$  produced back-to-back, cannot reconstruct position of production vertex



## High-luminosity $e^+e^-$ colliders with asymmetric beam energies

- produce  $\Upsilon(4s)$  with Lorentz boost
- Babar: 9 GeV  $e^-$  + 3.1 GeV  $e^+$ 
  - $\beta\gamma = 0.56$ ,  $\langle\Delta z\rangle = 260 \mu\text{m}$
- Belle: 8 GeV  $e^-$  + 3.5 GeV  $e^+$ 
  - $\beta\gamma = 0.425$ ,  $\langle\Delta z\rangle = 200 \mu\text{m}$

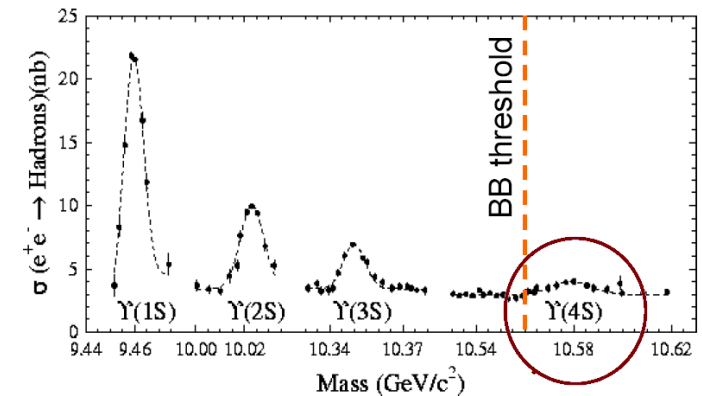


## Reconstruction strategy:

- reconstruct  $B_{rec}$  fully  $\rightarrow$   $B_{rec}$  decay vertex, momentum and flavour at decay
- assign remaining final-state particles to  $B_{tag}$  decay (no full reconstruction)
  - reconstruct  $B_{tag}$  decay vertex  $\rightarrow$  fixes  $t=0$  for oscillation measurement
  - infer flavour of  $B_{tag}$  at its decay  $\rightarrow$  fixes flavour of  $B_{rec}$  at  $t=0$
- $B_{rec}$  oscillated (not oscillated) if opposite (same) flavour at  $t=0$  and decay
- calculate oscillation time from  $B_{rec}$  momentum and  $\Delta z$  of decay vertices

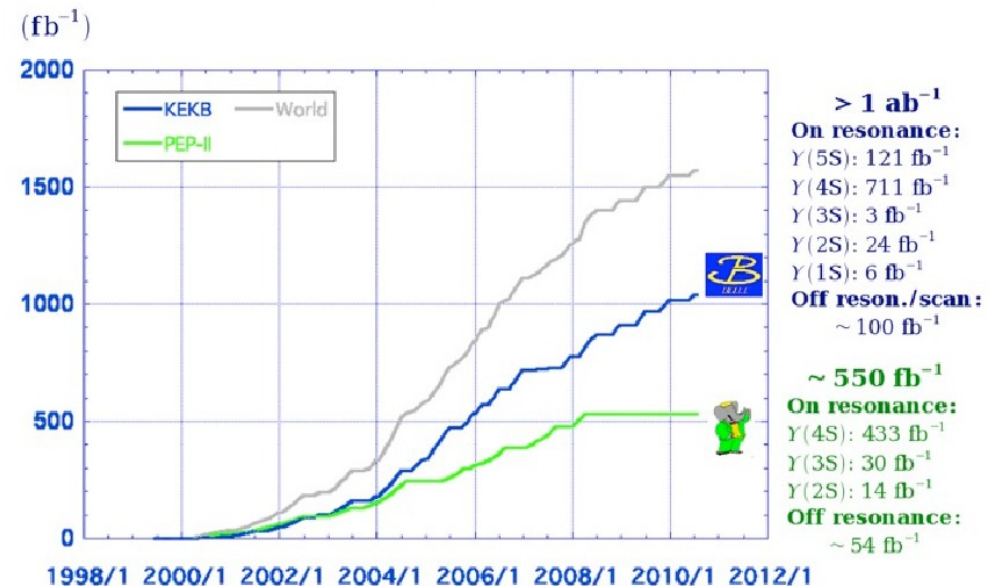
## $\Upsilon(4s)$ resonance: bound $b\bar{b}$ state just above $B\bar{B}$ threshold

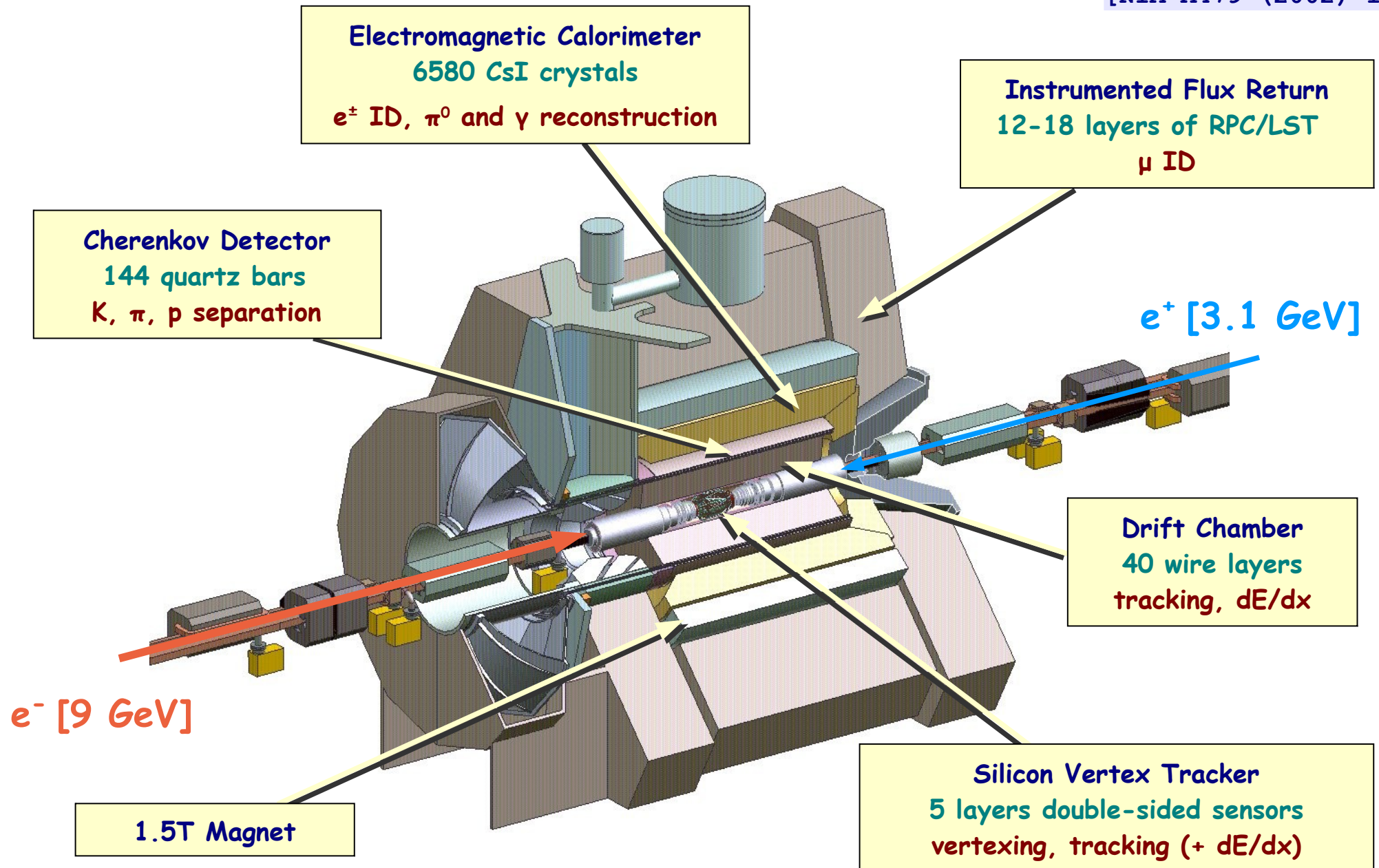
- decays  $\sim 50\%$  to  $B^+B^-$  and  $\sim 50\%$  to  $B^0\bar{B}^0$
- $\sigma_{b\bar{b}} \approx 1 \text{ nb} \rightarrow$  with  $1 \text{ fb}^{-1}$  produce  $10^6$   $B\bar{B}$  pairs
- $\sigma_{b\bar{b}} / \sigma_{\text{tot}} \approx 0.25 \rightarrow$  large fraction of B events
- “clean” events  $\rightarrow$  only tracks from B decays

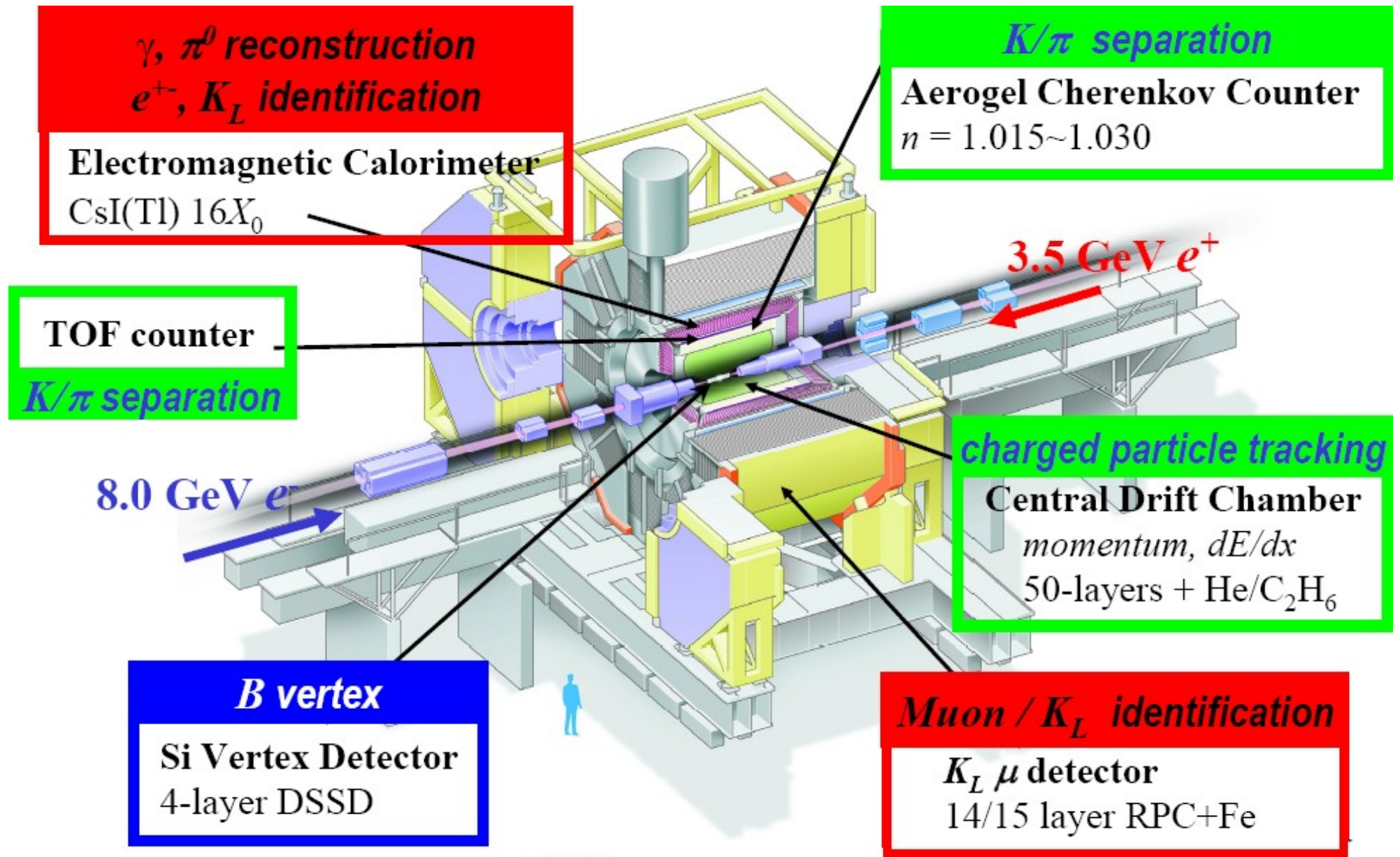


## Need highest possible luminosity to beat small production cross section

- PEP-II ring at SLAC, California
  - peak luminosity  $12 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
  - integrated luminosity:  $553 \text{ fb}^{-1}$
- KEK-B ring at KEK, Japan
  - peak luminosity  $21 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
  - integrated luminosity:  $1040 \text{ fb}^{-1}$







# Event Selection

## Kinematic variables: exploit precisely known beam energy

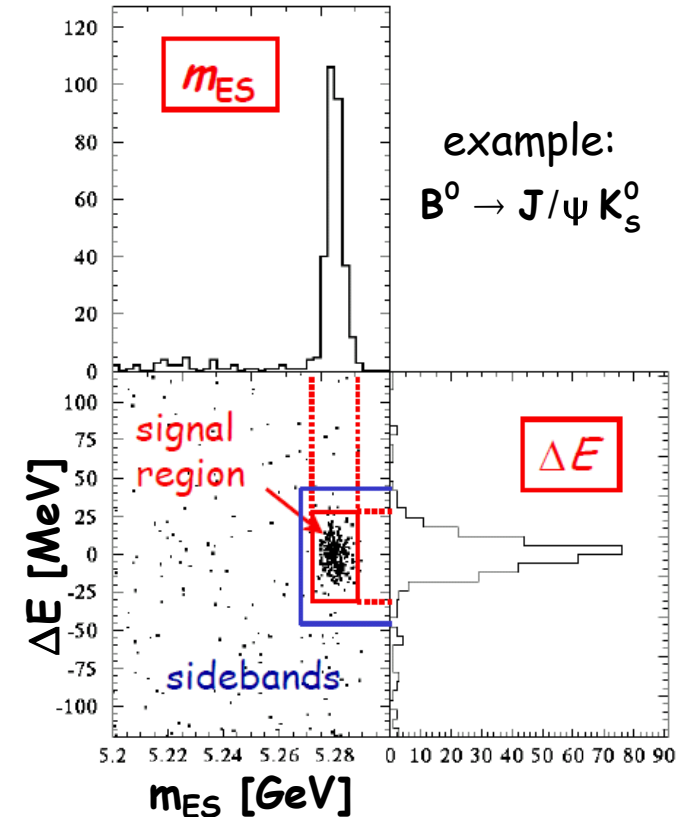
- energy conservation in center-of-mass frame

$$E_B^* = \frac{\sqrt{s}}{2} = E_{\text{beam}}^* \quad \left\{ \begin{array}{l} \Delta E \equiv E_B^* - E_{\text{beam}}^* = 0 \\ m_{\text{ES}} \equiv \sqrt{(E_{\text{beam}}^*)^2 - (\vec{p}_B^*)^2} \end{array} \right.$$

- $m_{\text{ES}}$ : “energy-substituted” invariant mass

- $E_{\text{beam}}^*$ : beam energy, known to  $\sim 2.5$  MeV

- $E_B^*$ : energy of B meson, only known to  $\sim 10$ -40 MeV from detector resolution



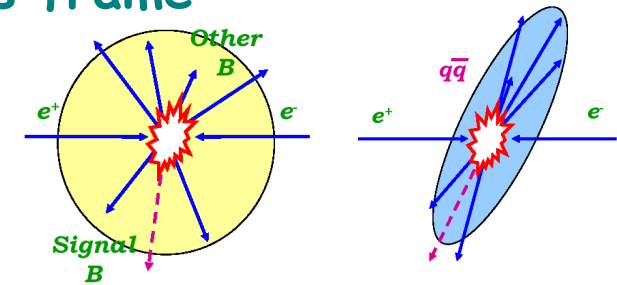
## Event shape:

- B mesons produced almost at rest in center-of-mass frame

→ decay products isotropically distributed

- light quarks produced with high momenta

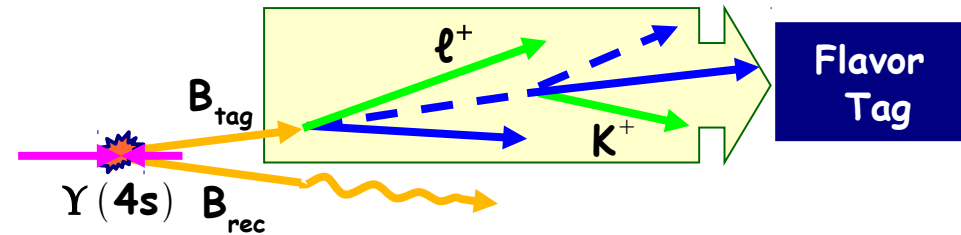
→ boost along flight direction → jet-like topology



# Flavour Tagging

Infer flavour of  $B_{rec}$  at  $t=0$  from decay properties of  $B_{tag}$

- lepton tag ( $b \rightarrow c \ell^- \bar{\nu}$ )
  - small wrong-tag fraction  $< 5\%$
  - contamination of wrong-sign leptons from  $b \rightarrow c \rightarrow s$  cascade decays small
  - clean identification of  $e^\pm, \mu^\pm$
  - low efficiency: BF only 11% each
- kaon tag ( $b \rightarrow c \rightarrow s$ )
  - high efficiency: 66% of  $B^0$  decay to  $K^+$
  - but significant wrong-tag fraction:
    - 13% of  $B^0$  have a  $K^-$  in the decay chain
    - contamination from mis-identified  $\pi^+$
- inclusive tags (e.g. decay vertex charge)
  - typically use neural-net techniques
  - high efficiency, high wrong-tag fraction



efficiency  $\varepsilon$ :

fraction of reconstructed events for which flavour tag is obtained

wrong-tag fraction  $\omega$ :

fraction of tagged events for which tagging decision is wrong

figure of merit:

effective tagging power

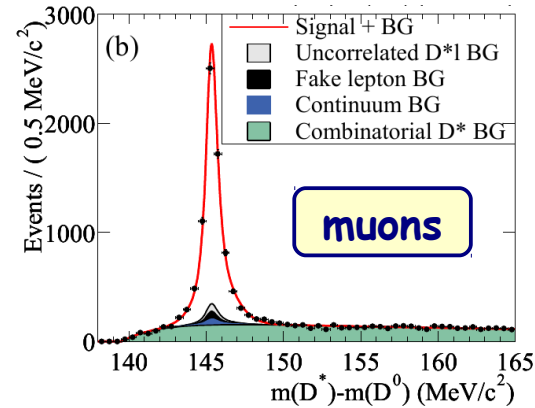
$$\varepsilon \cdot D^2 = \varepsilon \cdot (1 - 2\omega)^2$$

total tagging power at B factories, combining all algorithms

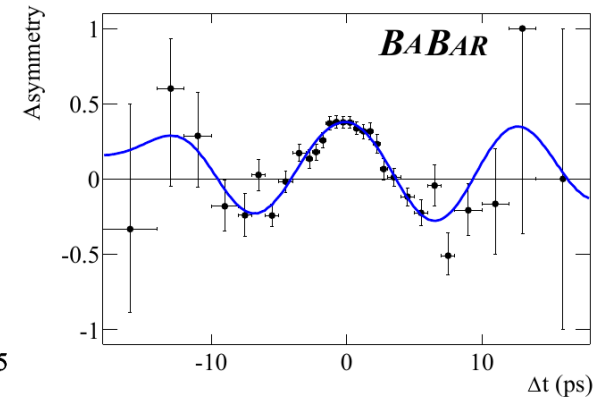
$$\varepsilon \cdot D^2 \approx 30\%$$

## Semi-leptonic decays:

- $B^0 \rightarrow D^{*-} \ell^+ \nu_\ell$  with  $D^{*-} \rightarrow \bar{D}^0 \pi^-$
- reasonable branching fraction
- clean event sample
  - soft pion from  $D^{*-} \rightarrow \bar{D}^0 \pi^-$
- but neutrino not reconstructed
- B flavour from lepton charge

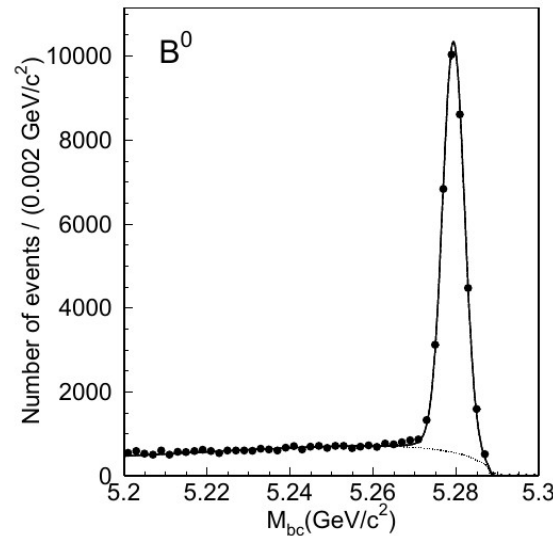


[PRD 67 (2003) 072002]

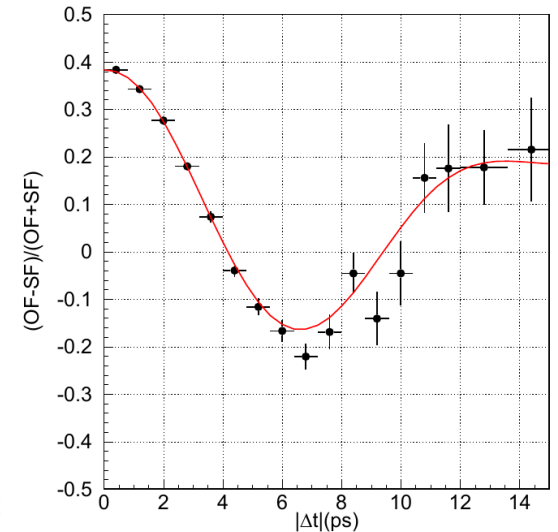


## Hadronic decays:

- $B^0 \rightarrow D^{*-} \pi^+$  with  $D^{*-} \rightarrow \bar{D}^0 \pi^-$
- $B^0 \rightarrow J/\psi K^{*0}$  with  $K^{*0} \rightarrow K^+ \pi^-$
- clean event samples
- all particles reconstructed
- but small branching fractions
- B flavour from charge of fast pion ( $D^{*-} \pi^+$ ) or Kaon ( $J/\psi K^{*0}$ )

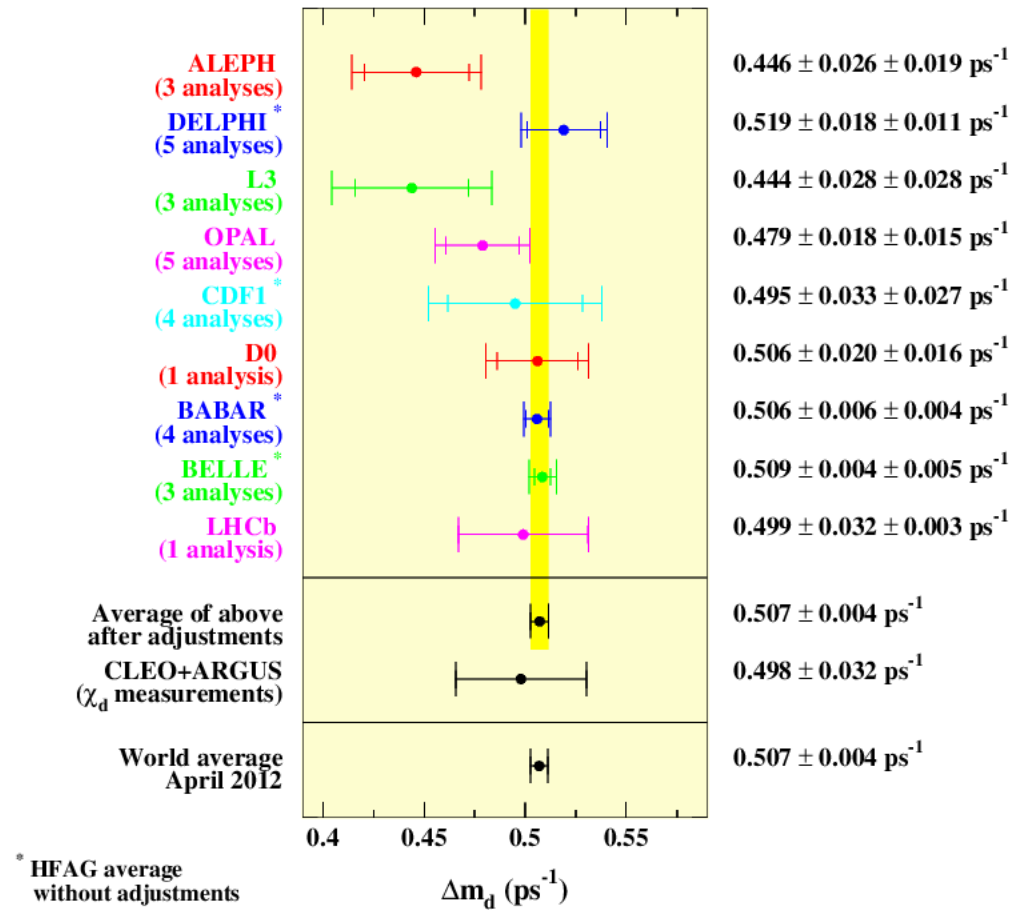
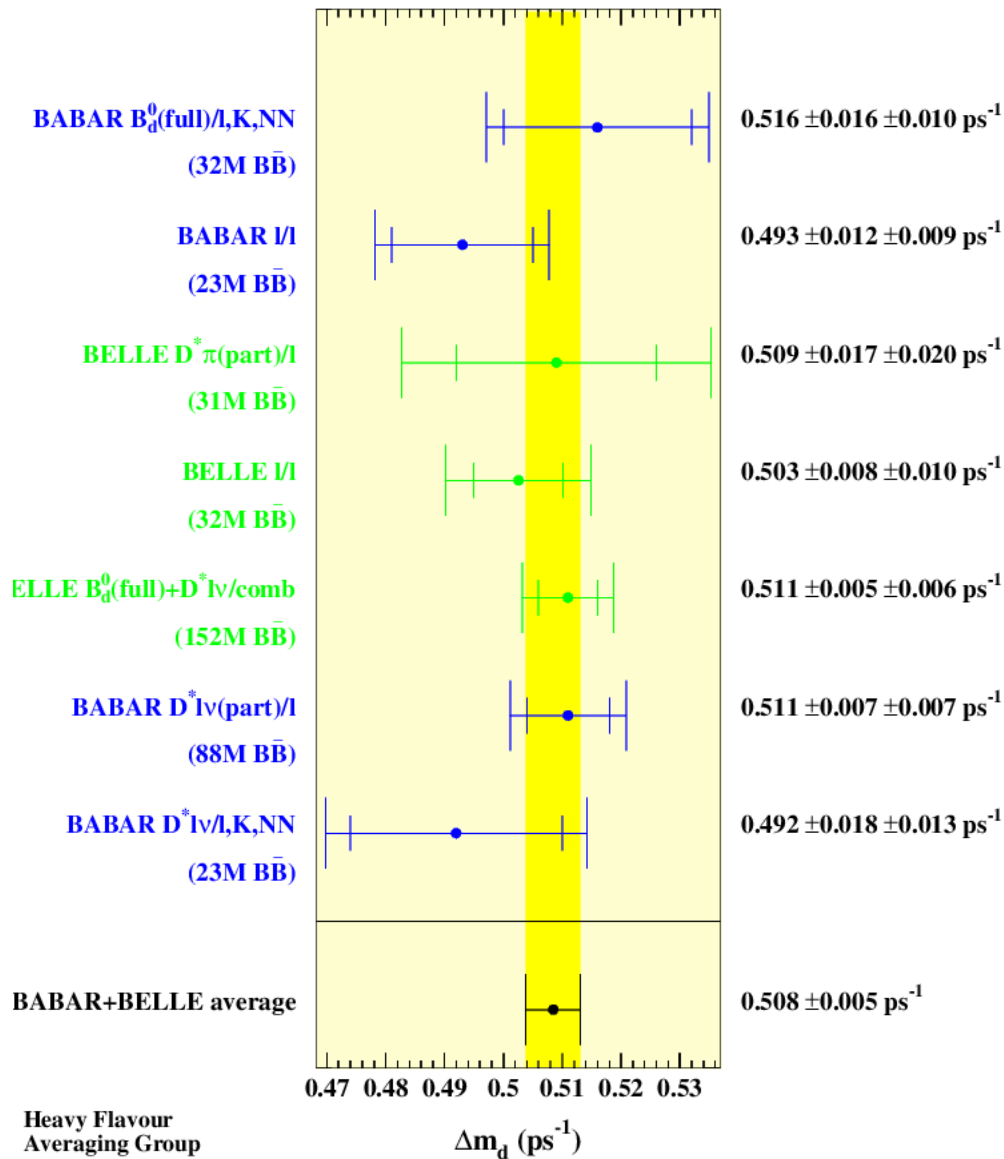


[PRD 71 (2005) 072003]





# Results $\Delta m_d$



**Heavy Flavour Averaging Group**  
[\[http://www.slac.stanford.edu/xorg/hfag/\]](http://www.slac.stanford.edu/xorg/hfag/)

# Theory Uncertainties

Uncertainty on  $|V_{tb}|^2 \cdot |V_{td}|^2$  dominated by non-perturbative QCD factors

$$\Delta m_d = \frac{G_F}{6\pi^2} \cdot m_W^2 \cdot \eta_b \cdot S_0\left(\frac{m_t^2}{m_W^2}\right) \cdot m_{B_d} \cdot f_{B_d}^2 \cdot \hat{B}_{B_d} \cdot |V_{tb}|^2 |V_{td}|^2$$

Fermi constant  $\rightarrow$   $G_F$   
 perturbative QCD  $\rightarrow$   $S_0\left(\frac{m_t^2}{m_W^2}\right)$   
 "Inami-Lim function" for box diagram  $\rightarrow$   $S_0\left(\frac{m_t^2}{m_W^2}\right)$   
 W-boson mass  $\rightarrow$   $m_W$   
 $B_d$  mass  $\rightarrow$   $m_{B_d}$   
 decay constant  $\rightarrow$   $f_{B_d}$   
 "bag parameter"  $\rightarrow$   $\hat{B}_{B_d}$   
 $|V_{tb}|^2 |V_{td}|^2$

- best determination of  $f_{B_d}^2$  and  $\hat{B}_{B_d}$  from lattice QCD  $\rightarrow$  uncertainty  $\sim 10\%$

Theory uncertainties partially cancel in the ratio  $\Delta m_d / \Delta m_s$

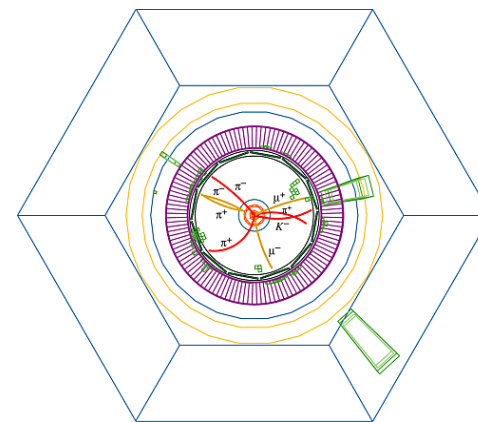
- uncertainty from lattice QCD  $\sim 3\%$
- still measure  $R_+$  side of unitarity triangle, since  $|V_{tb}|^2 \cdot |V_{ts}|^2$  hardly depends on  $\rho$  and  $\eta$
- measure  $\Delta m_s$  from  $B_s^0 \bar{B}_s^0$  oscillation frequency
- $B_s^0$  not produced at the  $\Upsilon(4s) \rightarrow$  hadron colliders

$$\frac{\Delta m_d}{\Delta m_s} = \frac{m_{B_d}}{m_{B_s}} \cdot \frac{f_{B_d}^2 \hat{B}_{B_d}}{f_{B_s}^2 \hat{B}_{B_s}} \cdot \frac{|V_{tb}|^2 |V_{td}|^2}{|V_{tb}|^2 |V_{ts}|^2}$$

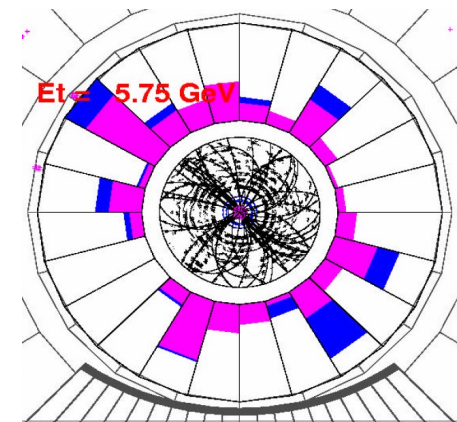
## Advantages and disadvantages with respect to $e^+e^- \rightarrow \Upsilon(4s)$ B factories

- all species of b hadrons produced:  
 $B^\pm, B^0, B_s^0, B_c^+, \Lambda_b$
- $\sigma_{b\bar{b}}$  much higher than at B factories
- $\sigma_{b\bar{b}}/\sigma_{\text{tot}}$  much smaller than at B factories
- large number of additional particles from underlying hadronic interaction
- selective and efficient trigger vital
- exploit features of B decays:
  - B mesons heavy  $\rightarrow$  decay products have large transverse momentum  $p_T$
  - B mesons live long  $\rightarrow$  decay products have large impact parameters with respect to primary vertex

Facility	$\sqrt{s}$	$\sigma_{b\bar{b}}$ [nb]	$\sigma_{b\bar{b}}/\sigma_{\text{tot}}$
$e^+e^- @ \Upsilon(4s)$	10.58 GeV	1	0.25
HERA-B pA	42 GeV	$\sim 30$	$10^{-6}$
Tevatron $p\bar{p}$	1.96 TeV	$5 \times 10^3$	$10^{-3}$
LHC pp	7 TeV	$3 \times 10^5$	$10^{-2}$
LHC pp	14 TeV	$6 \times 10^5$	$10^{-2}$



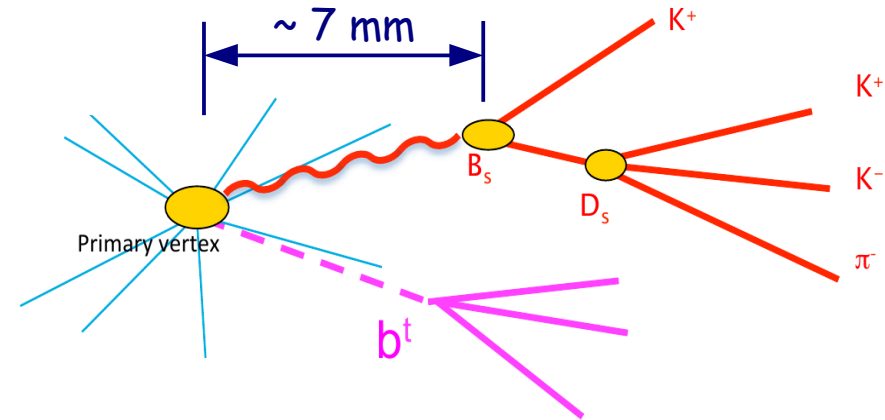
$B^0 \rightarrow J/\psi K_S^0$   
event in BaBar



$J/\psi \rightarrow \mu^+ \mu^-$   
event in CDF

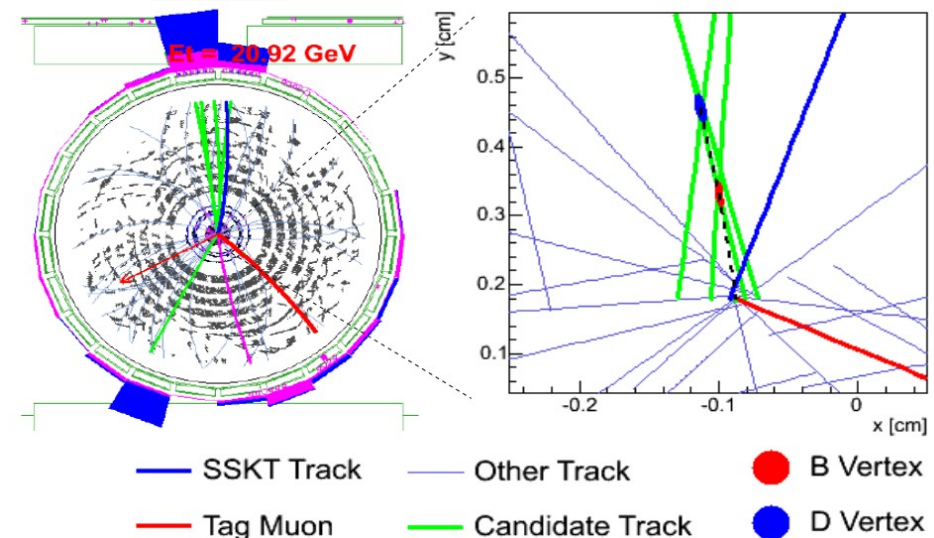
## $b\bar{b}$ pair is not created in a coherent quantum state

- reference for oscillation measurement: primary vertex, B flavour at production
- primary vertex reconstruction: excellent precision due to large number of charged tracks from underlying event



## Flavour tagging: more challenging due to the many extra tracks

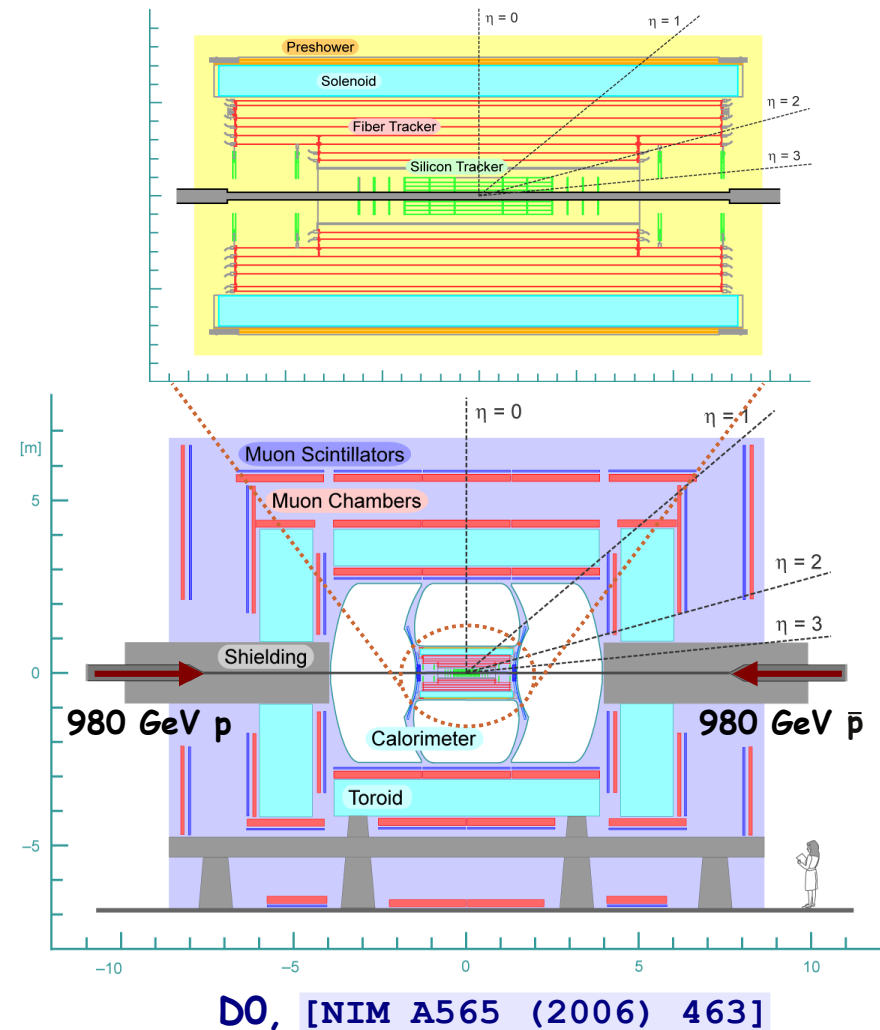
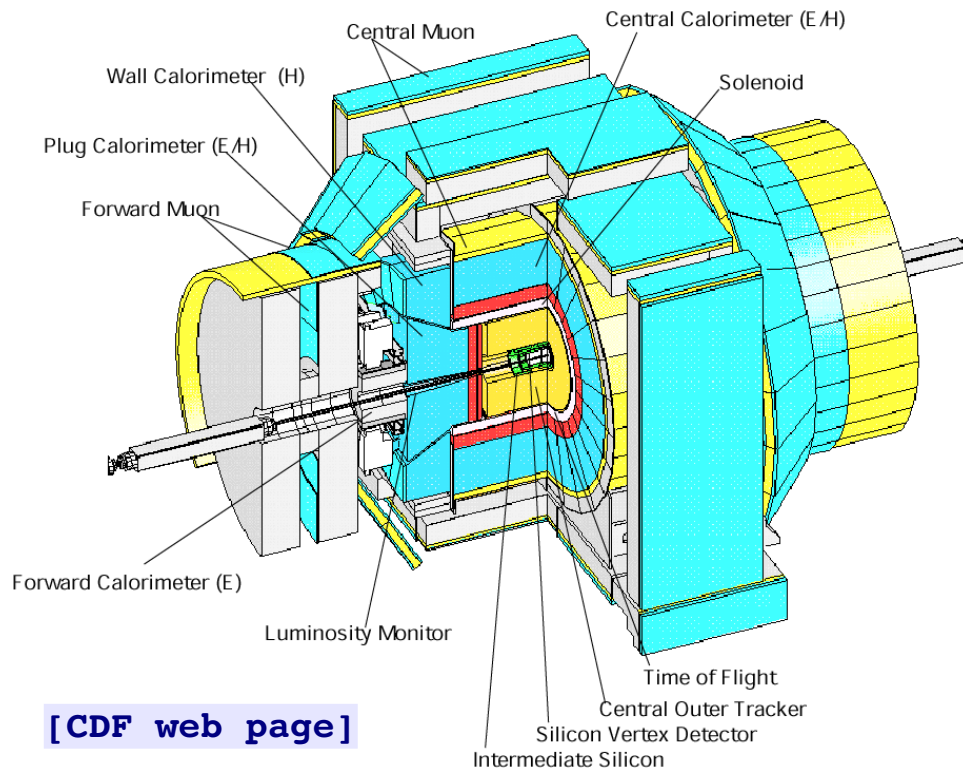
- “opposite side tagging” a la B factories (lepton, kaon, vertex charge)
- in addition “same side tagging”: charge of a kaon from b fragmentation chain or from  $B^{**}$  decays
  - select kaon close to B in phase space
- combined tagging power



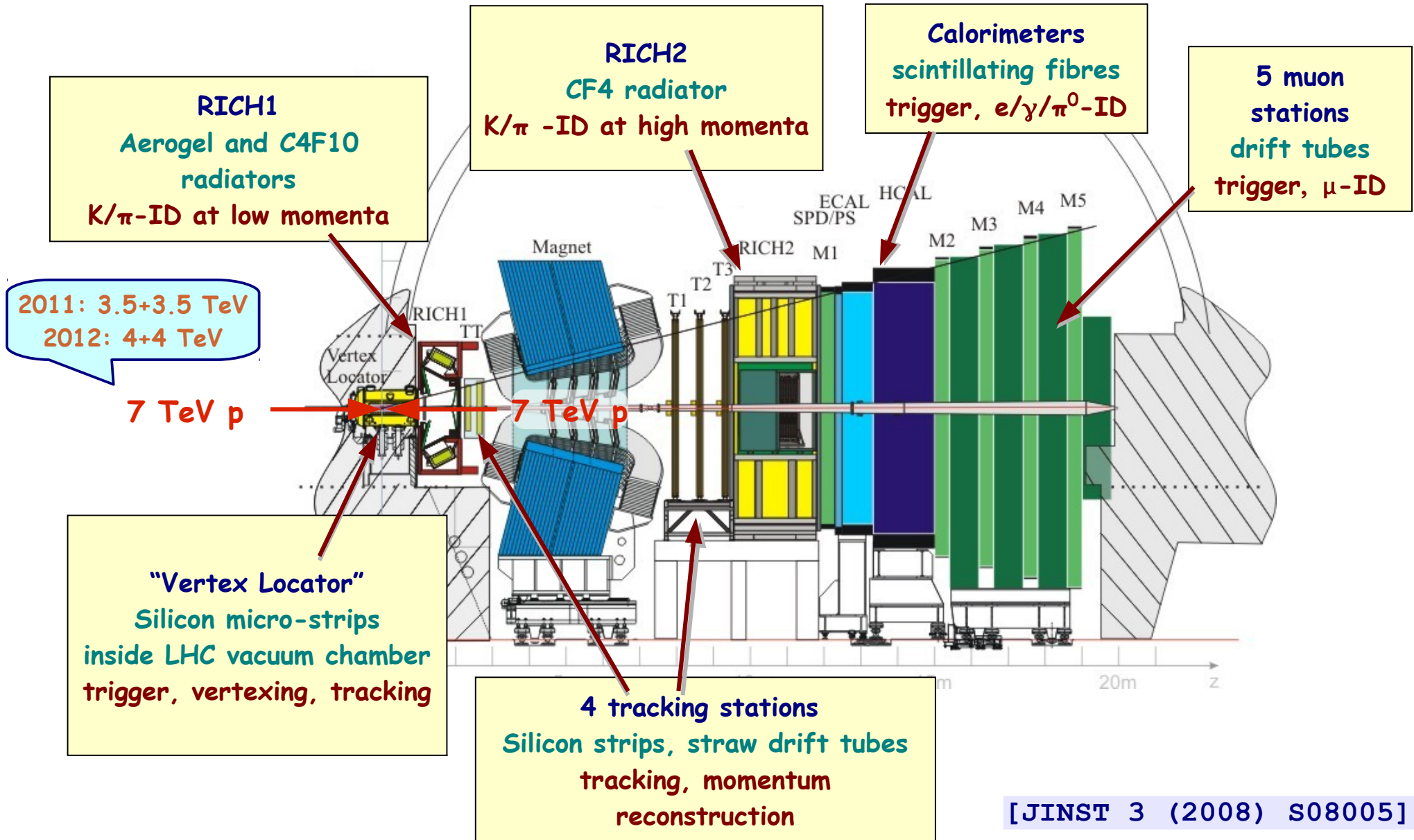
$$\epsilon \cdot D^2 = \text{few \%}$$

## Typical general-purpose detectors

- main focus: high-energy frontier, top-quark physics and Higgs searches
- but also significant B-physics programme
  - e.g. first observation of  $B_s^0 \bar{B}_s^0$  oscillation
  - main limitations: trigger,  $\pi/K$  separation

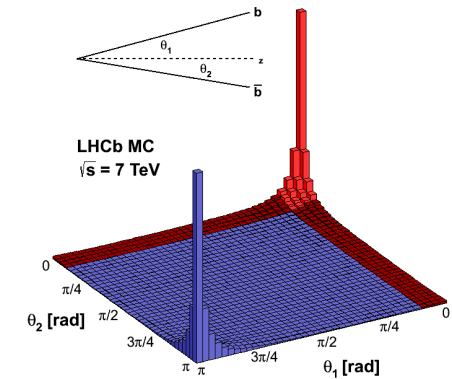


## Dedicated experiment for heavy flavour physics at the LHC



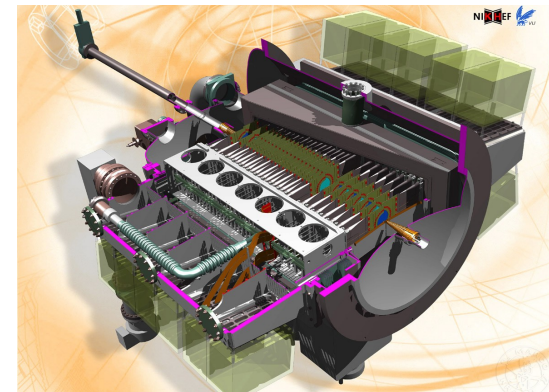
## Key features that distinguish LHCb from general purpose detectors

- forward geometry
- large acceptance,  $b\bar{b}$  production forward peaked
- large Lorentz boost, helps with proper-time resolution
- lower  $p_T$  trigger thresholds than at central detectors



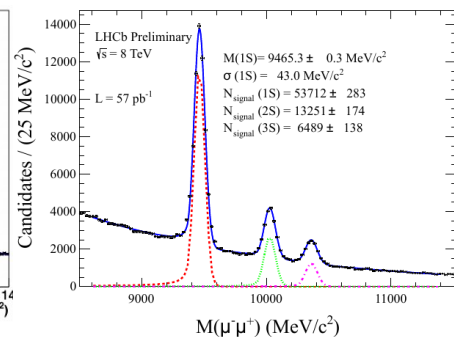
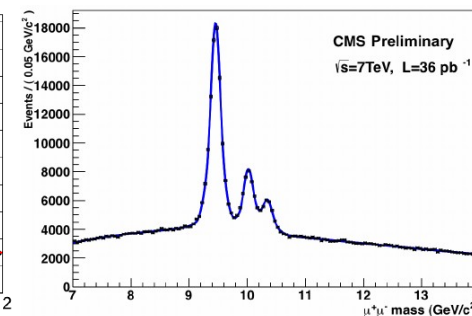
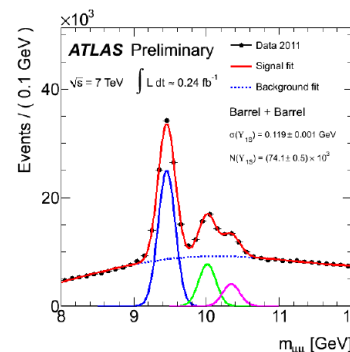
- vertex detector inside LHC vacuum vessel

- impact parameter resolution to identify tracks from B decays ( $\rightarrow$  trigger)
- proper-time resolution, e.g. to resolve fast  $B^0_s \bar{B}^0_s$  oscillations

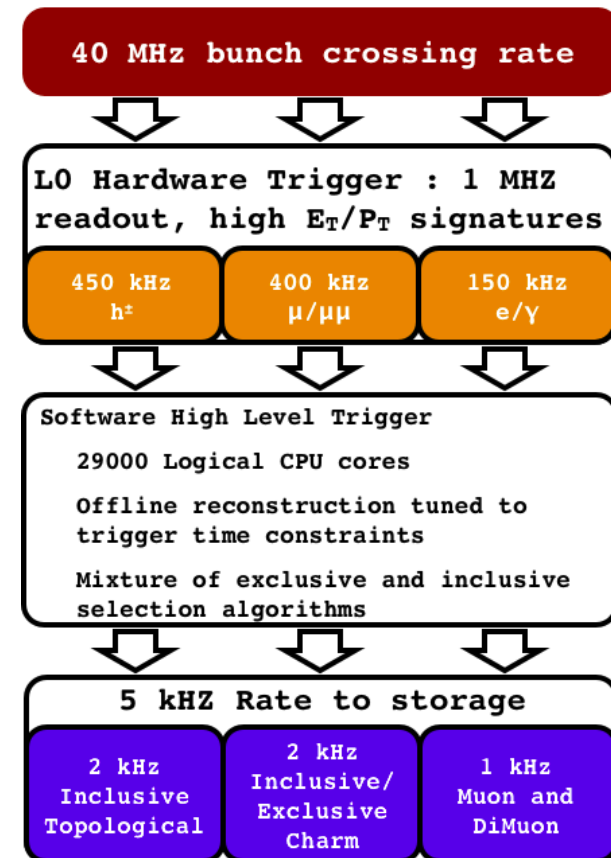
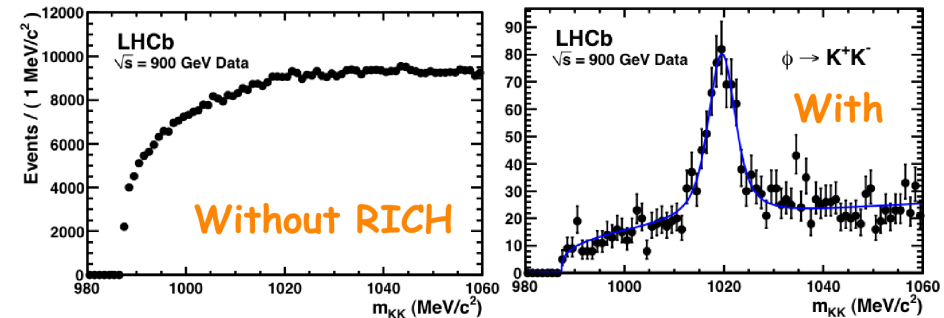


- tracking system

- momentum and invariant mass resolution to fight combinatorial backgrounds



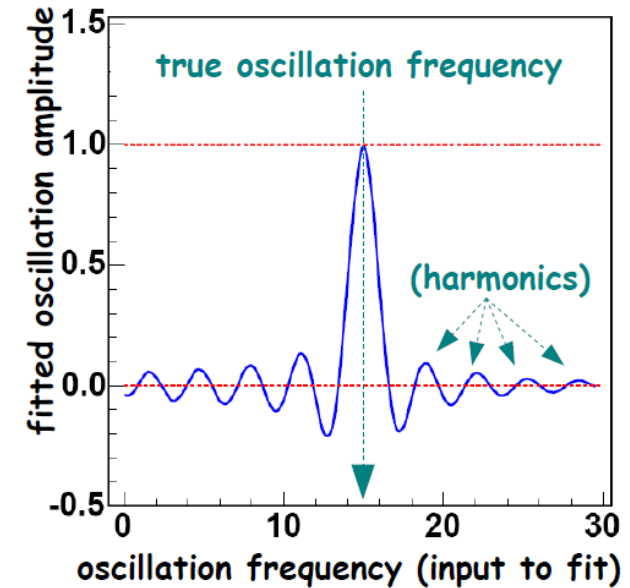
- two RICH detectors for
  - efficient  $K/\pi$  separation from few GeV for flavour tagging up to 100 GeV, e.g. to separate  $B^0 \rightarrow \pi\pi$ ,  $B^0_{(s)} \rightarrow K\pi$ ,  $B^0_s \rightarrow KK$
- flexible, selective and efficient trigger, also for hadronic final states
  - hardware level (L0):
    - high- $p_T$  track segments in muon system
    - high-ET clusters ( $e, h, \gamma$ ) in calorimeters
  - software level (HLT):
    - multi-processor computing farm
    - access to full detector data
  - combined efficiency:
    - 90 % for dimuon channels (e.g.  $J/\psi$ )
    - 30 % for fully hadronic final states





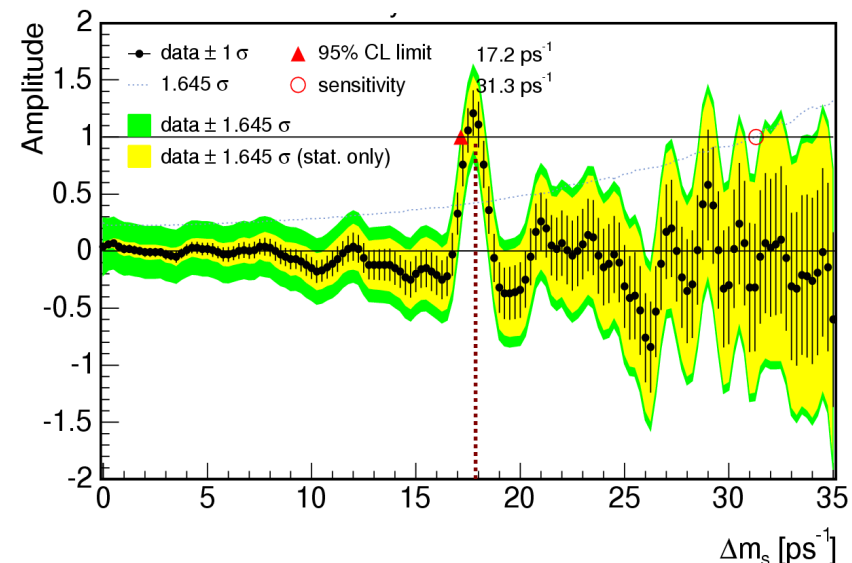
## Perform frequency-domain analysis

- scan over oscillation frequency, fit amplitude  $A$  as a function of the assumed frequency
- normalize to the expected signal amplitude  
→  $A=1$  at true mixing frequency,  $A \sim 0$  elsewhere
- useful method for combining results from different experiments when no clear signals observed
- similar method applied for Higgs searches now



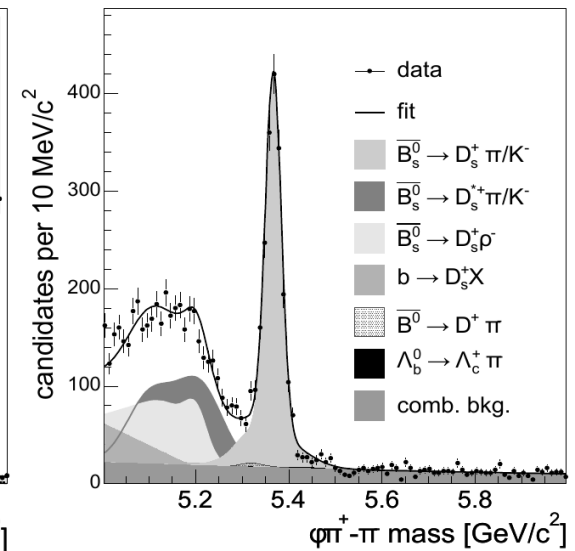
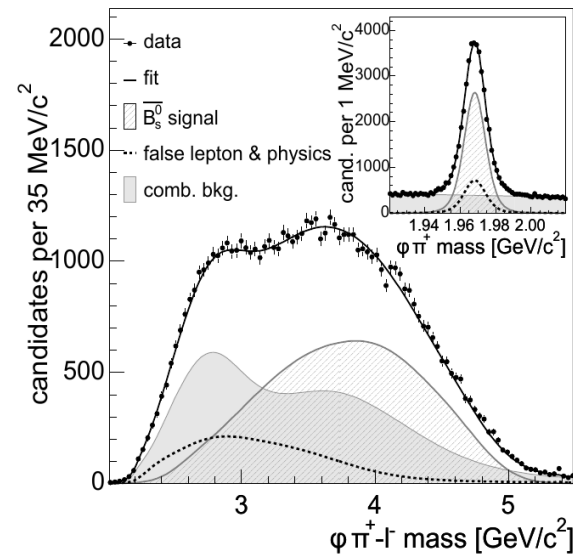
## CDF (2006, $1\text{fb}^{-1}$ )

- clear signal at  $\Delta m_s = 17.75 \text{ ps}^{-1}$   
→ statistical significance  $A/\sigma_A = 6.05$
- lower limit at 95 % CL:  $\Delta m_s = 17.2 \text{ ps}^{-1}$   
→ frequency below which  $A + 1.645 \cdot \sigma_A < 1$
- sensitivity:  $31.3 \text{ ps}^{-1}$   
→ value for which  $1.645 \cdot \sigma_A = 1$



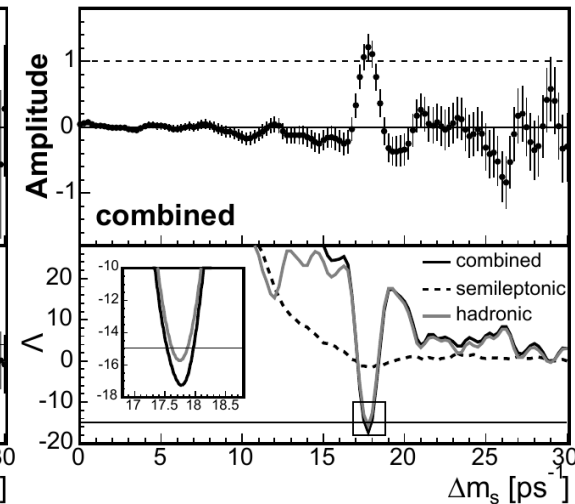
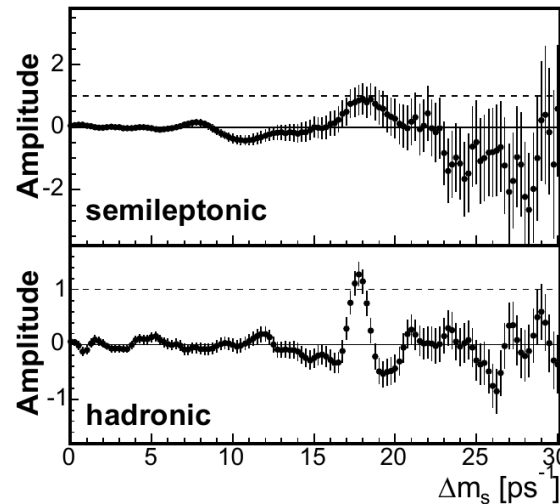
## Semi-leptonic decays:

- $B_s^0 \rightarrow D_s^- \ell^+ \nu_\ell$  with  
 $D_s^- \rightarrow \phi \pi^-, K^{*0} K^-$  or  $\pi^- \pi^+ \pi^-$
- B flavour from lepton charge
- reasonable branching fraction
- but neutrino not reconstructed
  - limits proper time resolution



## Hadronic decays:

- $B_s^0 \rightarrow D_s^- \pi^+, B_s^0 \rightarrow D_s^- 3\pi$  with  
 $D_s^- \rightarrow \phi \pi^-, K^{*0} K^-$  or  $\pi^- \pi^+ \pi^-$
- B flavour from fast pion charge
- smaller branching fraction
- but all particles reconstructed

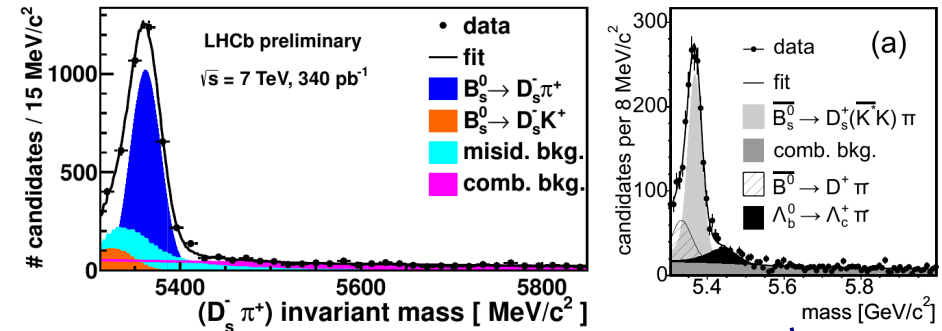
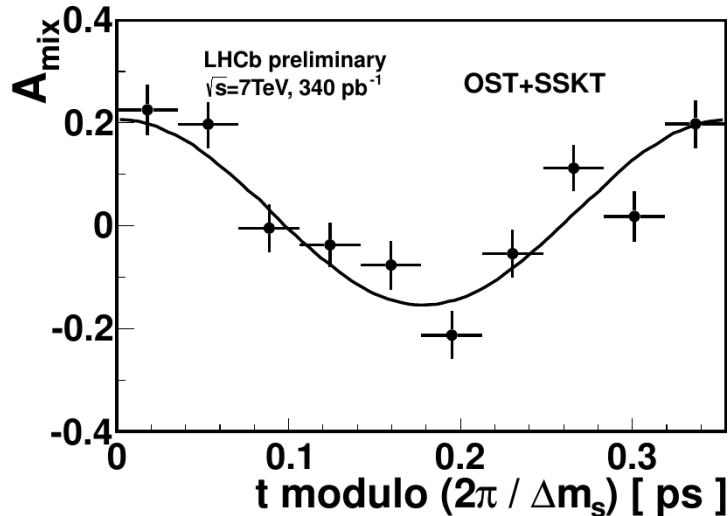


$$\Delta m_s = 17.75 \pm 0.10(\text{stat}) \pm 0.07(\text{syst}) \text{ ps}^{-1}$$

[PRL 97 (2006) 242003]

## Analysis strategy inspired by CDF

- but look only at fully reconstructed hadronic decays  $B_s^0 \rightarrow D_s^- \pi^+$  to fully exploit excellent proper-time resolution
- employ opposite-side tagging and same-side kaon tagging algorithms



	LHCb	CDF
signal event yields $B_s^0 \rightarrow D_s^- \pi^+$	9200 in $0.34 \text{ fb}^{-1}$	4100 in $1 \text{ fb}^{-1}$
proper time resolution	45 ps	87 ps
tagging power opposite side	3.2 %	1.8 %
tagging power same side	1.3 %	3.7 %

$$\Delta m_s = 17.725 \pm 0.041 \pm 0.026 \text{ ps}^{-1}$$

[LHCb-CONF-2011-050] preliminary

- **Part I: Introduction**

- what is (quark) flavour physics and why is it so exciting?
- how we got here: brief history of flavour physics in the 20<sup>th</sup> century

- **Part II: Particle-Antiparticle Mixing**

- a short summary of the formalism (don't worry, I'm an experimentalist ... )
- introduce experimental facilities and techniques

- **Part III: Precision tests of the Standard Model**

- **CP violating observables:**  $\sin 2\beta$ , CKM angle  $\gamma$ ,  $B_s^0 \bar{B}_s^0$  mixing phase  $\phi_s$
- rare decays: search for  $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ , angular observables in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

# CP Violation in Mixing

CP violated in  $P^0\bar{P}^0$  mixing if  $\bar{a}_{\text{mix}}(t) \neq a_{\text{mix}}(t)$

- requires relative phase  $\arg(q/p) \neq 0$  between  $M_{12}$  and  $\Gamma_{12}$

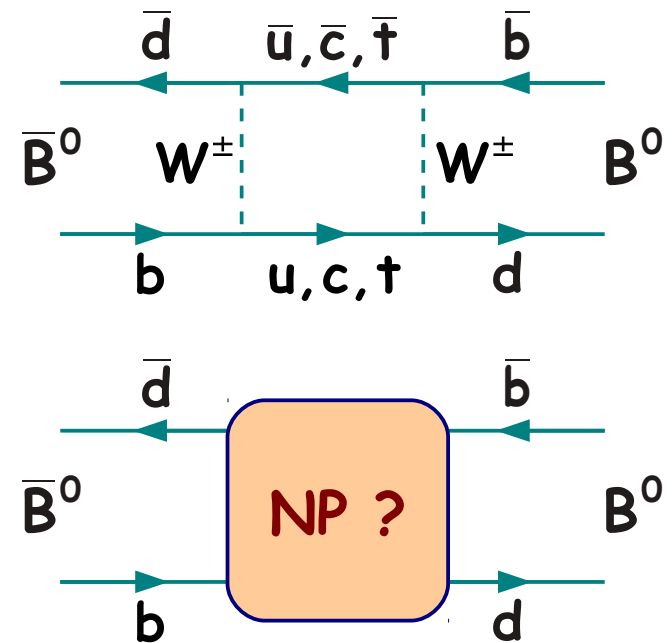
$$\left. \begin{aligned}
 a_{\text{mix}}(t) &= \frac{\cos(\Delta m \cdot t) \boxed{+} \delta \cdot \cosh(\Delta \Gamma \cdot t/2)}{\cosh(\Delta \Gamma \cdot t/2) \boxed{+} \delta \cdot \cos(\Delta m \cdot t)} \\
 \bar{a}_{\text{mix}}(t) &= \frac{\cos(\Delta m \cdot t) \boxed{-} \delta \cdot \cosh(\Delta \Gamma \cdot t/2)}{\cosh(\Delta \Gamma \cdot t/2) \boxed{-} \delta \cdot \cos(\Delta m \cdot t)}
 \end{aligned} \right\} \delta = \frac{1 - |q/p|^2}{1 + |q/p|^2} \quad ; \quad \frac{q}{p} = -\sqrt{\frac{M_{12}^* - (i/2)\Gamma_{12}^*}{M_{12} - (i/2)\Gamma_{12}}}$$

- remember, for  $B^0\bar{B}^0$  (and similar for  $B_s^0\bar{B}_s^0$ )

- $\Gamma_{12}$  dominated by c-box,  $\Gamma_{12} \propto (V_{cd} V_{cb}^*)^2$
- $M_{12}$  dominated by t-box,  $M_{12} \propto (V_{td} V_{tb}^*)^2$
- different weak phases involved, but  $\Gamma_{12} \ll M_{12}$
- expect CP violation in mixing to be very small

- promising hunting ground for New Physics:

**new heavy particles can enter in box, have significant effect!**



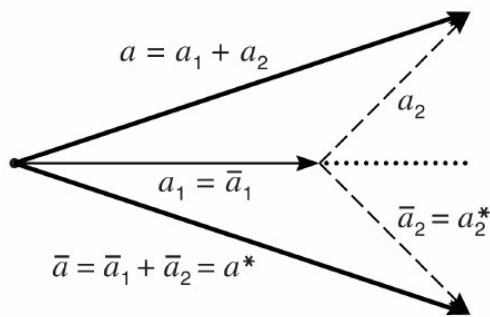
# CP Violation in Decay

CP violated in decay if  $A(\bar{P}^0 \rightarrow \bar{f}) \neq A(P^0 \rightarrow f)$

- requires interference of (at least) two decay amplitudes with different weak phase and different strong phase leading to the same final state

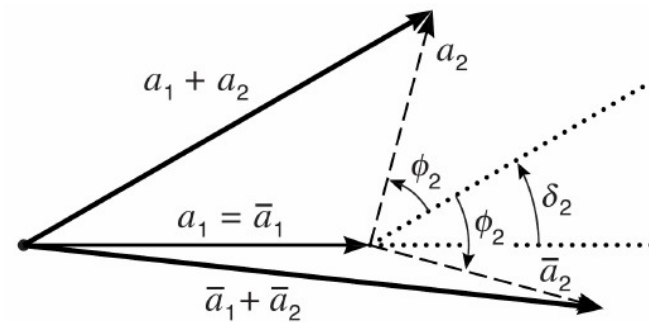
$$\left. \begin{aligned} \mathbf{A}_f &\equiv \mathbf{A}(P^0 \rightarrow f) = \sum_i \mathbf{a}_i e^{i(\delta_i + \phi_i)} \\ \bar{\mathbf{A}}_{\bar{f}} &\equiv \mathbf{A}(\bar{P}^0 \rightarrow \bar{f}) = \sum_i \mathbf{a}_i e^{i(\delta_i - \phi_i)} \end{aligned} \right\} \begin{array}{l} \phi_i: \text{weak phase, changes sign under CP} \\ \delta_i: \text{strong phase, does not change sign under CP} \end{array}$$

$$|\mathbf{A}_f|^2 - |\bar{\mathbf{A}}_{\bar{f}}|^2 = -2 \sum_{ij} \mathbf{a}_i \mathbf{a}_j \cdot \sin(\phi_i - \phi_j) \cdot \sin(\delta_i - \delta_j)$$



$$\begin{array}{l} \phi_2 \neq \phi_1 \\ \delta_2 = \delta_1 \\ \Rightarrow |\bar{\mathbf{a}}| = |\mathbf{a}| \end{array}$$

$(\varphi_1 = \delta_1 = 0)$



$$\begin{array}{l} \phi_2 \neq \phi_1 \\ \delta_2 \neq \delta_1 \\ \Rightarrow |\bar{\mathbf{a}}| \neq |\mathbf{a}| \end{array}$$

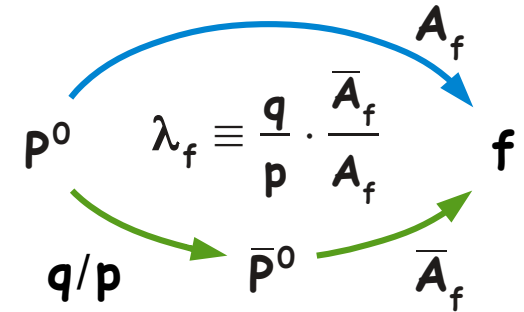
$(\varphi_1 = \delta_1 = 0)$

- interference and CP violation can be large
  - New Physics can enter through loops if Penguin diagrams involved
- but have to battle large theoretical uncertainties due to the strong phase

For decays into a CP eigenstate  $f$  that is accessible to both  $P^0$  and  $\bar{P}^0$

- CP violated due to interference between direct decay and decay after mixing if

$$\text{Im} \left( \frac{q}{p} \cdot \frac{\bar{A}_f}{A_f} \right) \neq 0$$



- measure time-dependent decay rate asymmetry:

$$a_f(t) = \frac{N(P^0_{(t=0)} \rightarrow f, t) - N(\bar{P}^0_{(t=0)} \rightarrow f, t)}{N(P^0_{(t=0)} \rightarrow f, t) + N(\bar{P}^0_{(t=0)} \rightarrow f, t)} \approx \frac{-C_f \cos(\Delta m \cdot t) + S_f \sin(\Delta m \cdot t)}{\cosh(\Delta \Gamma \cdot t/2) + \Omega_f \sinh(\Delta \Gamma \cdot t/2)}$$

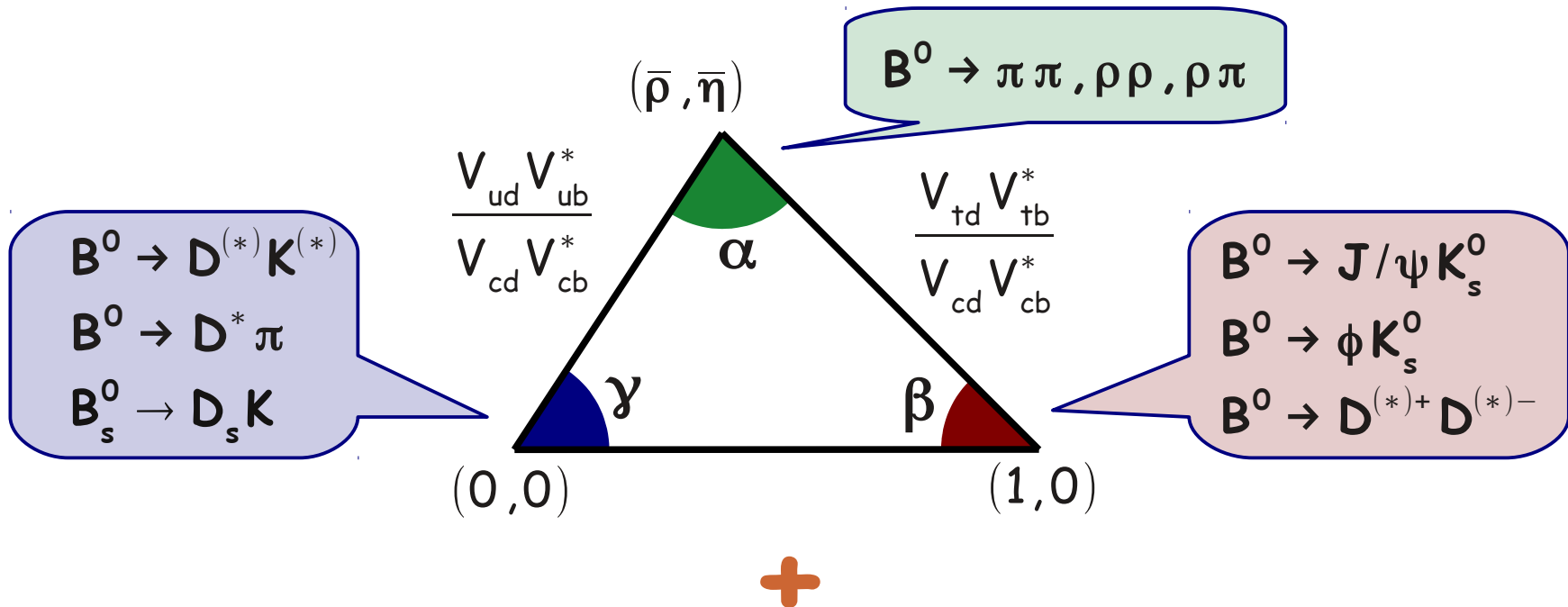
$$C_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} ; S_f = \frac{2 \cdot \Im(\lambda_f)}{1 + |\lambda_f|^2} ; \Omega_f = 1 - S_f^2 - C_f^2$$

- the ideal case: asymmetries can be large and no strong phase involved
- prominent example: measurement of CKM angle  $\sin 2\beta$  in  $B^0 \rightarrow J/\psi K^0_s$ 
  - one dominating decay amplitude, negligible CP violation in mixing,  $\Delta \Gamma \ll 1$

$$\Rightarrow a_f(t) = \Im(\lambda_f) \cdot \sin(\Delta m \cdot t) = \sin 2\beta \cdot \sin(\Delta m \cdot t)$$

## CP-violating observables depend on phases of CKM elements

- can be used to measure angles of Unitarity Triangle
- $\beta$  easiest, "golden channel"  $B^0 \rightarrow J/\psi K_s^0$ : measured to  $\pm 0.5^\circ$  at B factories
- $\gamma$  experimentally most challenging: currently measured to about  $\pm 15^\circ$

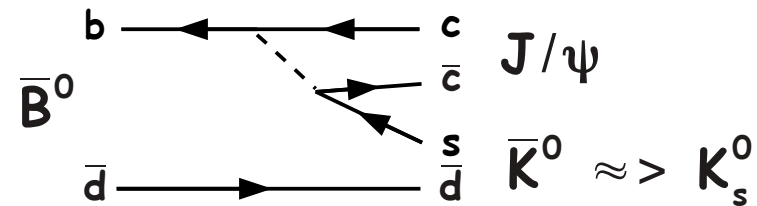
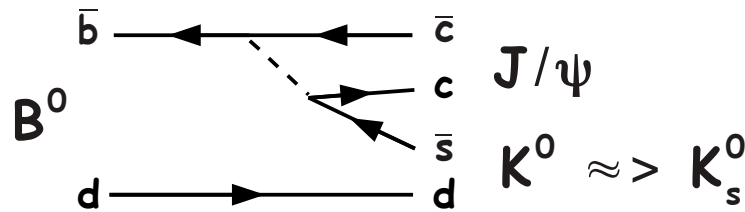


$B_s^0 \rightarrow J/\psi \phi \rightarrow$  "golden channel" to measure CP mixing phase in  $B_s^0 \bar{B}_s^0$  system



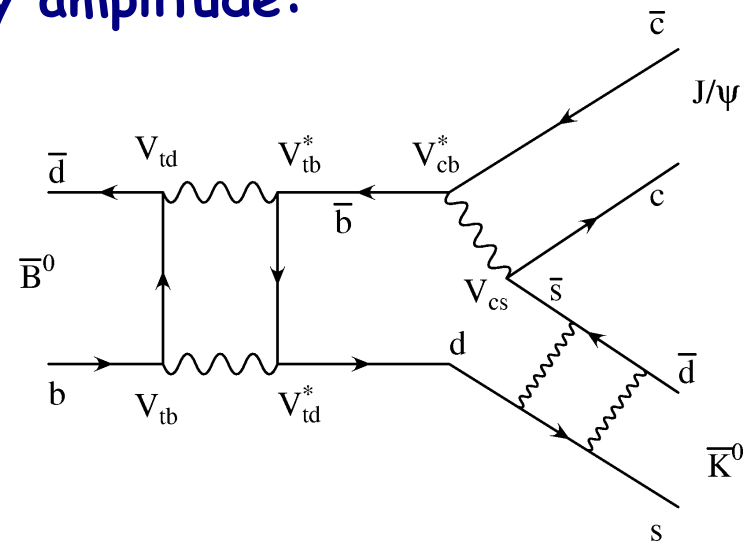
## CP violation due to interference between mixing and decay

- J/ψ K<sup>0</sup><sub>s</sub> is a CP-odd eigenstate, accessible to both B<sup>0</sup> and B<sup>0</sup><sub>̄</sub>



- CKM phase for the dominating tree decay amplitude:

$$\begin{aligned}
 \lambda_{J/\psi K_s} &= \begin{pmatrix} \mathbf{q} \\ \mathbf{p} \end{pmatrix}_{B^0} \cdot \begin{pmatrix} \bar{\mathbf{A}}_{J/\psi K^0} \\ \mathbf{A}_{J/\psi K^0} \end{pmatrix} \cdot \begin{pmatrix} \mathbf{q} \\ \mathbf{p} \end{pmatrix}_{K^0} \\
 &= \begin{pmatrix} V_{tb}^* V_{td} \\ V_{tb} V_{td}^* \end{pmatrix} \cdot \begin{pmatrix} V_{cs}^* V_{cb} \\ V_{cs} V_{cb}^* \end{pmatrix} \cdot \begin{pmatrix} V_{cd}^* V_{cs} \\ V_{cd} V_{cs}^* \end{pmatrix} \\
 &= \begin{pmatrix} V_{tb}^* V_{td} \\ V_{cb}^* V_{cd} \end{pmatrix} / \begin{pmatrix} V_{tb} V_{td}^* \\ V_{cb} V_{cd}^* \end{pmatrix} \\
 &= 2 \cdot \arg \left( \frac{V_{tb}^* V_{td}}{V_{cb}^* V_{cd}} \right) = 2 \cdot \beta \quad \Rightarrow
 \end{aligned}$$



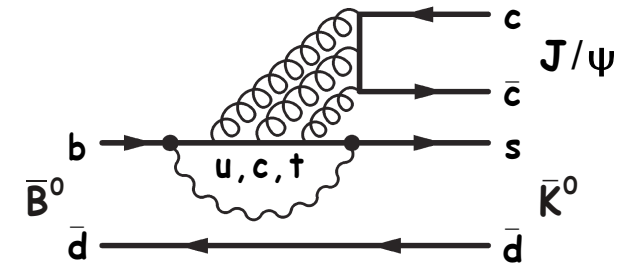
$$a_{B^0 \rightarrow J/\psi K_s^0}(t) = \sin 2\beta \cdot \sin(\Delta m_d \cdot t)$$

Theory "clean": leading Penguin (P) has same weak phase as Tree (T)

$$A_{J/\psi K^0} = (T + P_c) \cdot (V_{cb}^* V_{cs}) + P_t \cdot (V_{tb}^* V_{ts}) + P_u \cdot (V_{ub}^* V_{us})$$

- unitarity of CKM matrix:  $V_{tb}^* V_{ts} = -V_{cb}^* V_{cs} - V_{ub}^* V_{us}$

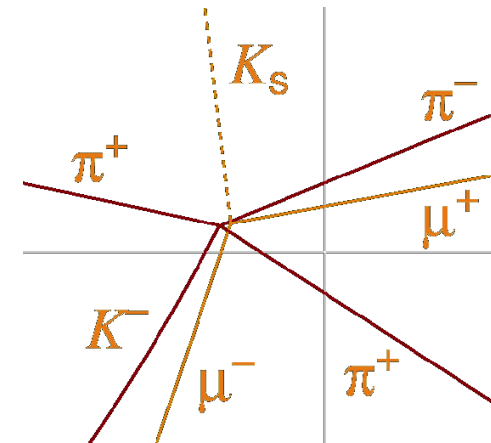
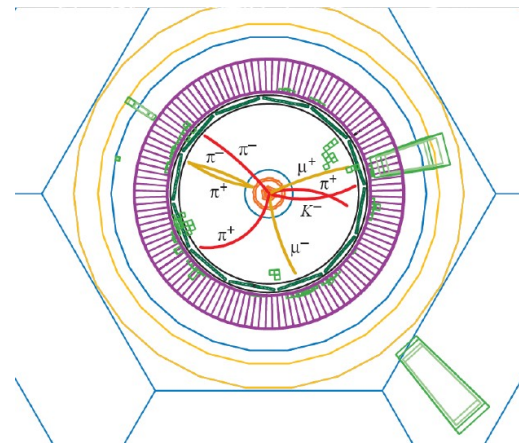
$$A_{J/\psi K^0} = \underbrace{(T + P_c - P_t)}_{\approx 0.1 \cdot T} \cdot \underbrace{(V_{cb}^* V_{cs})}_{\propto \lambda^2} + \underbrace{(P_u - P_t)}_{\approx 0.1 \cdot T} \cdot \underbrace{(V_{ub}^* V_{us})}_{\propto \lambda^4}$$



- contamination from  $V_{ub}^* V_{us}$  smaller than 1%

Also attractive from point of view of experiment

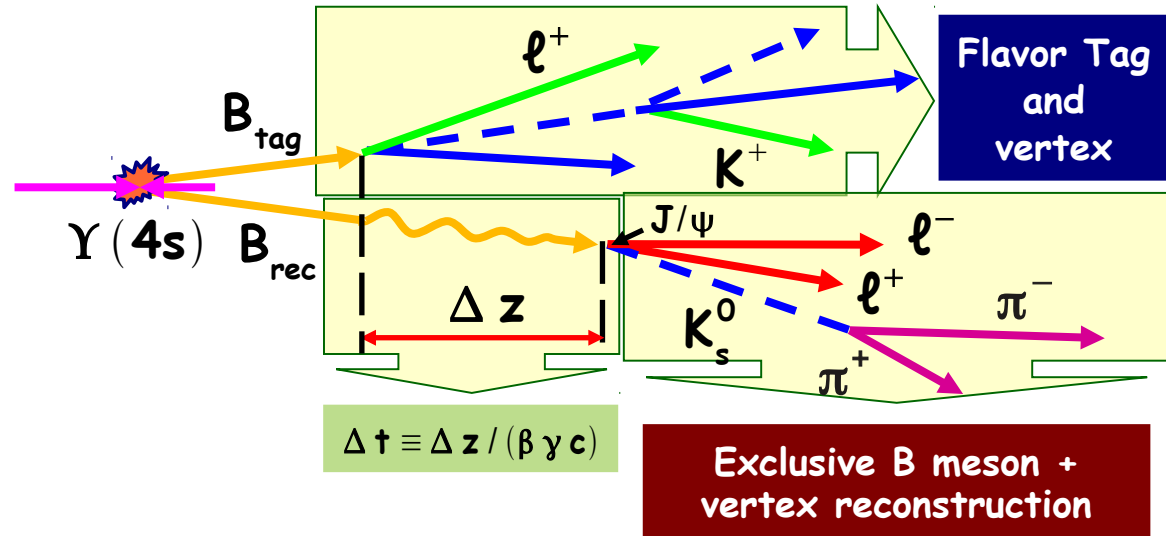
- clear event signature
  - lepton pair from  $J/\psi$  decay
  - 2<sup>nd</sup> displaced vertex from  $K^0_s$  decay
  - $J/\psi$  and  $K^0_s$  invariant masses
- reasonably large branching ratio



$$BF(B^0 \rightarrow J/\psi K^0_s) \times BF(J/\psi \rightarrow \ell^+ \ell^-) \times BF(K^0_s \rightarrow \pi^+ \pi^-) \approx 7 \times 10^{-5}$$

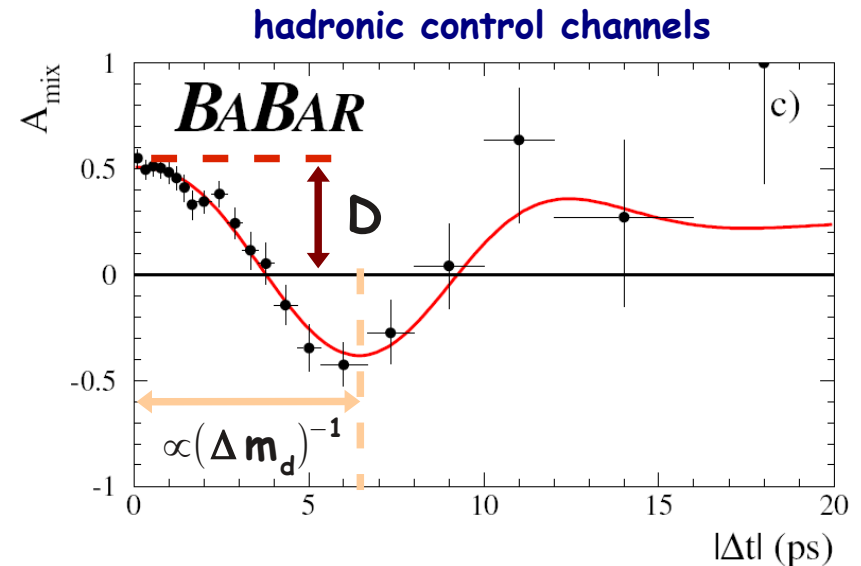
## Similar approach as for mixing measurements

- fully reconstruct signal B in final state  $J/\psi K_s$
- reconstruct the two B decay vertices, determine  $\Delta z$  and  $\Delta t$
- infer flavour at "t=0" from decay products of tagging B



## Extract sin 2β from oscillation AMPLITUDE

- measured asymmetry reduced by
  - tagging dilution  $D = 1 - 2 \cdot \omega$
  - finite decay-time resolution
- determine these effects from data using flavour-specific decay modes
  - e.g.  $B^0 \rightarrow D^{(*)+} \pi^-$  and  $B^0 \rightarrow J/\psi K^* (K^+ \pi^-)$

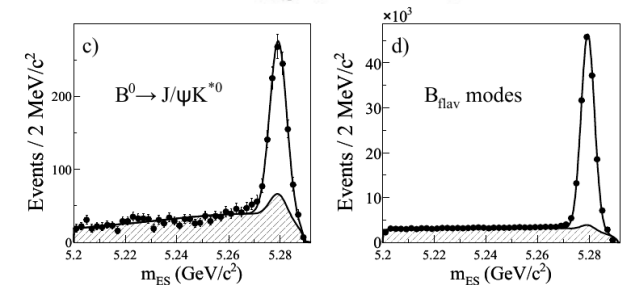
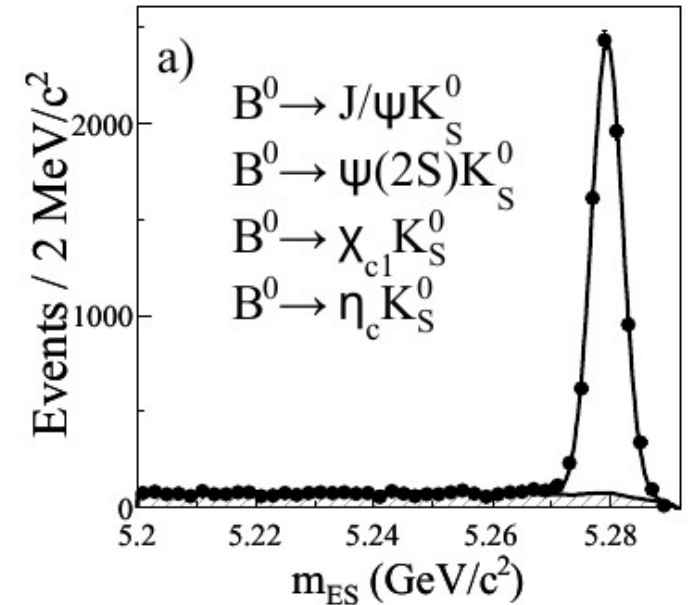


## Fit $m_{ES}$ distributions to determine composition of the event sample

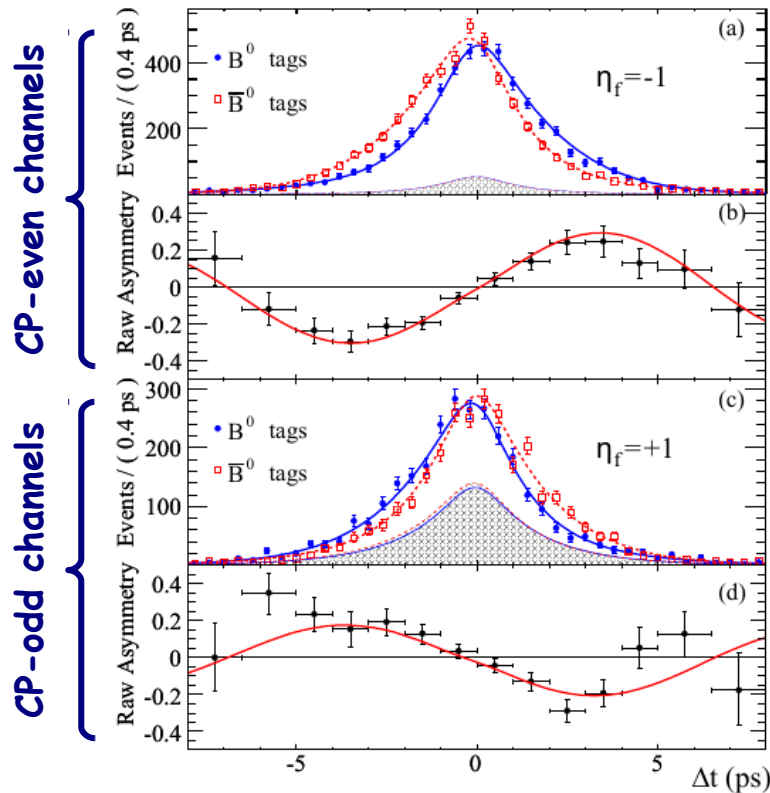
- $J/\psi K_S^0$  and other  $b \rightarrow c\bar{c}s$  signal channels
- other  $c\bar{c}$  resonances:  $\psi(2s)$ ,  $\chi_{c1}$ ,  $\eta_c$
- CP odd final state:  $J/\psi K_L^0$
- $B^0 \rightarrow D^{(*)+} \pi^-$ ,  $B^0 \rightarrow J/\psi K^*$  control channels

## Fit $\Delta t$ distributions to extract sin 2β

- simultaneous fit to signal and control channels
- e.g. Babar fit has 71 free parameters:
  - $S_f$  (= sin 2β) and  $C_f$
  - 7 to parametrize  $\Delta t$  resolution in signal channels
  - 12 for average mis-tag fractions  $\omega$  and possible differences  $\Delta\omega$  between  $B^0$  and  $\bar{B}^0$
  - 7 for possible difference in reconstruction and tagging efficiencies for  $B^0$  and  $\bar{B}^0$
  - 43 to describe mis-tag fraction,  $\Delta t$  resolution, possible CP violation in backgrounds



## Time-dependent CP asymmetry

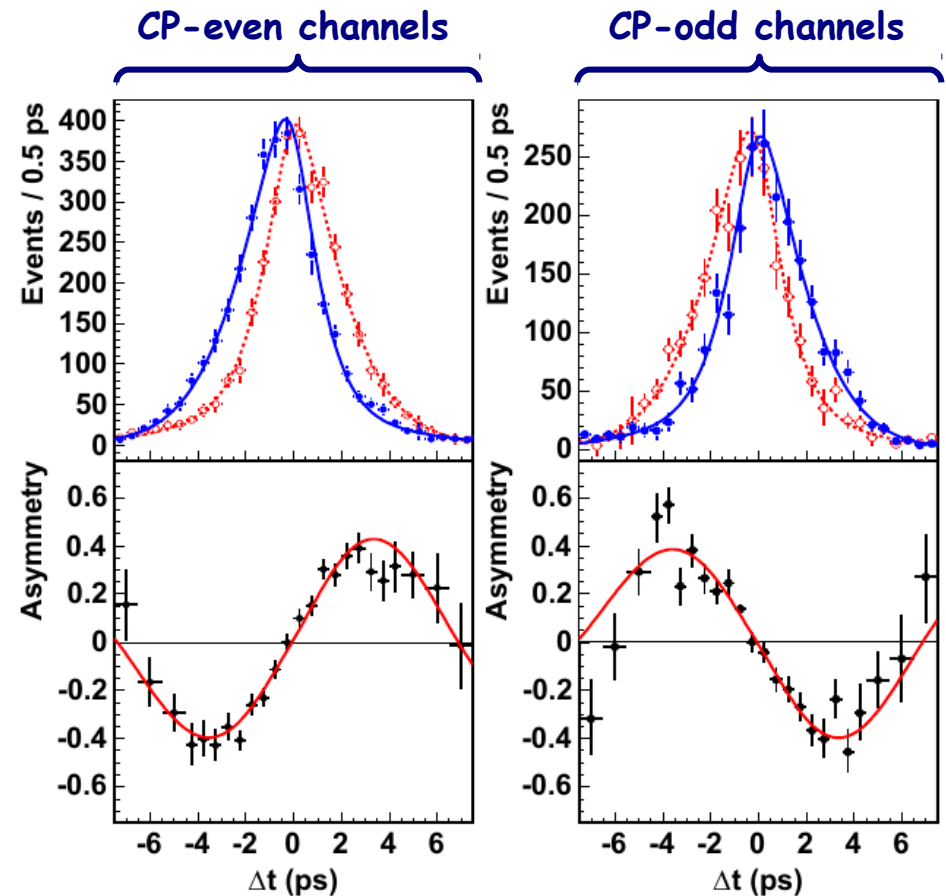


**Babar**

$$\sin 2\beta = 0.687 \pm 0.028 \pm 0.012$$

[PRD 79 (2009) 072009]

$$C_f = 0.024 \pm 0.020 \pm 0.016$$



**Belle**

$$\sin 2\phi_1 = 0.667 \pm 0.023 \pm 0.012$$

[PRL 108 (2012) 171802]

$$C_f = 0.006 \pm 0.019 \pm 0.012$$

- **Part I: Introduction**

- what is (quark) flavour physics and why is it so exciting?
- how we got here: brief history of flavour physics in the 20<sup>th</sup> century

- **Part II: Particle-Antiparticle Mixing**

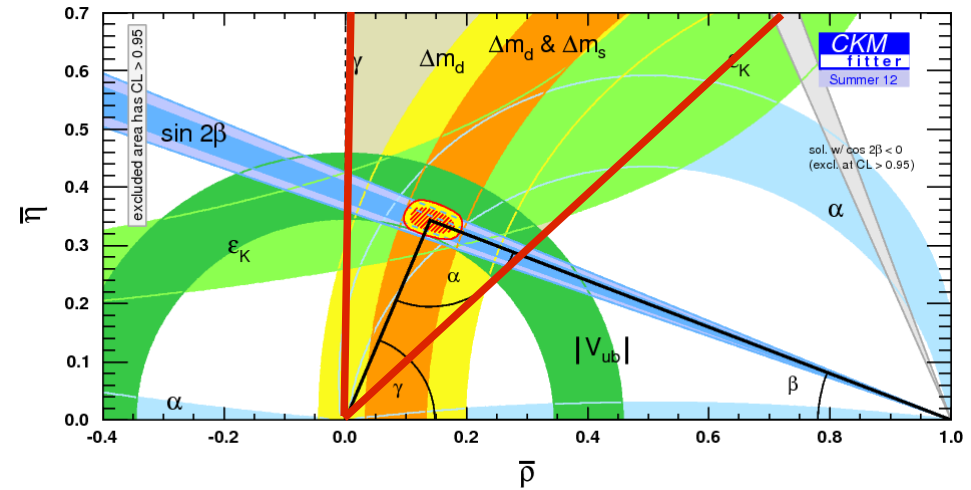
- a short summary of the formalism (don't worry, I'm an experimentalist ... )
- introduce experimental facilities and techniques

- **Part III: Precision tests of the Standard Model**

- **CP violating observables:**  $\sin 2\beta$ , **CKM angle  $\gamma$** ,  $B_s^0 \bar{B}_s^0$  mixing phase  $\phi_s$
- rare decays: search for  $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ , angular observables in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

# CKM angle $\gamma$ from Tree Decays

- CKM fits so far in good agreement with Standard Model
- need more precise measurements to test for subtle effects from possible New Physics



- the CKM parameter that is least well constrained by direct measurements:

$$\gamma = \arg \left( -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right)$$

$$\gamma = (66 \pm 12)^\circ \quad [\text{CKMfitter}]$$

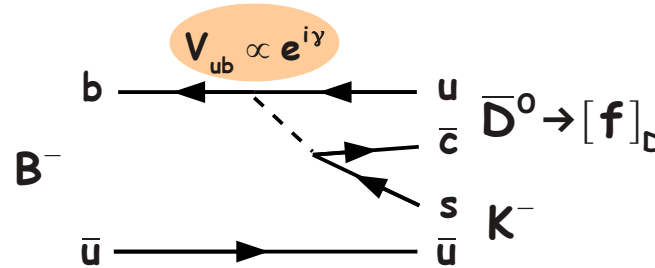
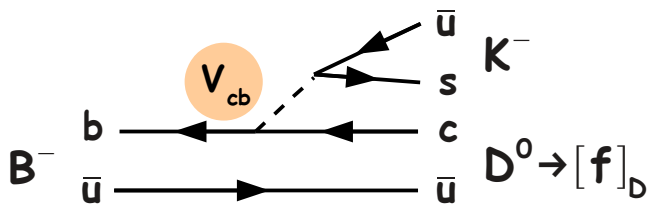
$$\gamma = (72 \pm 9)^\circ \quad [\text{UTfit}]$$

- tree-level B decays can provide a theoretically “clean” measurement of  $\gamma$ 
  - no loops → largely unaffected by possible effects from New Physics
- but experimentally very challenging
  - decays to purely hadronic final states (→ trigger, K/π separation)
  - branching fractions are small (→ need large number of B's)

# $\gamma$ from Trees: $B^\pm \rightarrow D K^\pm$

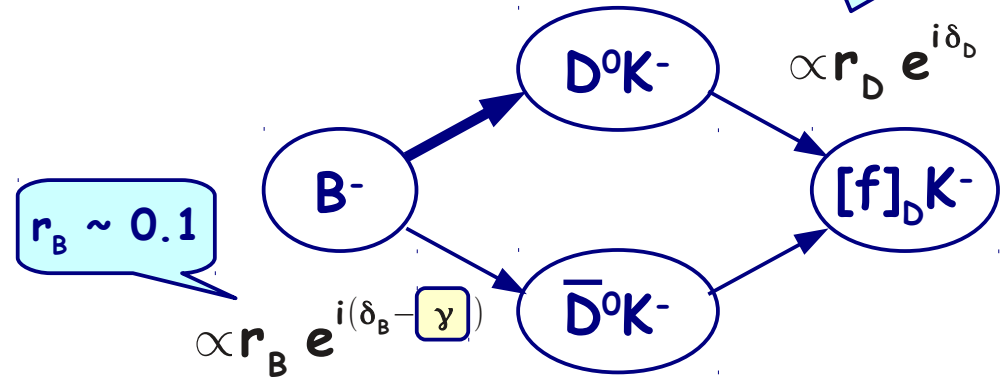
$B^\pm \rightarrow D K^\pm$  tree decays to final states  $[f]_D$  accessible to  $D^0$  and  $\bar{D}^0$

- interference of  $b \rightarrow c$  and  $b \rightarrow u$  ( $V_{ub} \propto e^{i\gamma}$ ) tree diagrams:



$r_D \sim 1$  for GLW,  
 $\sim 0.05$  for ADS

- theory uncertainties due to
  - strong phase difference  $\delta_B$
  - ratio  $r_B$  of the magnitudes of the two interfering amplitudes



- different methods proposed that in principle allow clean extraction of  $\gamma$ 
  - named after initials of their proponents: "GLW", "ADS", "GGSZ"
  - combined analysis to extract  $\gamma$  and hadronic parameters  $r_B, \delta_B, r_D, \delta_D$

(formalisms also hold for  $B^\pm \rightarrow D^* K^\pm$  and  $B^\pm \rightarrow D K^{*\pm}$ )



## "GLW": Gronau, London, Wyler

[PLB 253 (1991) 483]

[PLB 265 (1991) 172]

- D decays to CP eigenstates  $D^0 \rightarrow K^+K^-$ ,  $D^0 \rightarrow \pi^+\pi^-$
- disadvantage: small value of  $r_B \rightarrow$  small interference

## "ADS": Atwood, Dunietz, Soni

[PRL 78 (1997) 3257]

[PRD 63 (2001) 036005]

- Cabibbo favoured  $D^0 \rightarrow K^+\pi^-$  / doubly Cabibbo suppressed  $D^0 \rightarrow K^-\pi^+$
- advantage: small  $r_D$  compensates small  $r_B \rightarrow$  larger interference
- disadvantage: very small branching fraction for suppressed decay ( $\sim 10^{-7}$ )

## "GGSZ": Giri, Grossman, Soffer, Zupan

[PRD 68 (2003) 054018]

[PRD 70 (2004) 072003]

- exploit interference patterns in  $D^0 \rightarrow K_S^0 h^+ h^-$  Dalitz plot ( $h = \pi, K$ )
- powerful method, dominates precision on  $\gamma$  from B factories
- complication: rich resonance structure,  $\delta_D$  varies across Dalitz plot

## Measure decay rates to CP eigenstates and flavour-specific states

- CP eigenstates  $D_{CP+}^0 \rightarrow \pi^+ \pi^-, K^+ K^-$ ,  $D_{CP-}^0 \rightarrow K_S^0 \pi^0, K_S^0 \omega, K_S^0 \phi$
- flavour-specific final states:  $D^0 \rightarrow K^+ \pi^-, \bar{D}^0 \rightarrow K^- \pi^+$
- $|D_{CP+}^0\rangle = \frac{1}{\sqrt{2}} (|D^0\rangle + |\bar{D}^0\rangle) \rightarrow$  two triangles in complex plane

$$\sqrt{2} \cdot A(B^+ \rightarrow D_{CP+}^0 K^+) = A(B^+ \rightarrow D^0 K^+) + A(B^+ \rightarrow \bar{D}^0 K^+)$$

$$\sqrt{2} \cdot A(B^- \rightarrow D_{CP+}^0 K^-) = A(B^- \rightarrow \bar{D}^0 K^-) + A(B^- \rightarrow D^0 K^-)$$

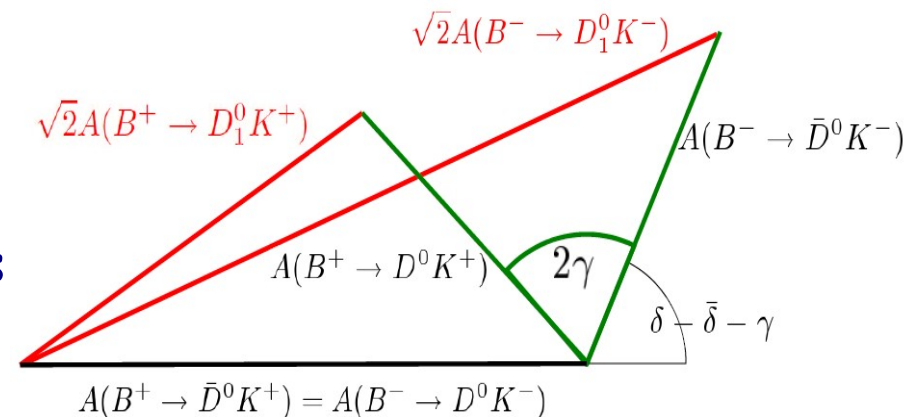
similar  
for  $|D_{CP-}^0\rangle$

- one common side ( $b \rightarrow c$  real)

$$A(B^+ \rightarrow \bar{D}^0 K^+) = A(B^- \rightarrow D^0 K^-)$$

- extract  $\gamma$  from angle between  $b \rightarrow u$  sides

$$A(B^+ \rightarrow D^0 K^+) = e^{2i\gamma} \cdot A(B^- \rightarrow \bar{D}^0 K^-)$$



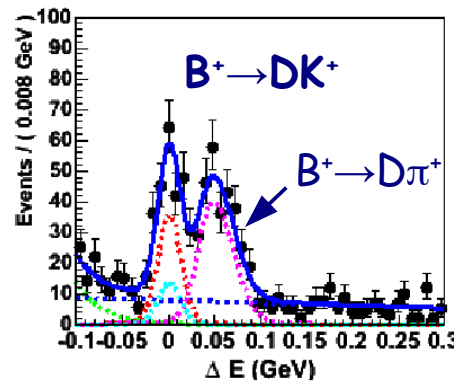
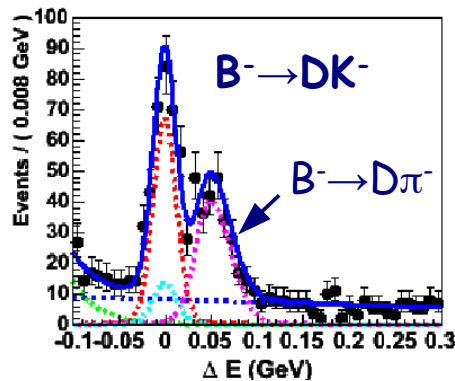
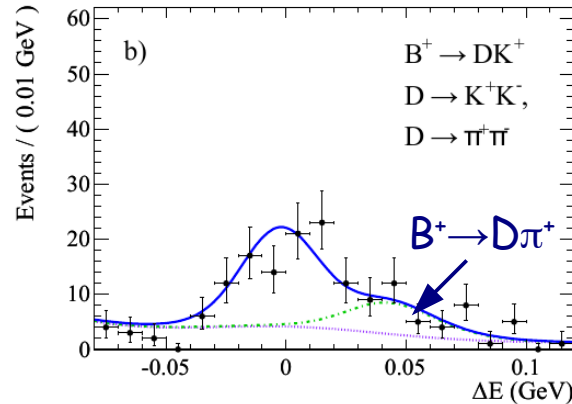
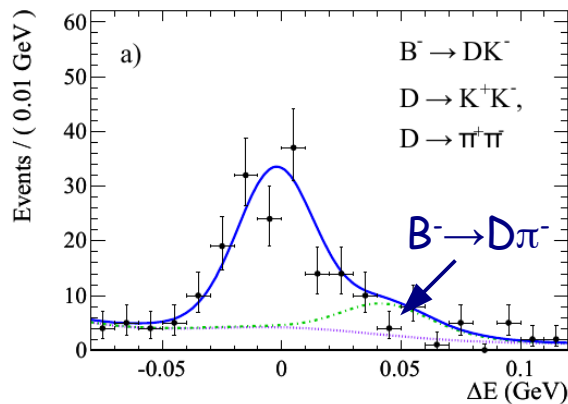
- $r_B$  small  $\rightarrow$  triangles very squashed  $\rightarrow$  sensitivity to  $\gamma$  limited

# GLW modes at B Factories

Decay rate ratios and asymmetries ( $\rightarrow$  cancellation of systematics)

$$R_{CP+} = \frac{\Gamma(B^- \rightarrow [h^+ h^-]_D K^-) + \Gamma(B^+ \rightarrow [h^+ h^-]_D K^+)}{1/2 \cdot [\Gamma(B^- \rightarrow [K^+ \pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^- \pi^+]_D K^+)]} = 1 + r_B^2 + 2 \cdot r_B \cdot \cos \delta_B \cdot \cos \gamma$$

$$A_{CP+} = \frac{\Gamma(B^- \rightarrow [h^+ h^-]_D K^-) - \Gamma(B^+ \rightarrow [h^+ h^-]_D K^+)}{\Gamma(B^- \rightarrow [h^+ h^-]_D K^-) + \Gamma(B^+ \rightarrow [h^+ h^-]_D K^+)} = + \frac{2 \cdot r_B \cdot \cos \delta_B \cdot \cos \gamma}{R_{CP+}}$$



Babar

$467 \times 10^6 \Upsilon(4s) \rightarrow B\bar{B}$  decays

$$A_{CP+} = (25 \pm 6 \pm 2) \%$$

[PRD 82 (2010) 072004]

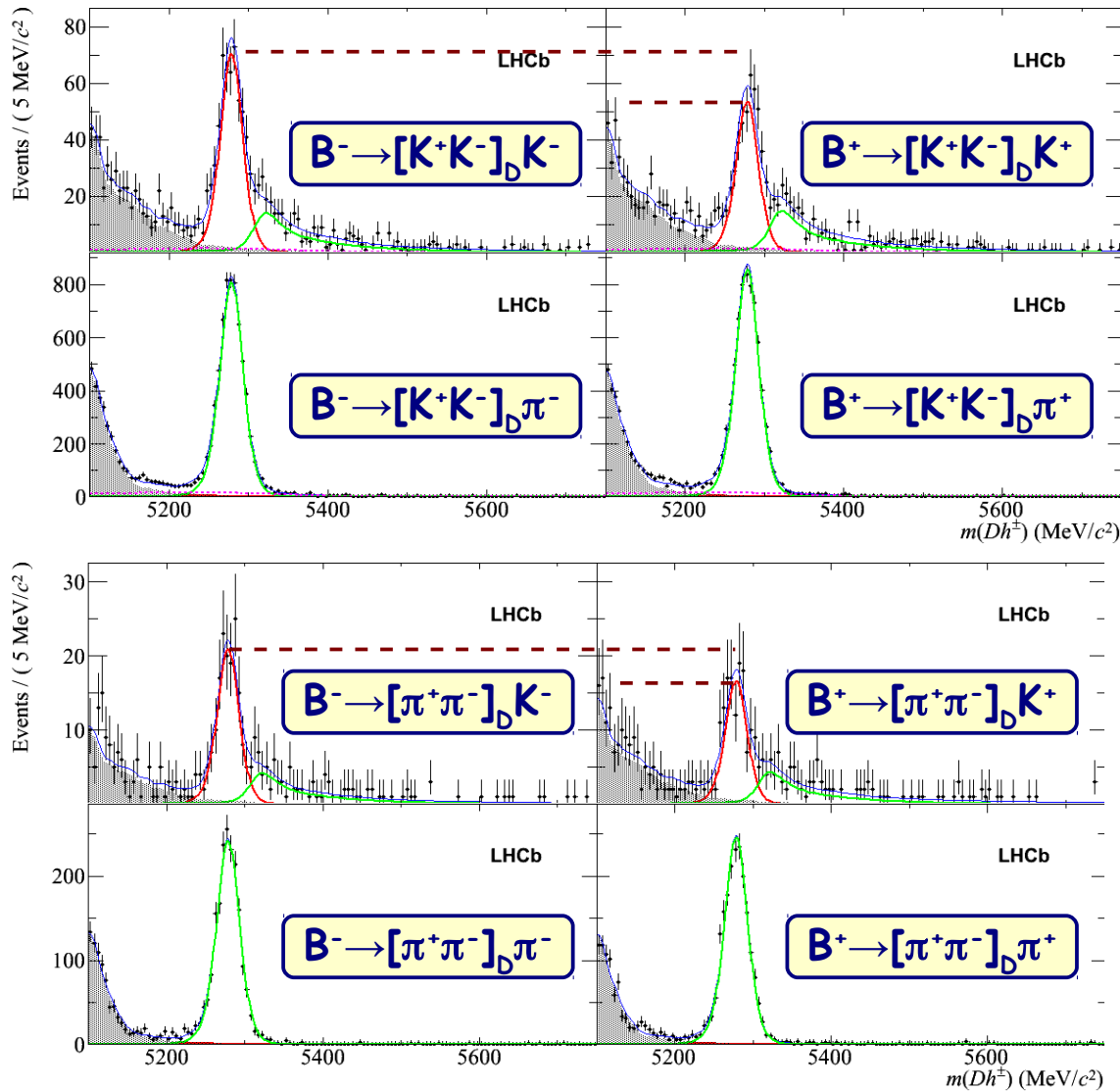
Belle

$772 \times 10^6 \Upsilon(4s) \rightarrow B\bar{B}$  decays

$$A_{CP+} = (29 \pm 6 \pm 2) \%$$

[arXiv:1112.1984]

## Analysis of $1.0 \text{ fb}^{-1}$ (2011 data set)



$$A_{CP^+} = (14.5 \pm 3.2 \pm 1.0) \%$$

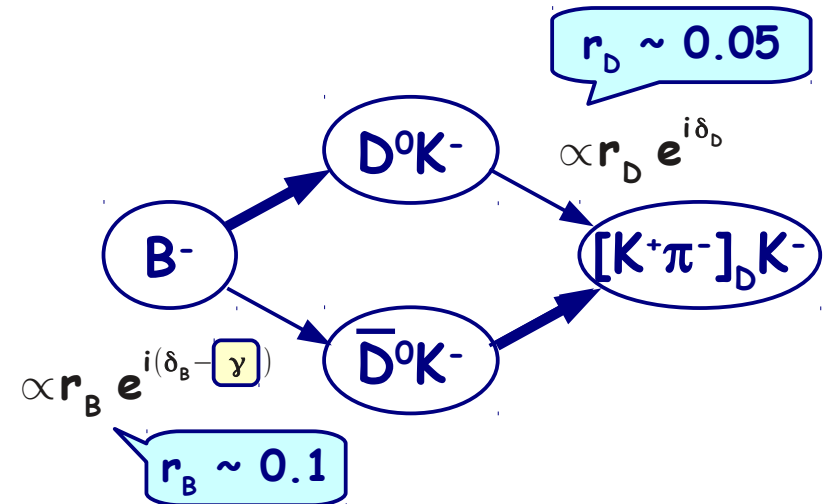
[PLB 713 (2012) 351]

- note suppression of  $B^\pm \rightarrow D \pi^\pm$  contamination in the  $B^\pm \rightarrow D K^\pm$  samples !

# $\gamma$ from Trees: ADS modes

## $\bar{D}^0$ decay Cabibbo-allowed / $D^0$ decay doubly Cabibbo-suppressed

- interfering amplitudes of similar magnitude, larger CP violation
- price to pay: very low branching fraction for the doubly Cabibbo-suppressed mode



$$r_D = \frac{|A(D^0 \rightarrow K^+ \pi^-)|}{|A(\bar{D}^0 \rightarrow K^+ \pi^-)|} \approx \frac{|V_{cd}^* V_{us}|}{|V_{ud}^* V_{cs}|} = \lambda^2 \approx 0.05$$

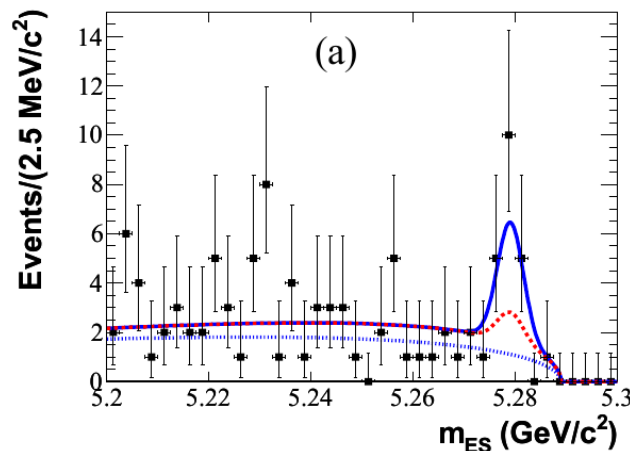
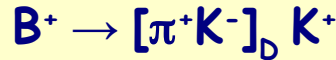
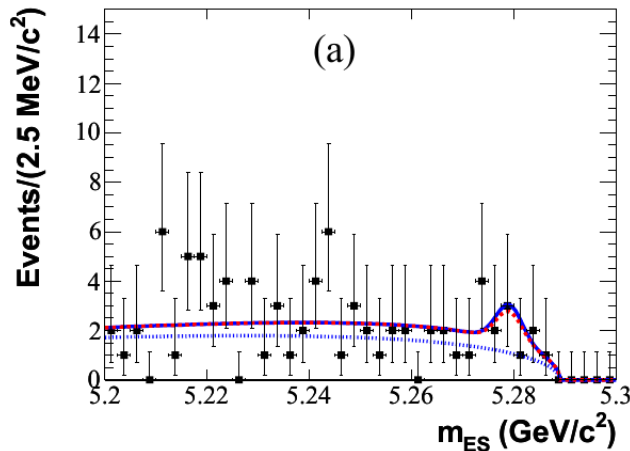
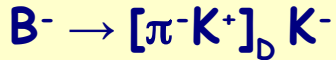
- again, measure ratios and asymmetries to cancel systematics

$$R_{\text{ADS}} = \frac{\Gamma(B^- \rightarrow [K^+ \pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^- \pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^- \pi^+]_D K^-) + \Gamma(B^+ \rightarrow [K^+ \pi^-]_D K^+)} = r_B^2 + r_D^2 + 2 \cdot r_B r_D \cdot \cos(\delta_B + \delta_D) \cdot \cos \gamma$$

$$A_{\text{ADS}} = \frac{\Gamma(B^- \rightarrow [K^+ \pi^-]_D K^-) - \Gamma(B^+ \rightarrow [K^- \pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^+ \pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^- \pi^+]_D K^+)} = \frac{2 \cdot r_B r_D \cdot \sin(\delta_B + \delta_D) \cdot \sin \gamma}{R_{\text{ADS}}}$$

# ADS modes at B Factories

## Limited statistics in the doubly Cabibbo suppressed decay mode

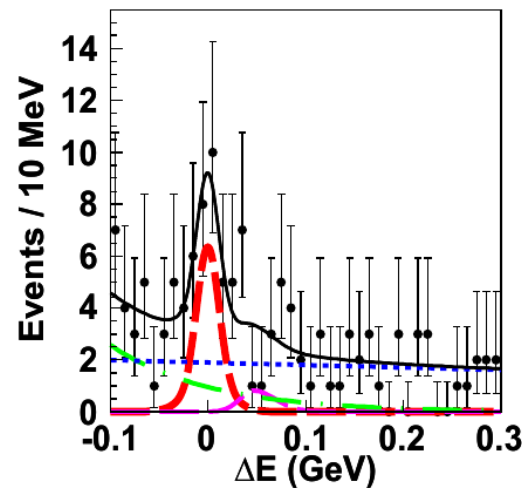
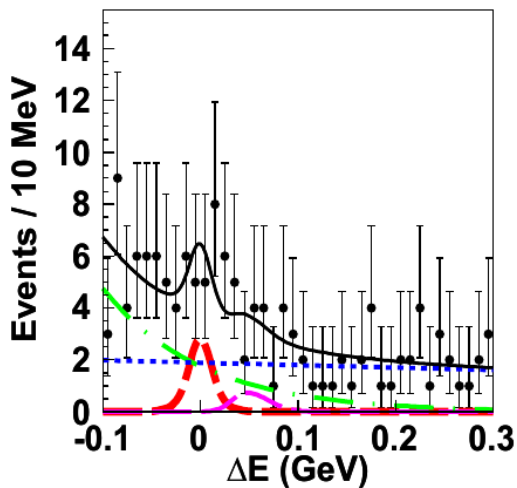


Babar

$467 \times 10^6 \Upsilon(4s) \rightarrow B\bar{B}$  decays

$$A_{\text{ADS}}(\text{DK}) = (-86 \pm 47^{+12}_{-16}) \%$$

[arXiv:1006.4241]



Belle

$772 \times 10^6 \Upsilon(4s) \rightarrow B\bar{B}$  decays

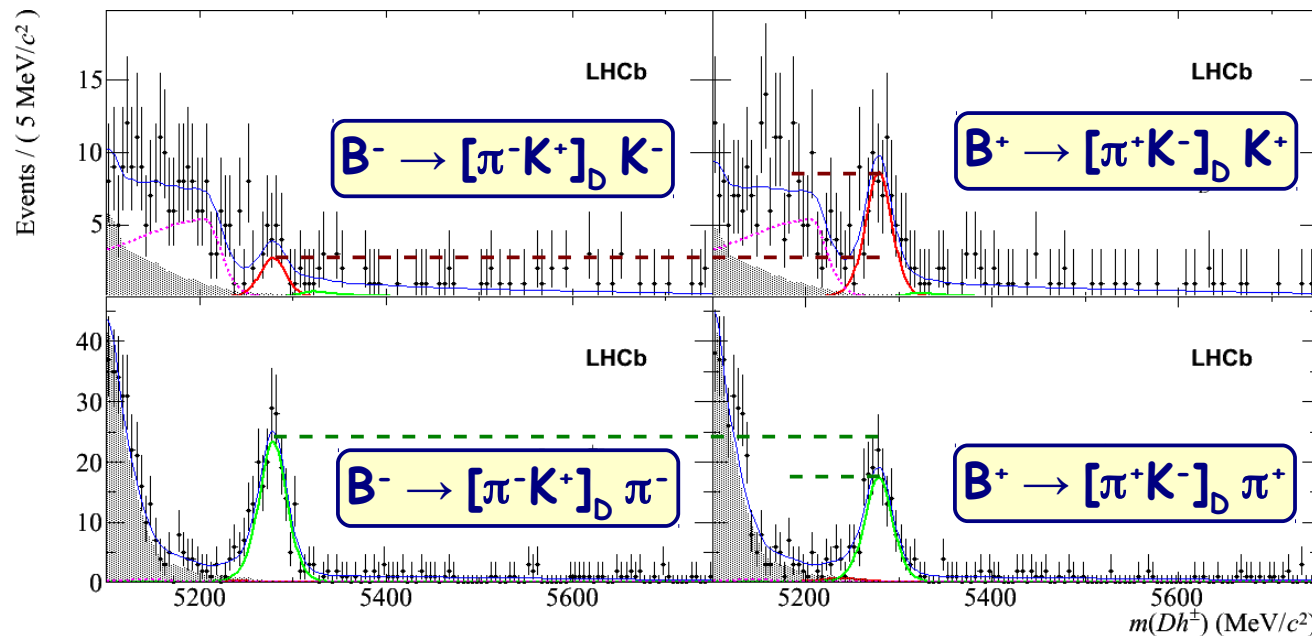
$$A_{\text{ADS}}(\text{DK}) = (-39^{+26 +4}_{-28 -3}) \%$$

[PRL 106 (2011) 231803]

# ADS modes at LHCb

## Analysis of $1 \text{ fb}^{-1}$ (2011 data set)

- first observation of the doubly Cabibbo suppressed mode ( $10 \sigma$  significance)
- evidence for asymmetry in  $B^\pm \rightarrow DK^\pm$  ( $4 \sigma$  significance)



$$A_{\text{ADS}}(\text{DK}) = (-52 \pm 15 \pm 2) \%$$

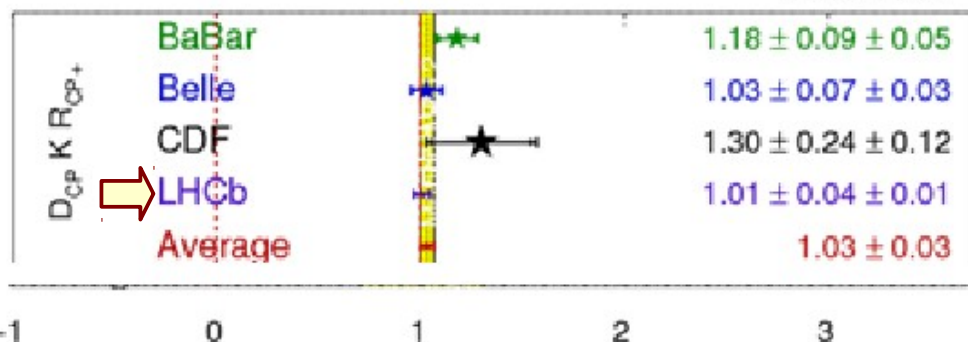
PLB 712 (2012) 203]

- hint of a positive asymmetry in  $B^\pm \rightarrow D \pi^\pm$  ( $2.4 \sigma$  significance)

# GLW / ADS: LHCb Impact

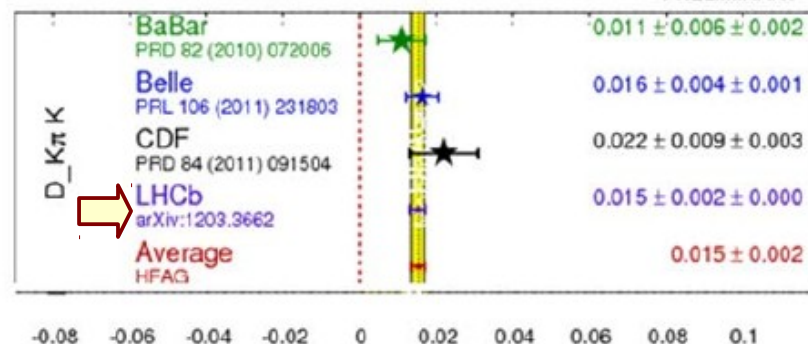
## $R_{CP}$ Averages

**HFAG**  
Moriond 2012  
PRELIMINARY



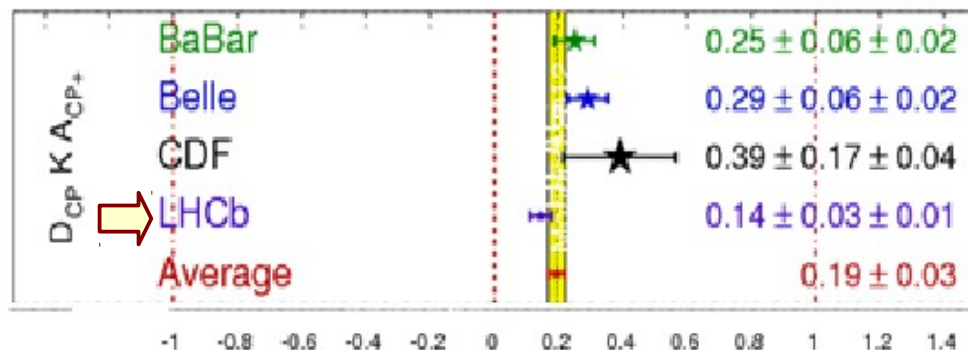
## $R_{ADS}$ Averages

**HFAG**  
Moriond 2012  
PRELIMINARY



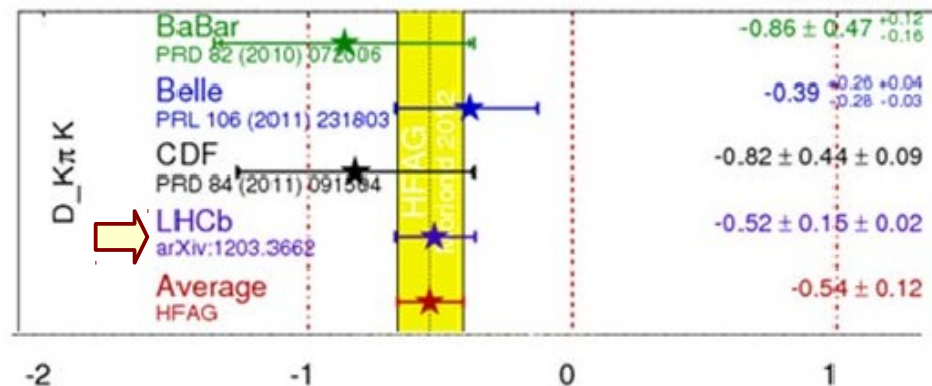
## $A_{CP}$ Averages

**HFAG**  
Moriond 2012  
PRELIMINARY



## $A_{ADS}$ Averages

**HFAG**  
Moriond 2012  
PRELIMINARY





# $\gamma$ from Trees: GGSZ

## Exploit interference patterns in $D \rightarrow K_s^0 h^+ h^-$ Dalitz plots ( $h = \pi, K$ )

- Dalitz plot:  $D \rightarrow K_s^0 h^+ h^-$  decay amplitude  $f_D$  as a function of

$$m_+^2 \equiv m^2(K_s^0 h^+) \quad ; \quad m_-^2 \equiv m^2(K_s^0 h^-)$$

- intermediate resonances  $\rightarrow$  structure above flat phase-space distribution
- assuming no CP violation in D decays (expected to be very small)

$$f_{\bar{D}^0}(m_+^2, m_-^2) = f_{D^0}(m_-^2, m_+^2)$$

- measure  $f_D(m_-^2, m_+^2)$  using large samples of flavour-tagged  $D \rightarrow K_s^0 h^+ h^-$  decays

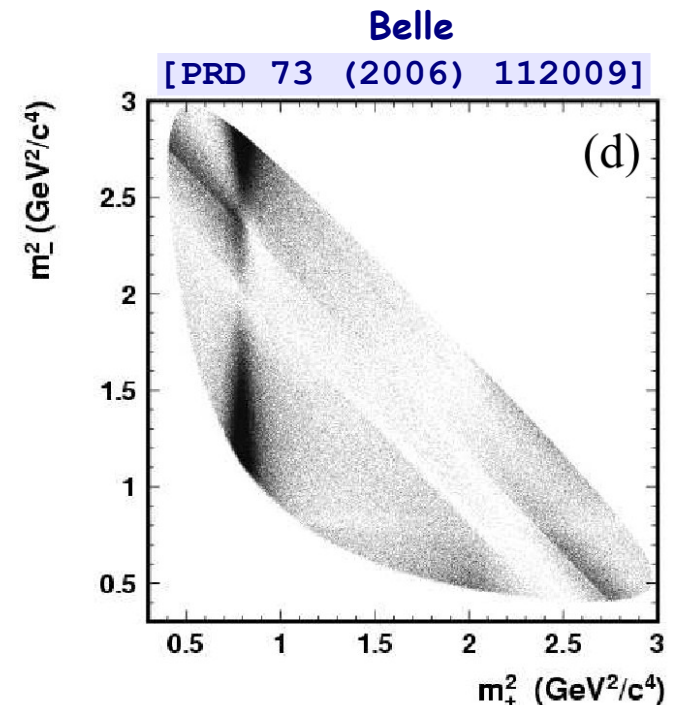
- B factories:  $D^{*\pm} \rightarrow D \pi^\pm$

- use pion charge to tag D flavour

- CLEO-c:  $e^+e^- \rightarrow \psi(3770) \rightarrow D^0 \bar{D}^0$

- use flavour-specific decay of accompanying D to tag D flavour

- observe rich resonance structure  $\rightarrow$  large interference possible

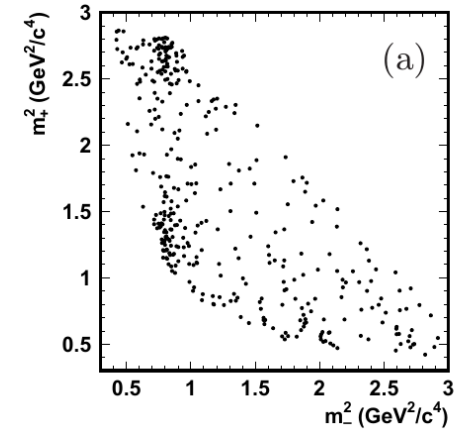


# $\gamma$ from Trees: GGSZ

Extract  $r_B, \delta_B, \gamma$  from difference in  $B^-$  and  $B^+$  interference patterns

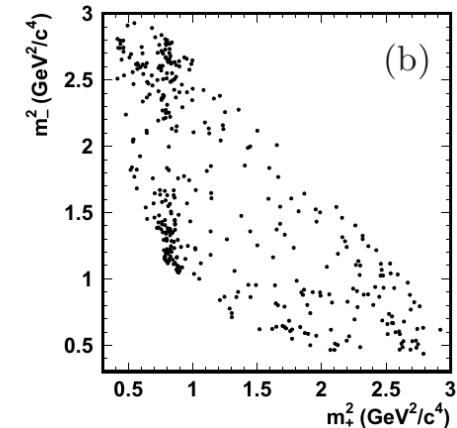
- $B^- \rightarrow [K_S^0 h^+ h^-]_D K^-$ :

$$\Gamma_{B^-}(m_+^2, m_-^2) \propto \left| \begin{array}{c} \text{Plot of } D^0 \text{ interference pattern} \\ + r_B \cdot e^{i(\delta_B - \gamma)} \cdot \text{Plot of } \bar{D}^0 \text{ interference pattern} \end{array} \right|^2$$



- $B^+ \rightarrow [K_S^0 h^+ h^-]_D K^+ \quad (f_{D^0} \leftrightarrow f_{\bar{D}^0}, -\gamma \leftrightarrow +\gamma)$

$$\Gamma_{B^+}(m_+^2, m_-^2) \propto \left| \begin{array}{c} \text{Plot of } \bar{D}^0 \text{ interference pattern} \\ + r_B \cdot e^{i(\delta_B + \gamma)} \cdot \text{Plot of } D^0 \text{ interference pattern} \end{array} \right|^2$$



- difference:**

$$\Delta \Gamma(m_-^2, m_+^2) \propto \left| f_D(m_-^2, m_+^2) \right|^2 + r_B^2 \cdot \left| f_D(m_+^2, m_-^2) \right|^2 + 2 r_B \cdot \text{Re} \left\{ f_D(m_-^2, m_+^2) \cdot f_D^*(m_+^2, m_-^2) \cdot e^{-i(\delta_B - \gamma)} \right\}$$

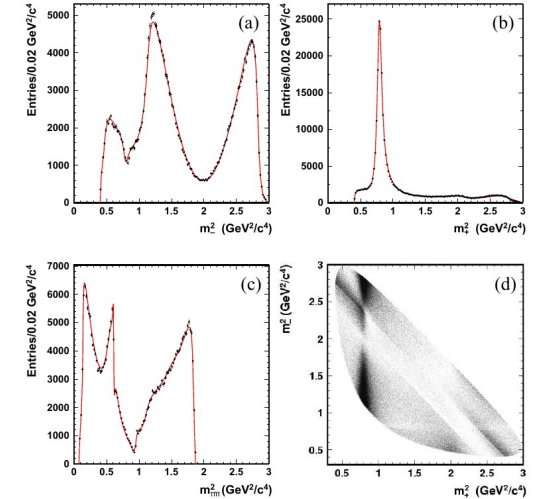
Belle, [PRD 81 (2010) 112002]

## Fit for $r_B, \delta_B, \gamma$ : model-dependent approach

- model  $f_D(m_+^2, m_-^2)$  by a coherent sum of two-body resonances and a non-resonant amplitude
- e.g. Belle: 18 + 1 amplitudes
- model uncertainty starts to limit precision on  $\gamma$

Intermediate state	Amplitude	Phase ( $^\circ$ )	Fit fraction
$K_S^0 \sigma_1$	$1.43 \pm 0.07$	$212 \pm 3$	9.8%
$K_S^0 \rho^0$	1.0 (fixed)	0 (fixed)	21.6%
$K_S^0 \omega$	$0.0314 \pm 0.0008$	$110.8 \pm 1.6$	0.4%
$K_S^0 f_0(980)$	$0.365 \pm 0.006$	$201.9 \pm 1.9$	4.9%
$K_S^0 \sigma_2$	$0.23 \pm 0.02$	$237 \pm 11$	0.6%
$K_S^0 f_2(1270)$	$1.32 \pm 0.04$	$348 \pm 2$	1.5%
$K_S^0 f_0(1370)$	$1.44 \pm 0.10$	$82 \pm 6$	1.1%
$K_S^0 \rho^0(1450)$	$0.66 \pm 0.07$	$9 \pm 8$	0.4%
$K^*(892)^+ \pi^-$	$1.644 \pm 0.010$	$132.1 \pm 0.5$	61.2%
$K^*(892)^- \pi^+$	$0.144 \pm 0.004$	$320.3 \pm 1.5$	0.55%
$K^*(1410)^+ \pi^-$	$0.61 \pm 0.06$	$113 \pm 4$	0.05%
$K^*(1410)^- \pi^+$	$0.45 \pm 0.04$	$254 \pm 5$	0.14%
$K_0^*(1430)^+ \pi^-$	$2.15 \pm 0.04$	$353.6 \pm 1.2$	7.4%
$K_0^*(1430)^- \pi^+$	$0.47 \pm 0.04$	$88 \pm 4$	0.43%
$K_2^*(1430)^+ \pi^-$	$0.88 \pm 0.03$	$318.7 \pm 1.9$	2.2%
$K_2^*(1430)^- \pi^+$	$0.25 \pm 0.02$	$265 \pm 6$	0.09%
$K^*(1680)^+ \pi^-$	$1.39 \pm 0.27$	$103 \pm 12$	0.36%
$K^*(1680)^- \pi^+$	$1.2 \pm 0.2$	$118 \pm 11$	0.11%
non-resonant	$3.0 \pm 0.3$	$164 \pm 5$	9.7%

Belle, [PRD 73 (2006) 112009]



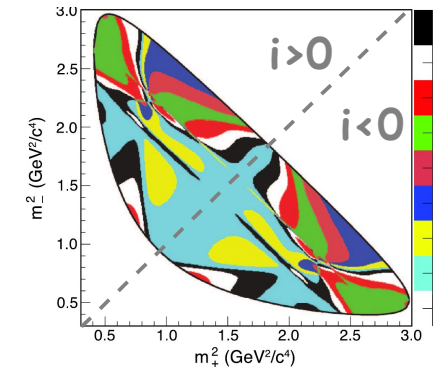
## Fit for $r_B, \delta_B, \gamma$ : model-independent approach

- use CLEO-c measurements of  $\delta_D$ , divide Dalitz plot in regions  $i$  of  $\sim$  constant phase difference  $\Delta\delta = \delta_{D^0} - \delta_{D^\pm}$
- determine  $B^+$  and  $B^-$  event yields in each region  $i$ :

$$N_i(B^\pm) = K_{\mp i} + (x_\pm^2 + y_\pm^2) \cdot K_{\pm i} + 2 \sqrt{K_{+i} K_{-i}} \cdot \left\{ x_\pm < \cos(\Delta\delta_D) >_i \mp y_\pm < \sin(\Delta\delta_D) >_i \right\}$$

$$x_\pm = r_B \cdot \cos(\delta_B \pm \gamma) \quad ; \quad y_\pm = r_B \cdot \sin(\delta_B \pm \gamma)$$

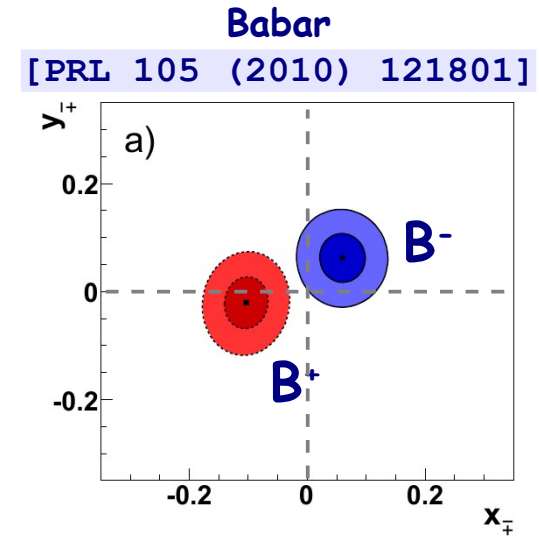
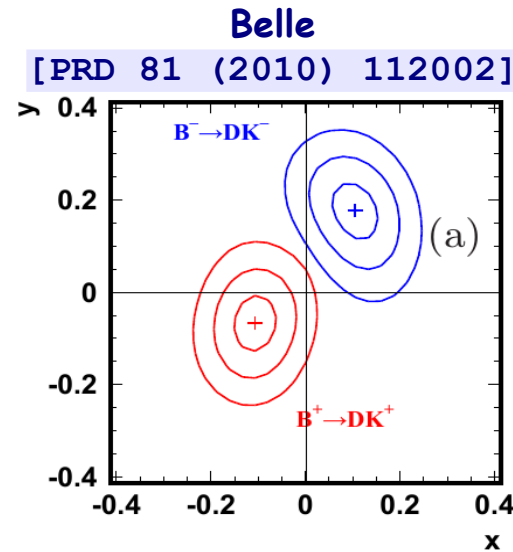
$K_i$ : numbers of  $D \rightarrow K^0 h^+ h^-$  events from  $D^{*\pm} \rightarrow D \pi^\pm$



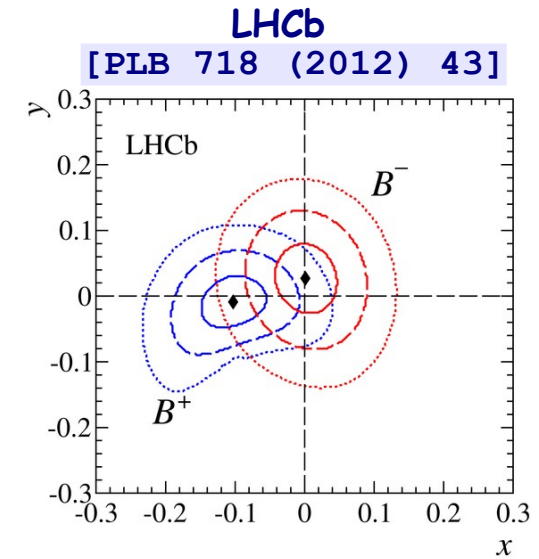
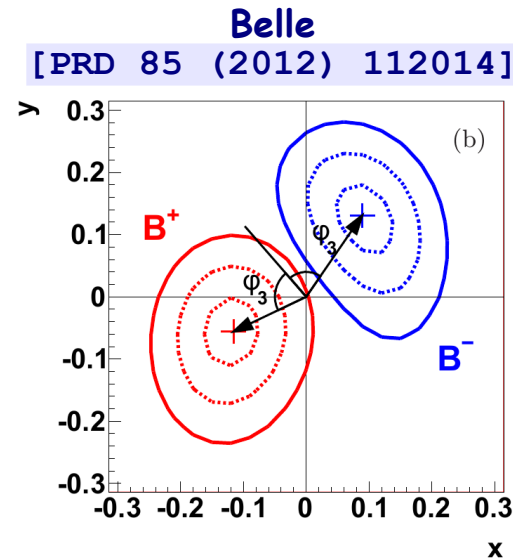
CLEO-c [PRD 82 (2010) 112006]

Fit in "cartesian" coordinates  $x_{\pm}, y_{\pm}$  to avoid bias from  $r_b > 0$

- model-dependent approach:
  - Belle,  $657 \times 10^6 \Upsilon(4s) \rightarrow B\bar{B}$  decays
  - Babar,  $467 \times 10^6 \Upsilon(4s) \rightarrow B\bar{B}$  decays



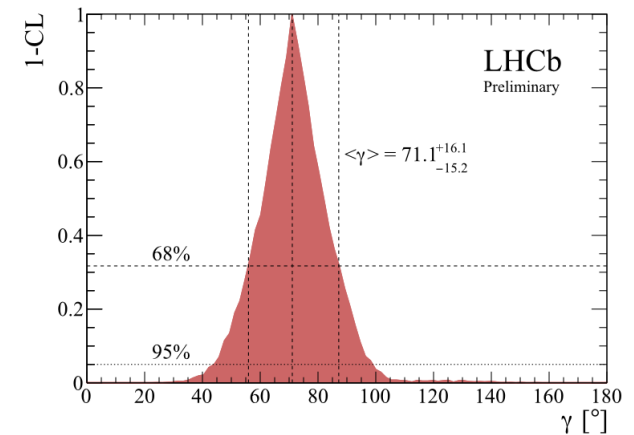
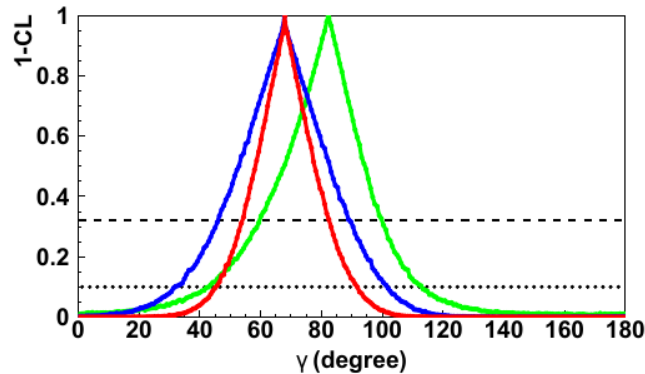
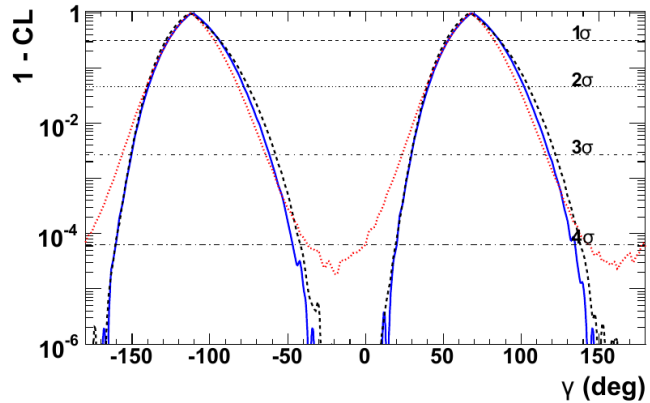
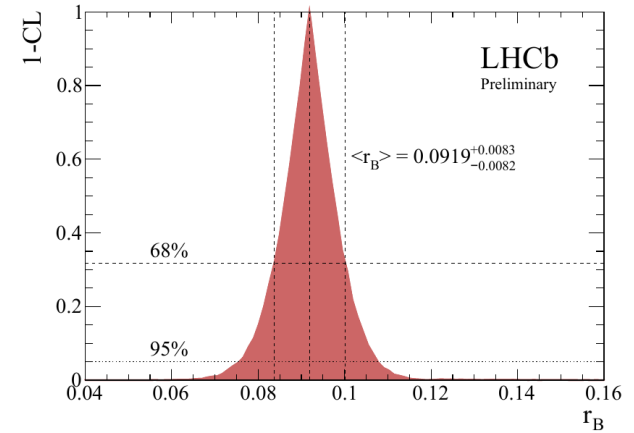
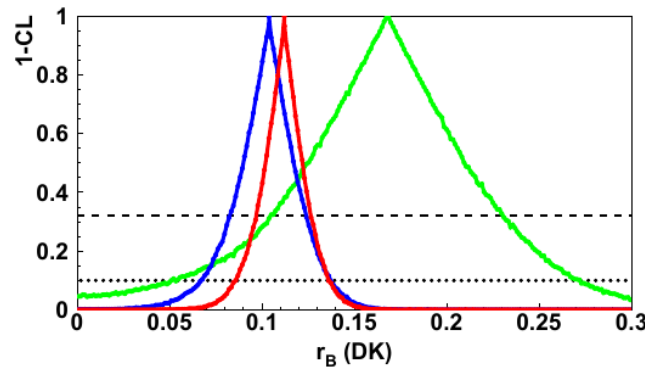
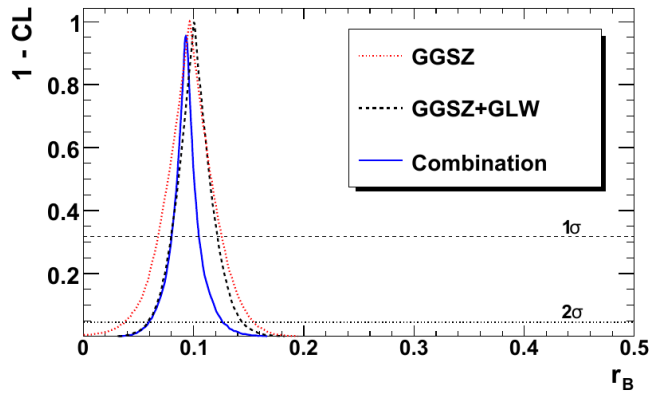
- model-independent approach:
  - Belle,  $772 \times 10^6 \Upsilon(4s) \rightarrow B\bar{B}$  decays
  - LHCb,  $1\text{fb}^{-1}$  (2011 data set)



- LHCb results already match precision from B factories

- LHCb result indicates smaller value of  $r_b \rightarrow$  sensitivity to  $\gamma$  reduced

# $\gamma$ from Trees: Combinations



$$\langle \gamma \rangle_{\text{Babar}} = \left( 69^{+17}_{-16} \right)^\circ$$

[arXiv:1301.1029]

$$\langle \gamma \rangle_{\text{Belle}} = \left( 68^{+15}_{-14} \right)^\circ$$

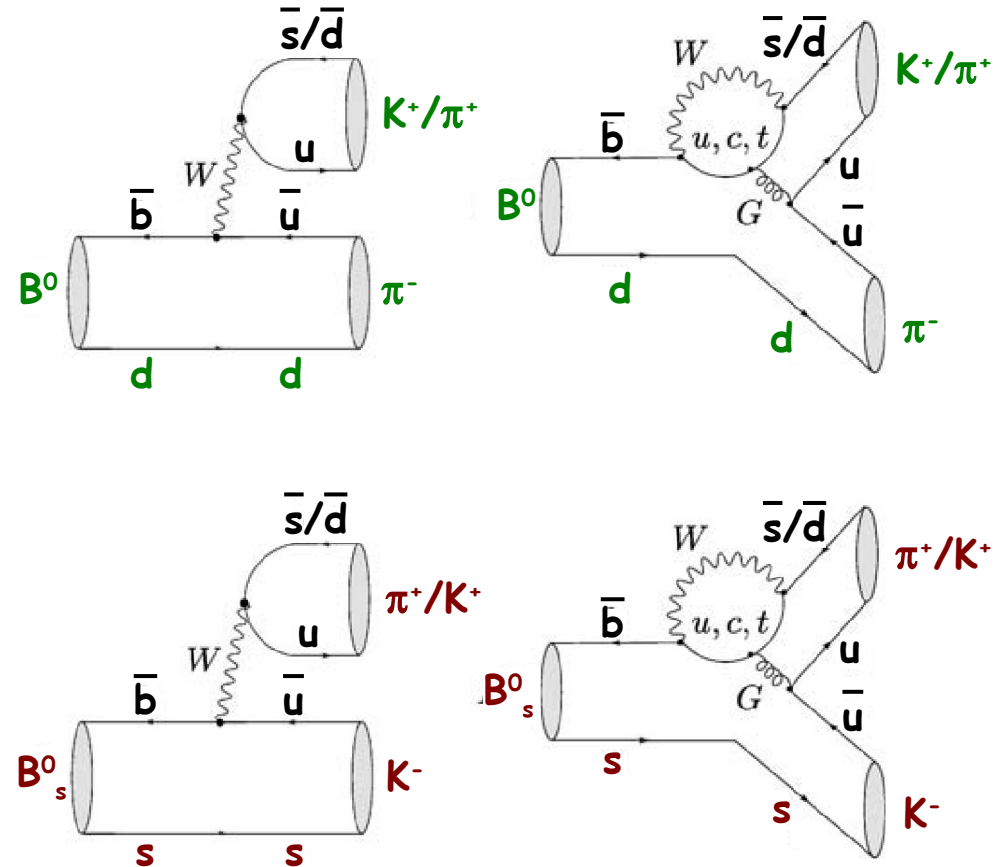
[arXiv:1301.2033]

$$\langle \gamma \rangle_{\text{LHCb}} = \left( 71^{+16.1}_{-15.2} \right)^\circ$$

[LHCb-CONF-2012-032]  
preliminary

## Direct CP violation in 2-body charmless B decays

- sensitivity to  $\gamma$  through interference of  $b \rightarrow u$  Tree diagrams ( $V_{ub} \sim e^{i\gamma}$ ) and  $b \rightarrow s(d)$  Penguin diagrams
- sensitive to possible contribution from New Physics in Penguin loops
- comparison with from  $\gamma$  Trees !
- hadronic uncertainties: can be controlled using U-Spin symmetry between  $B^0$  and  $B_s^0$  decays
- two approaches:
  - time-dependent CP asymmetry in  $B^0 \rightarrow \pi^+ \pi^-$  and  $B_s^0 \rightarrow K^+ K^-$
  - time-integrated CP asymmetry in  $B^0 \rightarrow K^+ \pi^-$  and  $B_s^0 \rightarrow \pi^+ K^-$



R.Fleischer, [EPJ C52 (2007) 267]

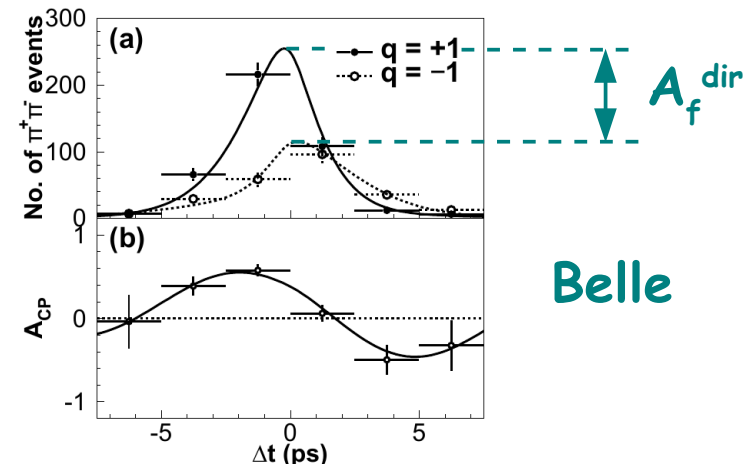
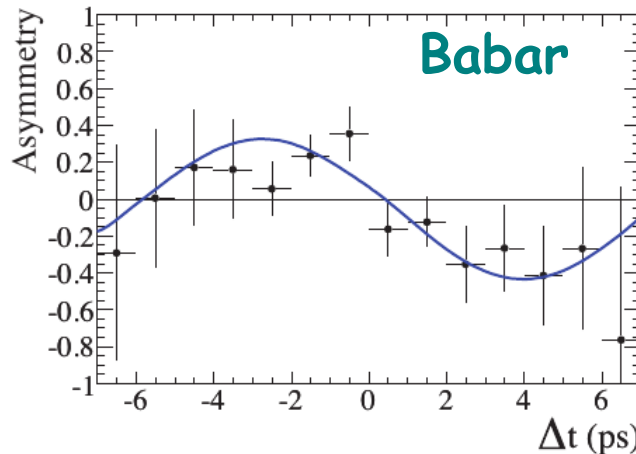
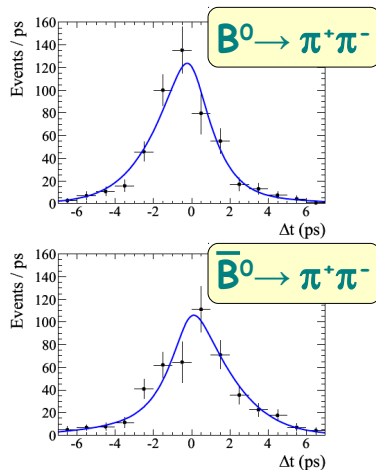
# $B^0 \rightarrow \pi^+ \pi^-$ : B factories

## Measure time-dependent asymmetry of decay rates

$$A_{CP}(t) = \frac{\Gamma(B_{(s)}^0(t=0) \rightarrow f) - \Gamma(\bar{B}_{(s)}^0(t=0) \rightarrow f)}{\Gamma(B_{(s)}^0(t=0) \rightarrow f) + \Gamma(\bar{B}_{(s)}^0(t=0) \rightarrow f)} = \frac{A_f^{dir} \cos(\Delta m_{(s)} t) + A_f^{mix} \sin(\Delta m_{(s)} t)}{\cosh\left(\frac{\Delta \Gamma_{(s)}}{2} t\right) - A_f^{\Delta \Gamma} \sinh\left(\frac{\Delta \Gamma_{(s)}}{2} t\right)}$$

- both mixing-induced CP violation ( $A_f^{mix}$ ) and CP violation in decay ( $A_f^{dir}$ )
- for  $\gamma$  measurements, we are interested in  $A_f^{dir}$
- $A_f^{mix}$  in  $B^0 \rightarrow \pi^+ \pi^-$  allows to extract CKM angle  $\sin 2\alpha$  at B factories
  - exploiting Isospin relations between  $B^0 \rightarrow \pi^+ \pi^-$ ,  $B^0 \rightarrow \pi^0 \pi^0$  and  $B^\pm \rightarrow \pi^\pm \pi^0$
  - sorry, no time to cover this here (maybe in the discussion session?)

[arXiv:1206.3525]



[PRL 98 (2007) 211801]

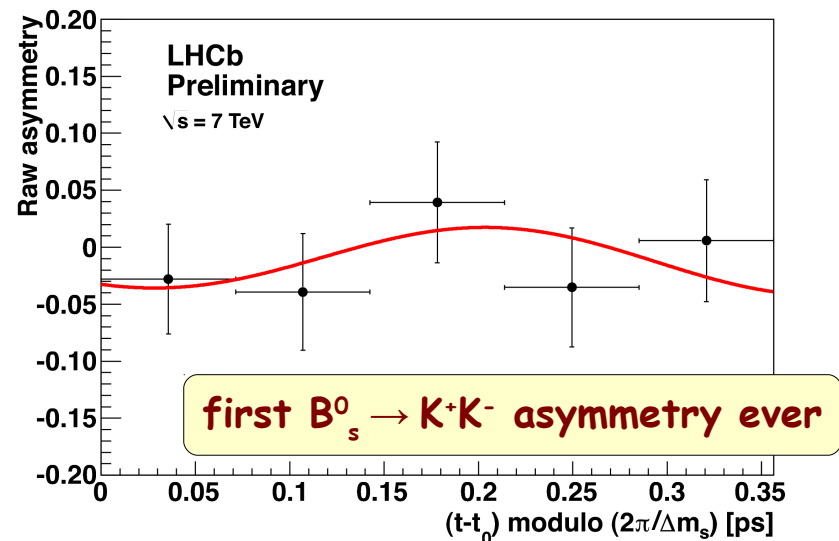
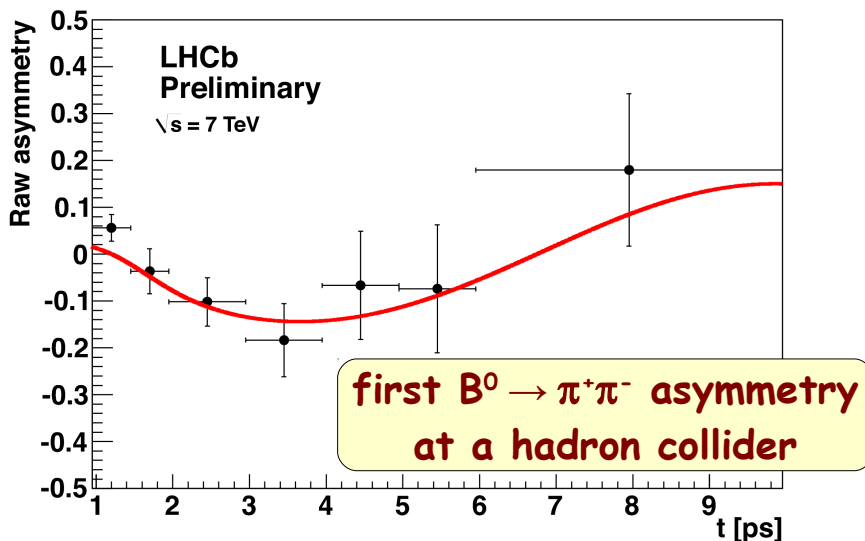
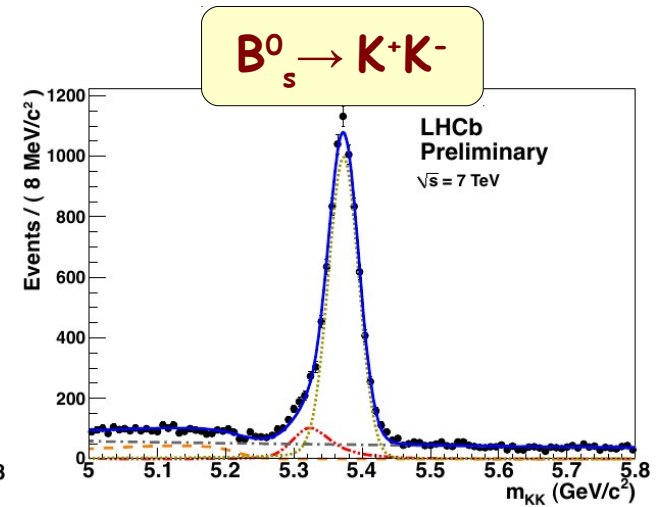
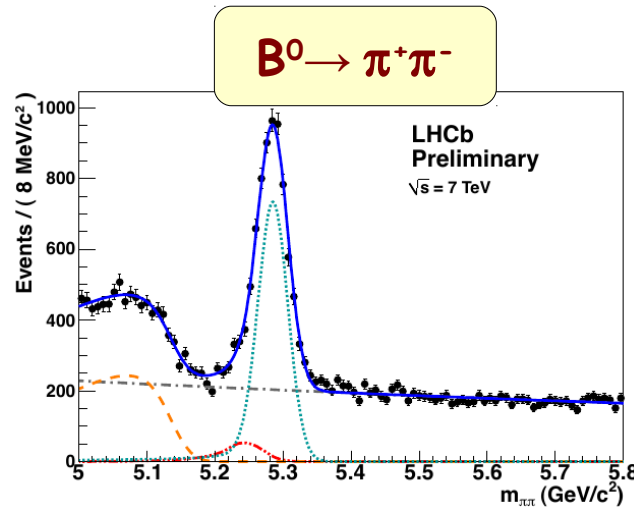
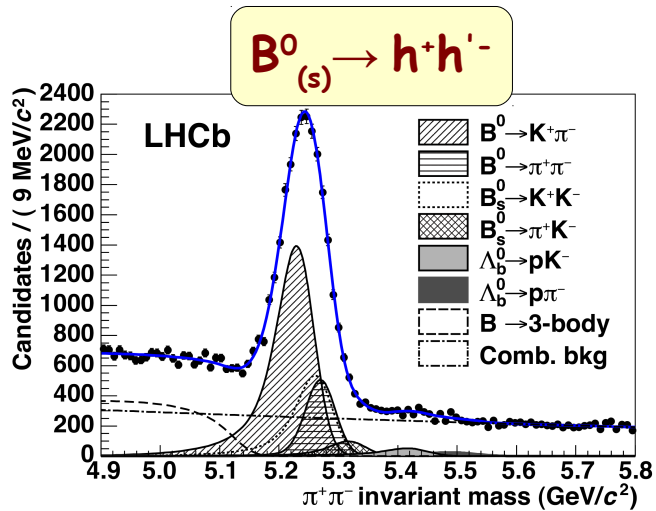
# $B^0_{(s)} \rightarrow h^+ h^- : \text{LHCb}$

Analysis of  $0.69 \text{ fb}^{-1}$  (2/3 of 2011 data set)

[LHCb-CONF-2012-007]

preliminary

- note the power and importance of  $\pi/K$  separation:





# $B^0_{(s)} \rightarrow h^+ h^-$ : Comparison

## First LHCb results promising

[LHCb-CONF-2012-007]

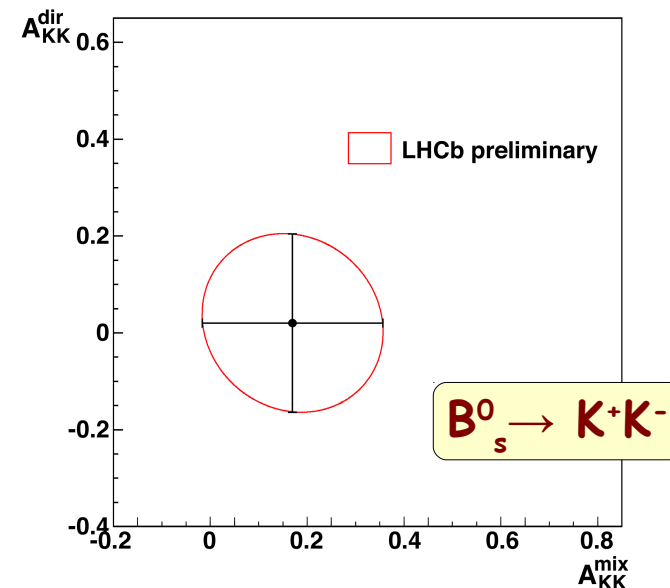
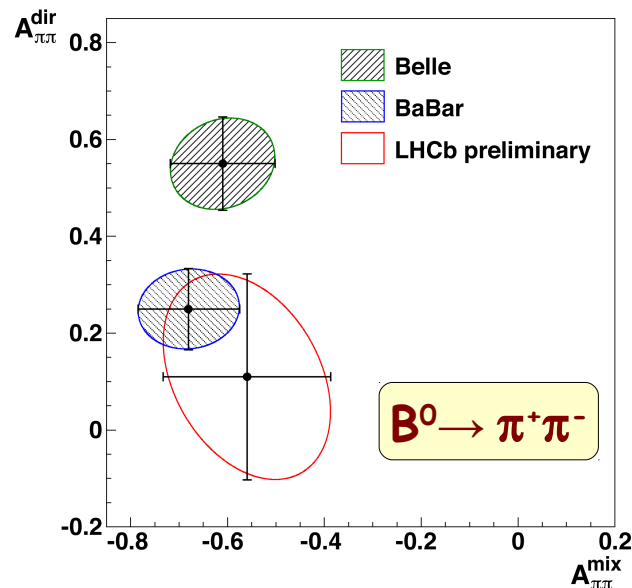
preliminary

- statistical precision not yet sufficient to attempt a  $\gamma$  determination
- but systematic uncertainties very small and six times more data “on tape”

$$A_{\pi\pi}^{\text{dir}} = 0.11 \pm 0.21 \pm 0.03$$

$$A_{KK}^{\text{dir}} = 0.02 \pm 0.18 \pm 0.04$$

- $A_{\pi\pi}^{\text{dir}}$  comparison with B factories: LHCb result favours Babar over Belle



# $B^0_{(s)} \rightarrow h^+ h^-$ : Comparison

## First LHCb results promising

[LHCb-CONF-2012-007]

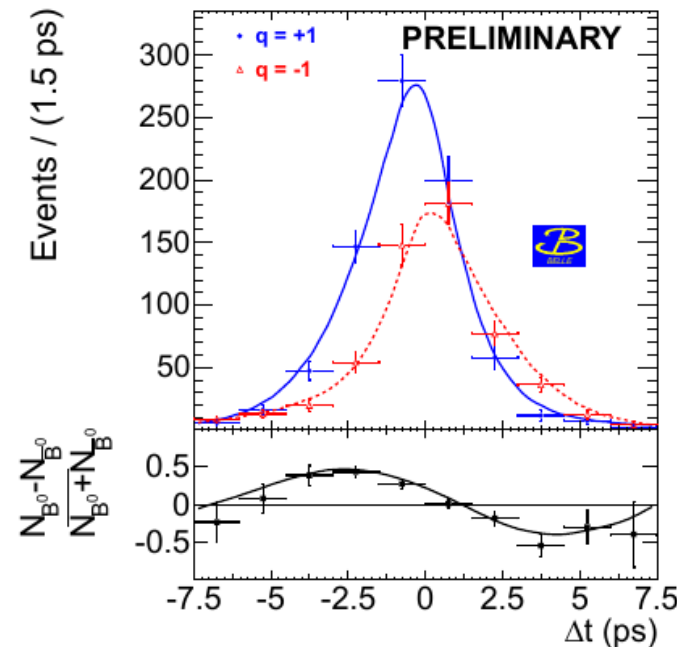
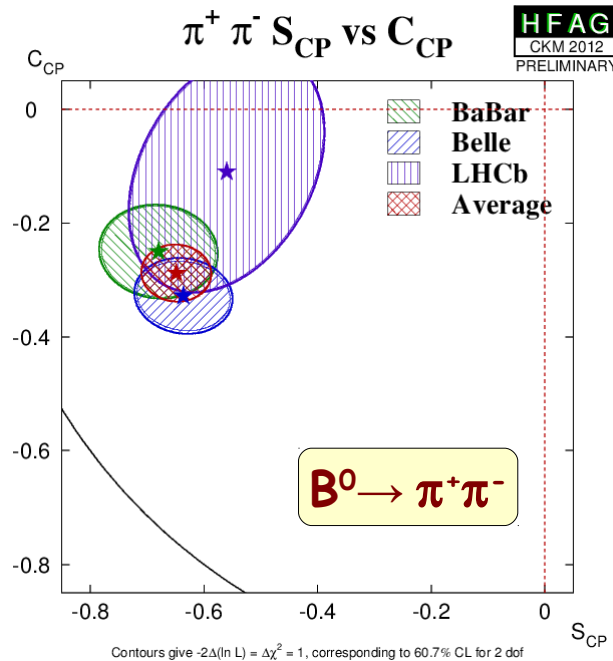
preliminary

- statistical precision not yet sufficient to attempt a  $\gamma$  determination
- but systematic uncertainties very small and six times more data "on tape"

$$A_{\pi\pi}^{\text{dir}} = 0.11 \pm 0.21 \pm 0.03$$

- $A_{\pi\pi}^{\text{dir}}$  comparison with B factories: new preliminary Belle result

[CKM 2012]



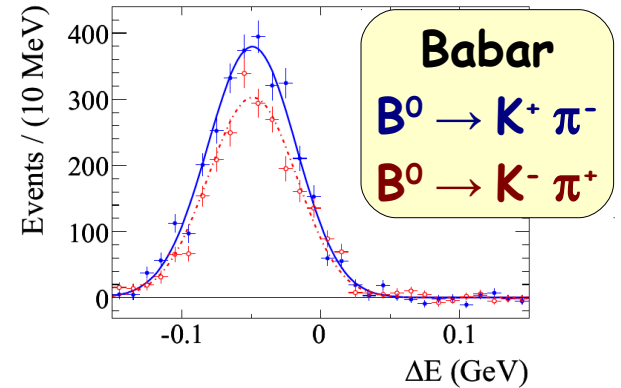
## Time-integrated decay rate asymmetry to flavour-specific final states

$$A_{CP} = \frac{\Gamma(B^0_{(s)} \rightarrow f) - \Gamma(\bar{B}^0_{(s)} \rightarrow \bar{f})}{\Gamma(B^0_{(s)} \rightarrow f) + \Gamma(\bar{B}^0_{(s)} \rightarrow \bar{f})}$$

- Babar analysis of full dataset

[arXiv:1206.3525]

$$A_{CP} = -0.107 \pm 0.016^{+0.006}_{-0.004}$$



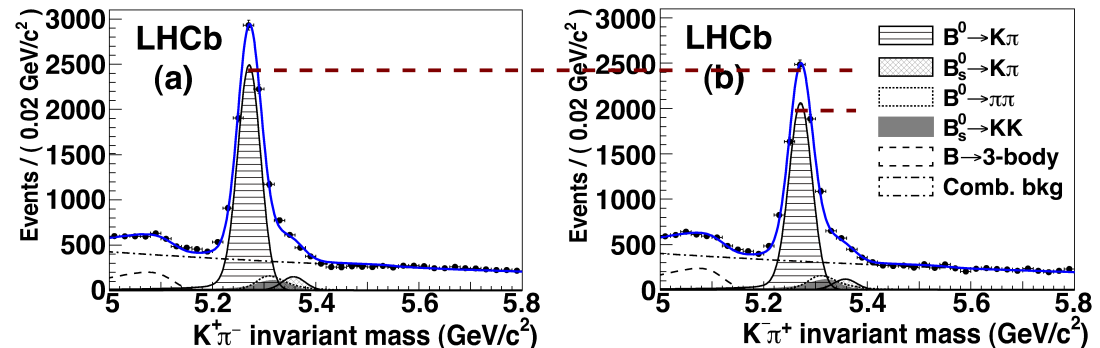
- LHCb analysis of  $0.35 \text{ fb}^{-1}$  (1/3 of 2011 data set)

[PRL 108 (2012) 201601]

- $B^0 \rightarrow K^+ \pi^- / \bar{B}^0 \rightarrow K^- \pi^+$

$$A_{CP} = -0.088 \pm 0.011 \pm 0.008$$

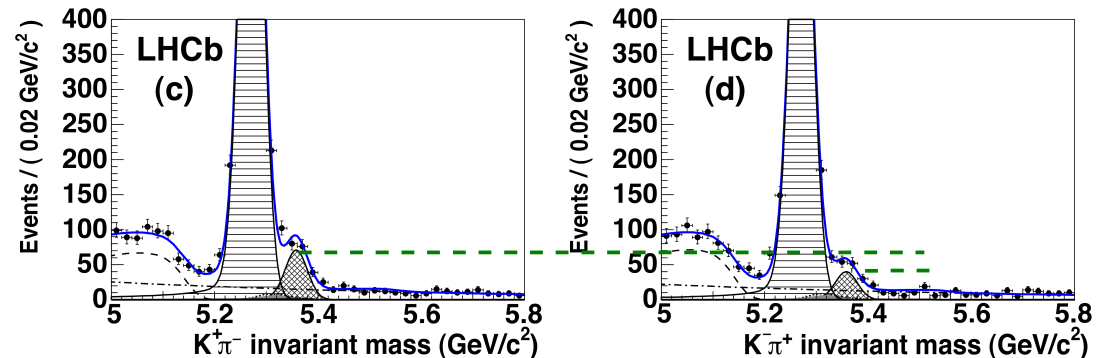
- first observation of CP violation at a hadron collider ( $6 \sigma$ )



- $B^0_s \rightarrow K^- \pi^+ / \bar{B}^0_s \rightarrow K^+ \pi^-$

$$A_{CP} = 0.27 \pm 0.08 \pm 0.02$$

- first evidence for CP violation in the  $B^0_s$  system ( $3.2 \sigma$ )



- **Part I: Introduction**

- what is (quark) flavour physics and why is it so exciting?
- how we got here: brief history of flavour physics in the 20<sup>th</sup> century

- **Part II: Particle-Antiparticle Mixing**

- a short summary of the formalism (don't worry, I'm an experimentalist ... )
- introduce experimental facilities and techniques

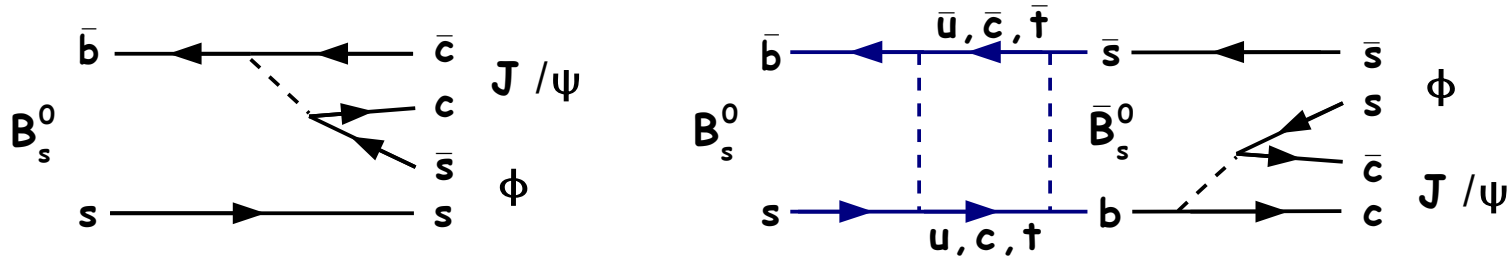
- **Part III: Precision tests of the Standard Model**

- **CP violating observables:**  $\sin 2\beta$ , CKM angle  $\gamma$ ,  $B_s^0 \bar{B}_s^0$  mixing phase  $\phi_s$
- rare decays: search for  $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ , angular observables in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

# CP violation in $B_s^0 \rightarrow J/\psi \phi$

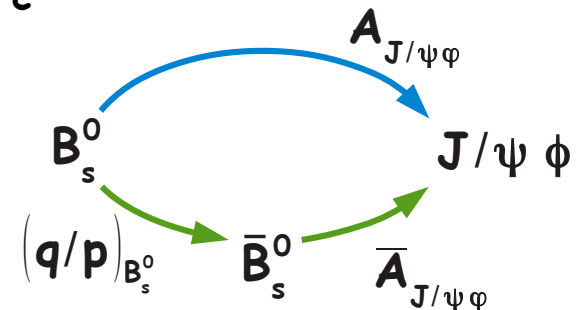
"Golden decay" of the  $B_s^0$  system, equivalent of  $B^0 \rightarrow J/\psi K^0$

- CP violation through interference between mixing and decay



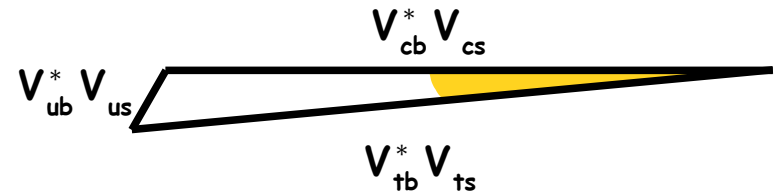
- but CP violating phase predicted to be very small

$$\lambda_{J/\psi\phi} = \left( \frac{q}{p} \right)_{B_s^0} \cdot \left( \frac{\bar{A}_{J/\psi\phi}}{A_{J/\psi\phi}} \right) = 2 \left( \frac{V_{tb}^* V_{ts}}{V_{cb}^* V_{cs}} \right) = e^{-i\phi_s}$$



- $\phi_s$  is the small angle in one of the "squashed" unitarity triangles

$$\begin{pmatrix} V_{ud}^* & V_{cd}^* & V_{td}^* \\ V_{us}^* & V_{cs}^* & V_{ts}^* \\ V_{ub}^* & V_{cb}^* & V_{tb}^* \end{pmatrix} \times \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



- Standard Model prediction:

$$\phi_s = 0.036 \pm 0.002 \text{ rad}$$

J.Charles et al., [PRD 84 (2011) 033005]

- sensitive to possible New Physics contributions in  $B_s^0 - \bar{B}_s^0$  mixing

## Measure time-dependent CP asymmetry

- for CP eigenstate  $f$  with eigenvalue  $\eta_f = \pm 1$

$$A_{CP}(\mathbf{t}) = \frac{\Gamma(\bar{B}_s^0(\mathbf{t}=0) \rightarrow f) - \Gamma(B_s^0(\mathbf{t}=0) \rightarrow f)}{\Gamma(\bar{B}_s^0(\mathbf{t}=0) \rightarrow f) + \Gamma(B_s^0(\mathbf{t}=0) \rightarrow f)} = \eta_f \boxed{\sin \phi_s} \sin(\Delta m_s \mathbf{t})$$

- determine flavour of  $B_s$  meson at  $\mathbf{t} = 0 \rightarrow$  mis-tag fraction  $\boxed{\omega_{\text{tag}}}$

- resolve rapid  $B_s^0 - \bar{B}_s^0$  oscillations  $\rightarrow$  finite proper time resolution  $\boxed{\sigma_{\mathbf{t}}}$

$$A_{CP}(\mathbf{t}) \approx (1 - \boxed{2\omega_{\text{tag}}}) e^{-\frac{1}{2}\Delta m_s^2 \boxed{\sigma_{\mathbf{t}}^2}} \eta_f \boxed{\sin \phi_s} \sin(\Delta m_s \mathbf{t})$$

- final state in  $B_s^0 \rightarrow J/\psi \phi$  is a mix of CP even and odd ( $L_{J/\psi\phi} = 0, 1, 2$ )
  - three polarisation amplitudes, plus non-resonant  $K^+ K^-$  amplitude (S-wave)
  - time-dependent angular analysis to disentangle these and determine  $\phi_s$
- finite lifetime difference  $\Delta\Gamma_s$  between CP eigenstates in  $B_s^0 \bar{B}_s^0$  system
  - not well measured yet, needs to be determined simultaneously with  $\phi_s$

## Unbinned Maximum Likelihood fit to extract physics parameters

- fit parameters:

$$\phi_s, \Delta\Gamma_s$$

usually constrained to the value obtained in oscillation measurements

$$m_s, \bar{\Gamma}_s, (\Delta m_s)$$

$$|A_0|, |A_{\parallel}|, |A_{\perp}|, \delta_{\parallel}, \delta_{\perp}, \delta_0$$

- tagging parameters

- signal fraction

- background parameters

- event-by-event inputs:

- reconstructed invariant mass & uncertainty

- reconstructed decay time & uncertainty

- three decay angles  $\Omega = (\theta = \theta_{\mu}, \phi = \phi_h, \psi = \theta_K)$

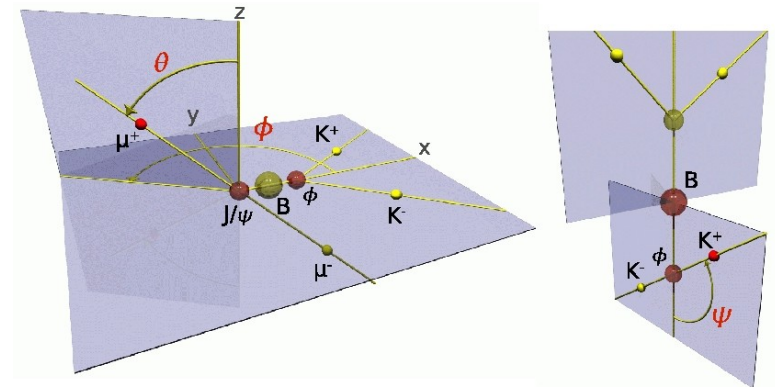
- tagging decision & estimated tagging dilution

$$\frac{d^4\Gamma(B_s^0 \rightarrow J/\psi \phi)}{dt d\Omega} \propto \sum_{k=1}^{10} h_k(t) f_k(\Omega)$$

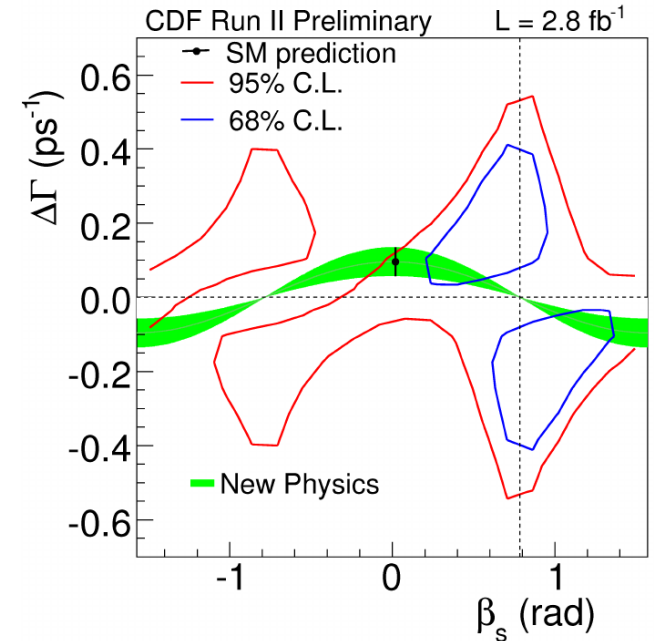
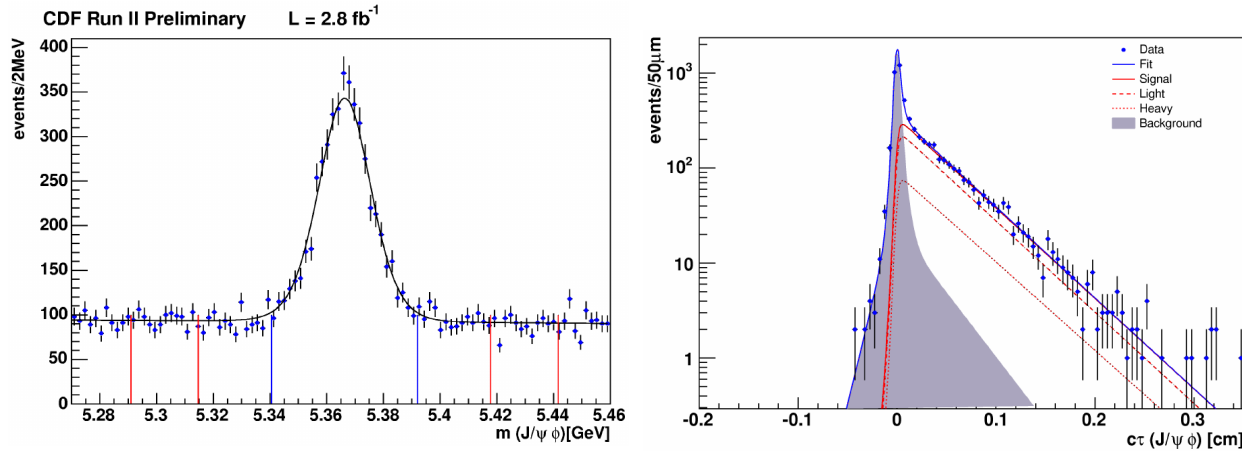
$$h_k(t) = N_k e^{-Gt} \left[ a_k \cosh\left(\frac{1}{2}\Delta\Gamma_s t\right) + b_k \sinh\left(\frac{1}{2}\Delta\Gamma_s t\right) + c_k \cos(\Delta m_s t) + d_k \sin(\Delta m_s t) \right]$$

$k$	$f_k(\theta_{\mu}, \theta_K, \phi_h)$	$N_k$	$a_k$	$b_k$	$c_k$	$d_k$
1	$2 \cos^2 \theta_K \sin^2 \theta_{\mu}$	$ A_0(0) ^2$	1	$D$	$C$	$-S$
2	$\sin^2 \theta_K (1 - \sin^2 \theta_{\mu} \cos^2 \phi_h)$	$ A_{\parallel}(0) ^2$	1	$D$	$C$	$-S$
3	$\sin^2 \theta_K (1 - \sin^2 \theta_{\mu} \sin^2 \phi_h)$	$ A_{\perp}(0) ^2$	1	$-D$	$C$	$S$
4	$\sin^2 \theta_K \sin^2 \theta_{\mu} \sin 2\phi_h$	$ A_{\parallel}(0)A_{\perp}(0) $	$C \sin(\delta_{\perp} - \delta_{\parallel})$	$S \cos(\delta_{\perp} - \delta_{\parallel})$	$\sin(\delta_{\perp} - \delta_{\parallel})$	$D \cos(\delta_{\perp} - \delta_{\parallel})$
5	$\frac{1}{2}\sqrt{2} \sin 2\theta_K \sin 2\theta_{\mu} \cos \phi_h$	$ A_0(0)A_{\parallel}(0) $	$\cos(\delta_{\parallel} - \delta_0)$	$D \cos(\delta_{\parallel} - \delta_0)$	$C \cos(\delta_{\parallel} - \delta_0)$	$-S \cos(\delta_{\parallel} - \delta_0)$
6	$-\frac{1}{2}\sqrt{2} \sin 2\theta_K \sin 2\theta_{\mu} \sin \phi_h$	$ A_0(0)A_{\perp}(0) $	$C \sin(\delta_{\perp} - \delta_0)$	$S \cos(\delta_{\perp} - \delta_0)$	$\sin(\delta_{\perp} - \delta_0)$	$D \cos(\delta_{\perp} - \delta_0)$
7	$\frac{2}{3} \sin^2 \theta_{\mu}$	$ A_s(0) ^2$	1	$-D$	$C$	$S$
8	$\frac{1}{3}\sqrt{6} \sin \theta_K \sin 2\theta_{\mu} \cos \phi_h$	$ A_s(0)A_{\parallel}(0) $	$C \cos(\delta_{\parallel} - \delta_S)$	$S \sin(\delta_{\parallel} - \delta_S)$	$\cos(\delta_{\parallel} - \delta_S)$	$D \sin(\delta_{\parallel} - \delta_S)$
9	$-\frac{1}{3}\sqrt{6} \sin \theta_K \sin 2\theta_{\mu} \sin \phi_h$	$ A_s(0)A_{\perp}(0) $	$\sin(\delta_{\perp} - \delta_S)$	$-D \sin(\delta_{\perp} - \delta_S)$	$C \sin(\delta_{\perp} - \delta_S)$	$S \sin(\delta_{\perp} - \delta_S)$
10	$\frac{4}{3}\sqrt{3} \cos \theta_K \sin^2 \theta_{\mu}$	$ A_s(0)A_0(0) $	$C \cos(\delta_0 - \delta_S)$	$S \sin(\delta_0 - \delta_S)$	$\cos(\delta_0 - \delta_S)$	$D \sin(\delta_0 - \delta_S)$

$$(S = \sin \phi_s ; C = \cos \phi_s ; D = 1 - C - S)$$

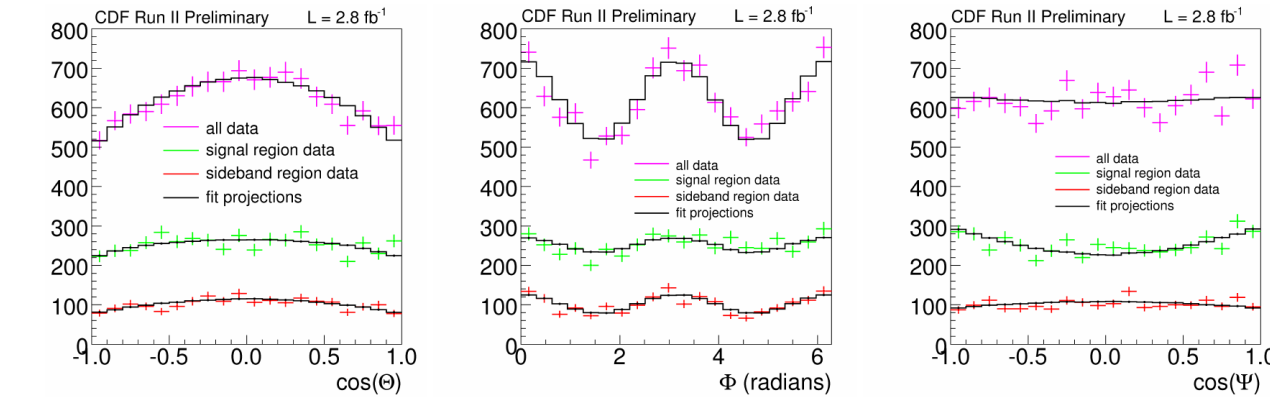


**CDF:  $\sim 3'200$  signal events from  $2.8 \text{ fb}^{-1}$**



**1.8  $\sigma$  deviation from Standard Model prediction (p-value = 7 %)**

[CDF/ANAL/BOTTOM/PUBLIC 9458]

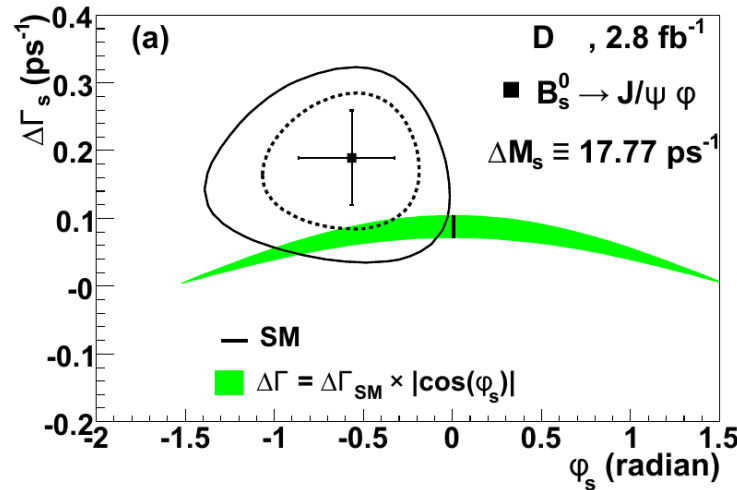
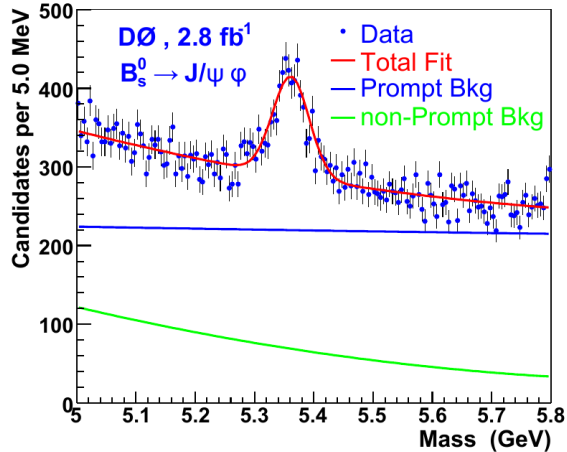


- note different convention:  $\phi_s = -2 \beta_s$
- note two-fold ambiguity: fit function invariant under transformation

$$(\phi_s, \Delta\Gamma_s, \delta_{\parallel}, \delta_{\perp}) \leftrightarrow (\pi - \phi_s, -\Delta\Gamma_s, 2\pi - \delta_{\parallel}, -\delta_{\perp})$$



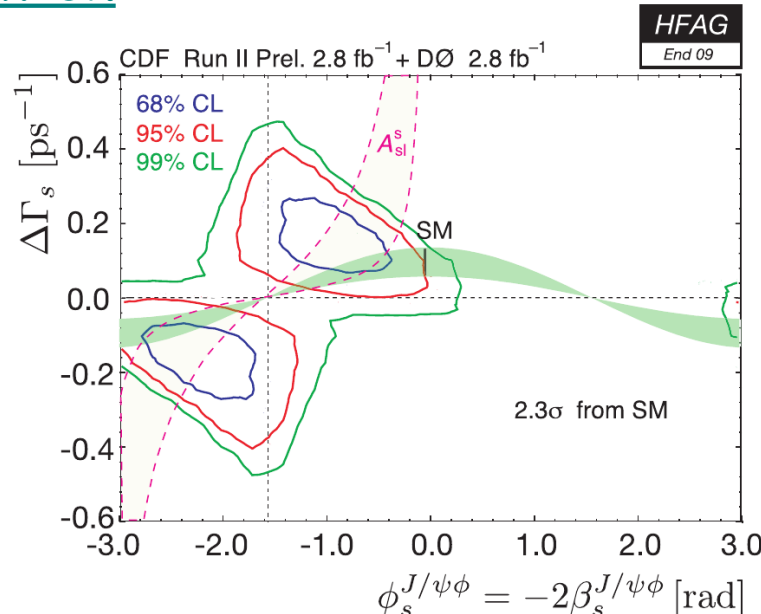
DØ: ~ 2'000 signal events from 2.8 fb<sup>-1</sup>



**1.5  $\sigma$  deviation from Standard Model prediction (p-value = 6.6 %)**

[PRL 101 (2008) 241801]

## CDF + DØ combination



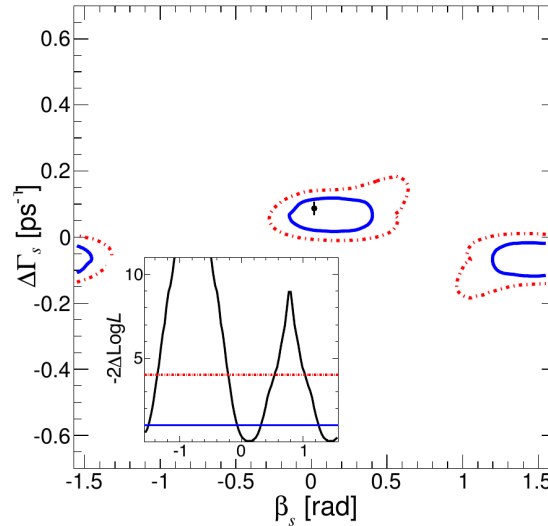
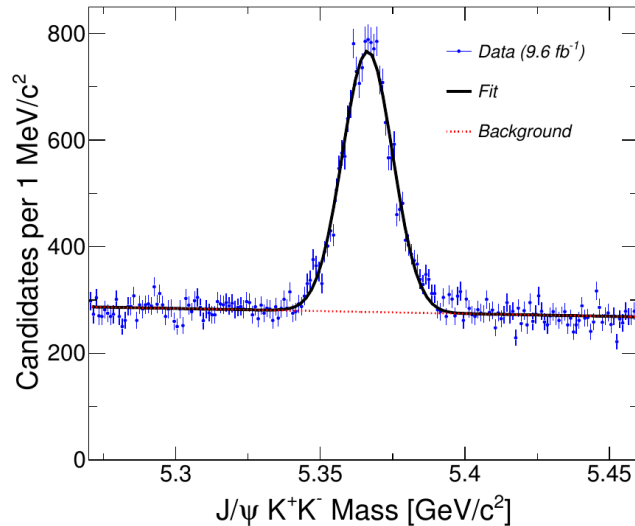
**2.3  $\sigma$  deviation from Standard Model prediction**

**2.8  $\sigma$  deviation when including DØ result for  $A_{sl}^s$**

[arXiv:1010.1589]

# $B_s^0 \rightarrow J/\psi \phi$ : Tevatron 2012

CDF:  $\sim 11'000$  signal events from  $9.6 \text{ fb}^{-1}$  (their full dataset)

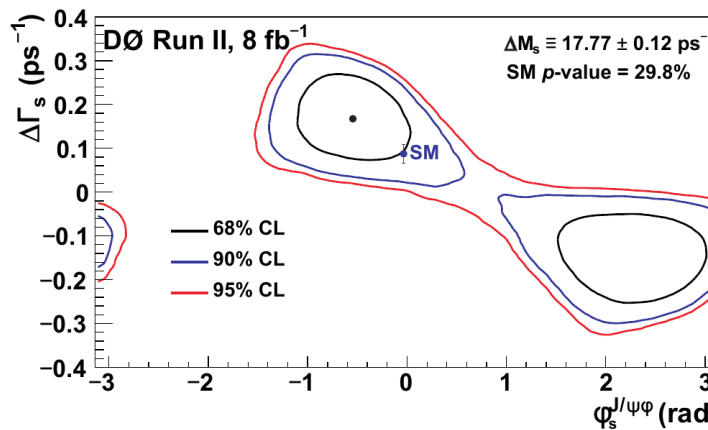
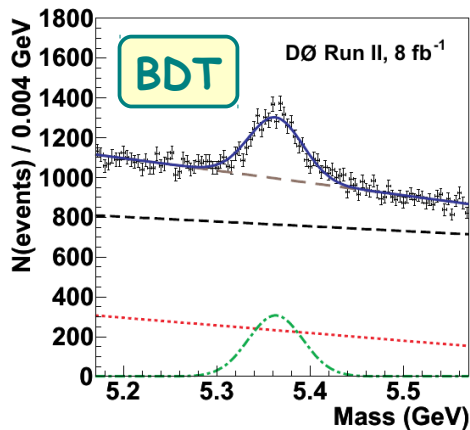


$$-0.60 < \phi_s < 0.12 \text{ @ } 68\% \text{ C.L.}$$

$$(\phi_s = -2\beta_s)$$

[PRL 109 (2012) 171802]

DØ:  $\sim 5'600$  signal events from  $8.0 \text{ fb}^{-1}$  (for BDT-based selection)



$$\phi_s = -0.55^{+0.38}_{-0.36} \text{ @ } 68\% \text{ C.L.}$$

[PRD 85 (2012) 032006]

both compatible with Standard Model prediction

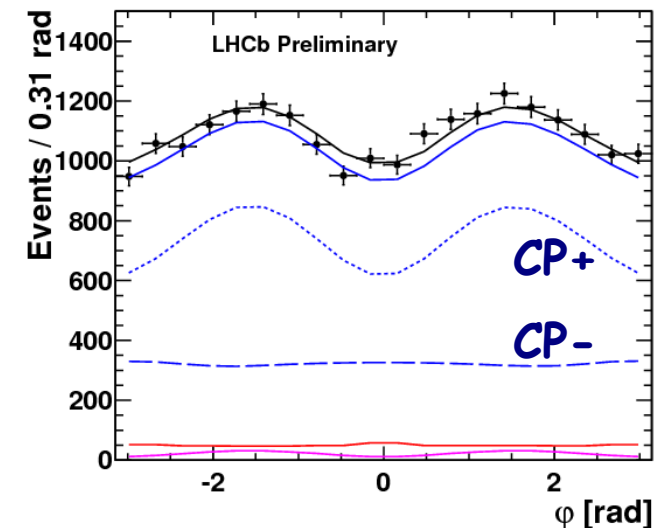
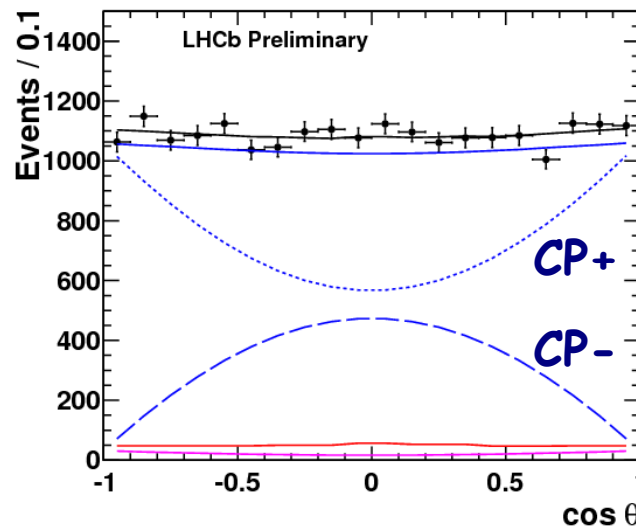
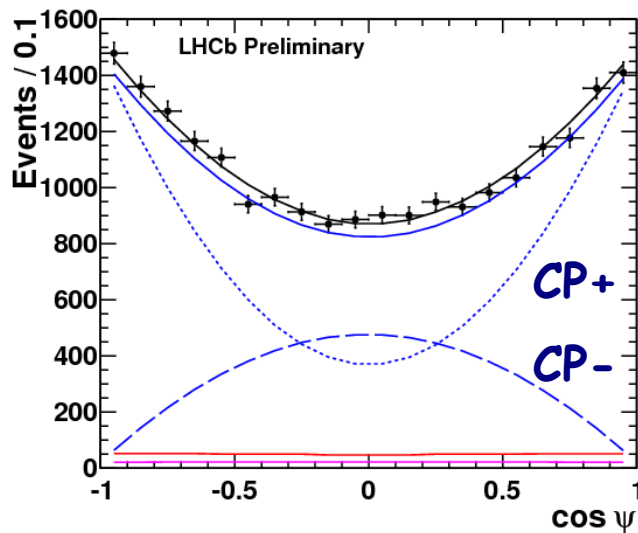
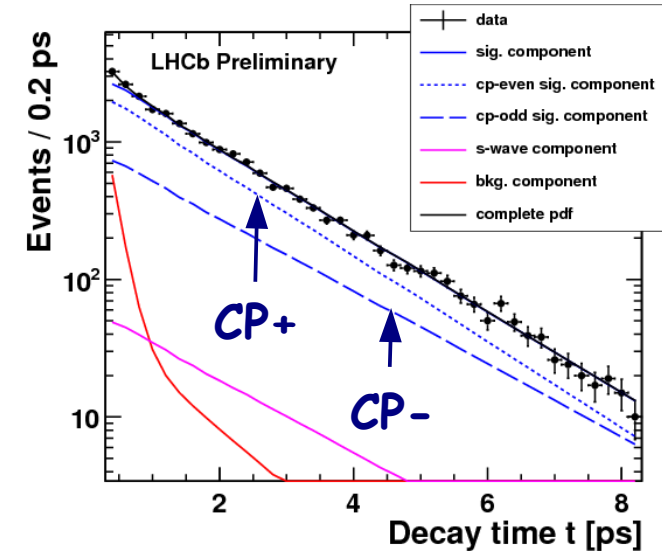
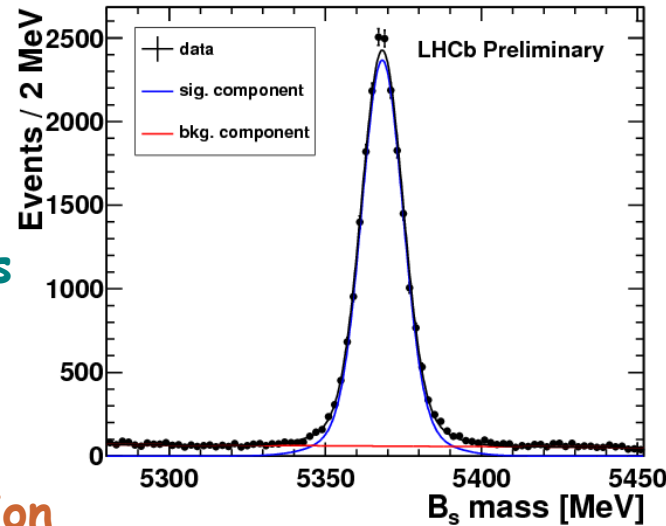
# $B_s^0 \rightarrow J/\psi \phi$ : LHCb

Analysis based on  $1 \text{ fb}^{-1}$  (2011 data set)

- $\sim 21'000$  signal events
- $2 \times \text{CDF}$  (!)
- only few % background
- angular fit cleanly separates CP even/odd components
- different  $B_H, B_L$  lifetimes clearly visible in fit projection

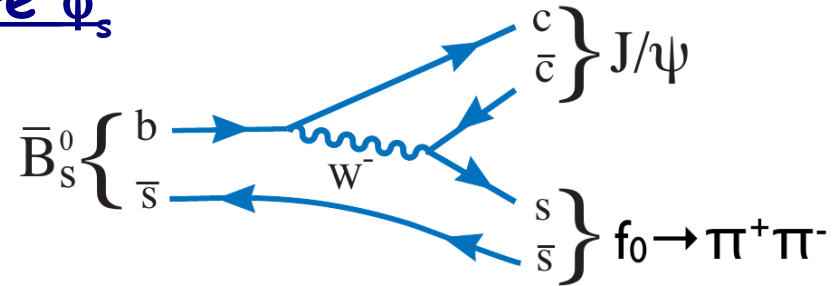
[LHCb-CONF-2012-002]

preliminary



## $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$ : another channel to measure $\phi_s$

- lower branching fraction than  $B_s^0 \rightarrow J/\psi \phi$ 
  - 7400 candidates from  $1.0 \text{ fb}^{-1}$
- but no angular analysis required
  - dominated by  $f_0(980) \rightarrow \pi^+ \pi^-$  resonance
  - almost pure CP odd (>99.7 % @ 95% CL)



$$\phi_s = -0.019^{+0.173 + 0.004}_{-0.174 - 0.003} \text{ rad}$$

[PLB 713 (2012) 378]

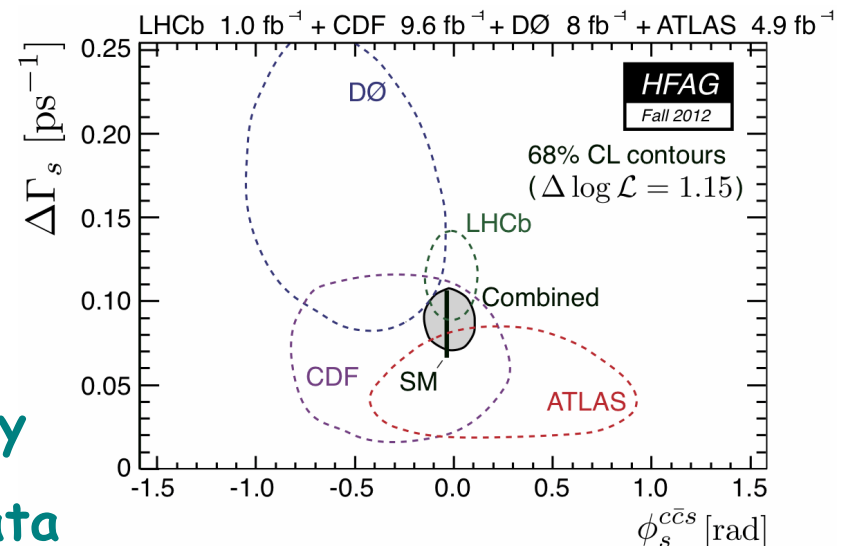
[PRD 86 (2012) 052006]

## Simultaneous LHCb fit of $B_s^0 \rightarrow J/\psi \phi$ and $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$

$$\phi_s = -0.002 \pm 0.083 \pm 0.027 \text{ rad}$$

[LHCb-CONF-2012-002] preliminary

- most precise measurement to date
- excellent agreement with Standard Model
- precision dominated by statistical uncertainty
- expect significant improvement with more data



## Resolve two-fold ambiguity in fit solution

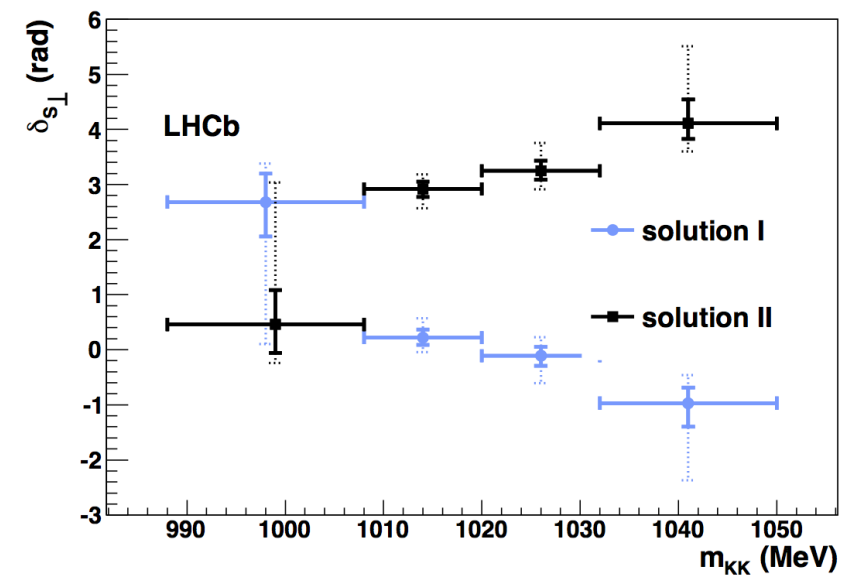
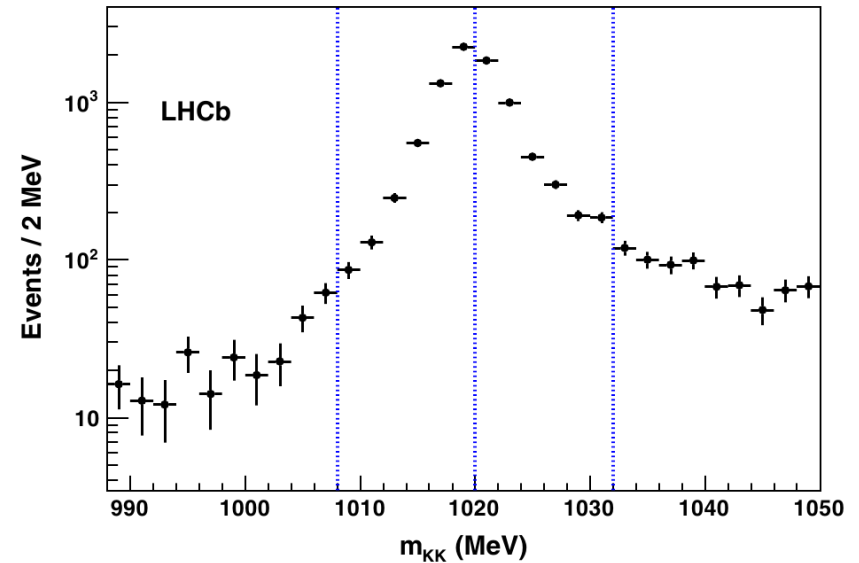
[PRL 108 (2012) 241801]

$$(\phi_s, \Delta\Gamma_s, \delta_{\parallel}, \delta_{\perp}) \leftrightarrow (\pi - \phi_s, -\Delta\Gamma_s, 2\pi - \delta_{\parallel}, -\delta_{\perp})$$

("solution I")                      ("solution II")

- look at strong phase difference  $\delta_{s\perp} = \delta_s - \delta_{\perp}$  between  $K^+K^-$  P-wave and S-wave amplitudes as a function of  $m(K^+K^-)$  around the  $\phi(1020)$ 
  - P-wave: going through  $\phi(1020)$  resonance  $\rightarrow$  expect rapid positive phase shift
  - S-wave: non-resonant + tail from  $f_0(980)$   $\rightarrow$  expect no significant variation of phase
- LHCb analysis based on  $0.37 \text{ fb}^{-1}$
- determine  $\delta_{s\perp}$  in four  $K^+K^-$  mass bins

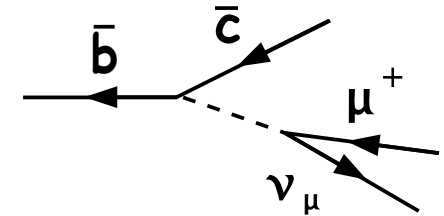
solution corresponding to  $\Delta\Gamma_s > 0$   
selected with  $4.7 \sigma$  significance



# Like-Sign Dimuon Asymmetry

## Compare numbers of $\mu^+\mu^+$ and $\mu^-\mu^-$ events from semileptonic B decays

- in collision produce  $b\bar{b}$  pairs;  $b \rightarrow \mu^- \bar{\nu}_\mu$  and  $\bar{b} \rightarrow \mu^+ \nu_\mu$
- observe  $\mu^-\mu^-$  event  $\rightarrow B^0_{(s)}$  must have mixed
- observe  $\mu^+\mu^+$  event  $\rightarrow \bar{B}^0_{(s)}$  must have mixed
- observe different numbers of  $\mu^-\mu^-$  and  $\mu^+\mu^+$  events  $\rightarrow$  CP violation in mixing



$$A_{sl}^b \equiv \frac{N_b^{++} - N_b^{--}}{N_b^{++} + N_b^{--}} \approx 0.6 \cdot a_{sl}^d + 0.4 \cdot a_{sl}^s$$

hadronization fractions,  
mixing probabilities

with the semileptonic asymmetries:

$$a_{sl}^d = \frac{\Delta\Gamma_d}{\Delta m_d} \cdot \tan\phi_d \quad ; \quad a_{sl}^s = \frac{\Delta\Gamma_s}{\Delta m_s} \cdot \tan\phi_s$$

- CP violation in mixing expected to be very small
- Standard Model predictions:

$$a_{sl}^d = (-4.1 \pm 0.6) \times 10^{-4} \quad ; \quad a_{sl}^s = (-1.9 \pm 0.3) \times 10^{-5}$$

A. Lenz,  
[arXiv:1205.1444]

## Challenge: large backgrounds and $\mu^\pm$ asymmetries from other sources

- largest source of background asymmetry: muons from kaon decays
  - $K^+$  ( $u\bar{s}$ ) have smaller interaction cross section with matter than  $K^-$  ( $\bar{u}s$ )
  - $K^+$  have more time to decay in the detector volume  $\rightarrow$  more  $\mu^+$  than  $\mu^-$
- other sources of backgrounds: pion decays, hadron punchthrough
- other sources of asymmetries: muon detection and identification efficiency

## $D0$ analysis using $9.0 \text{ fb}^{-1}$ (full data sample)

[PRD 84 (2011) 052007]

- basic idea: estimate and correct for background asymmetries from data using the measured charge asymmetry in large samples of inclusive muons

$$a \equiv \frac{n^+ - n^-}{n^+ + n^-}$$

$$A_{\text{raw}} = (+0.126 \pm 0.041) \%$$

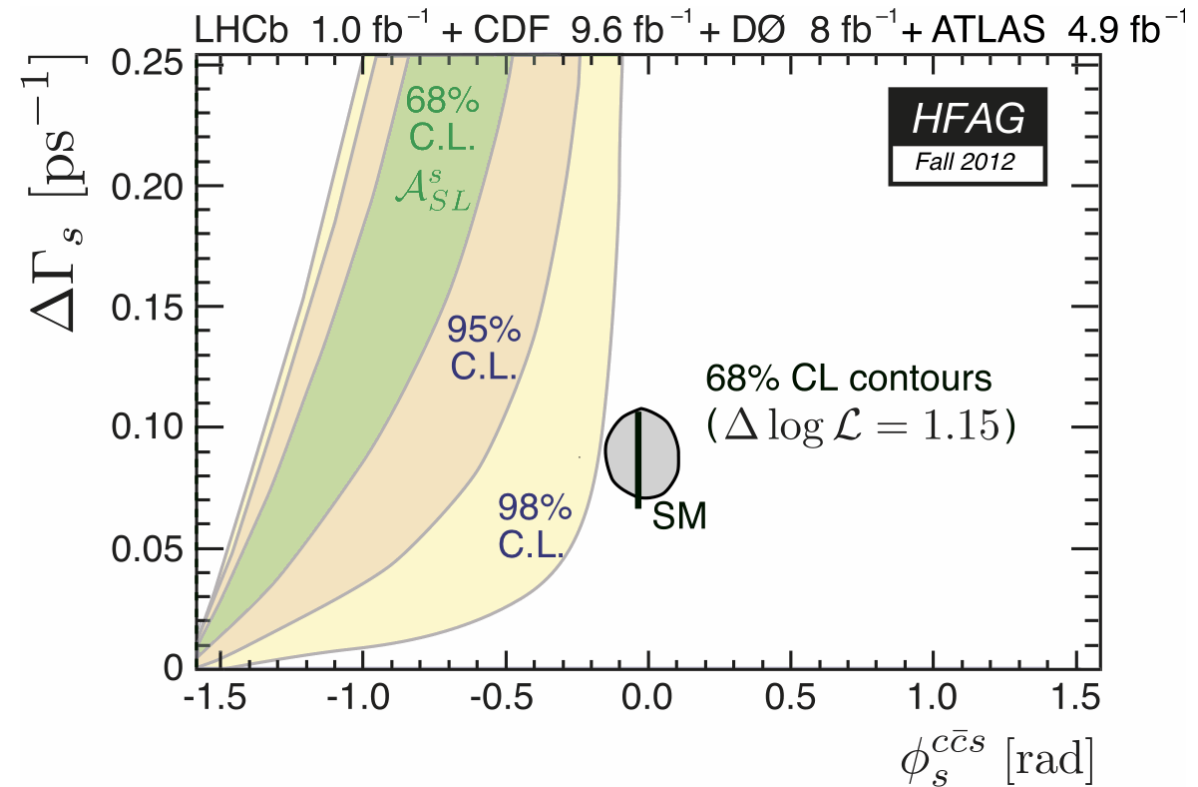
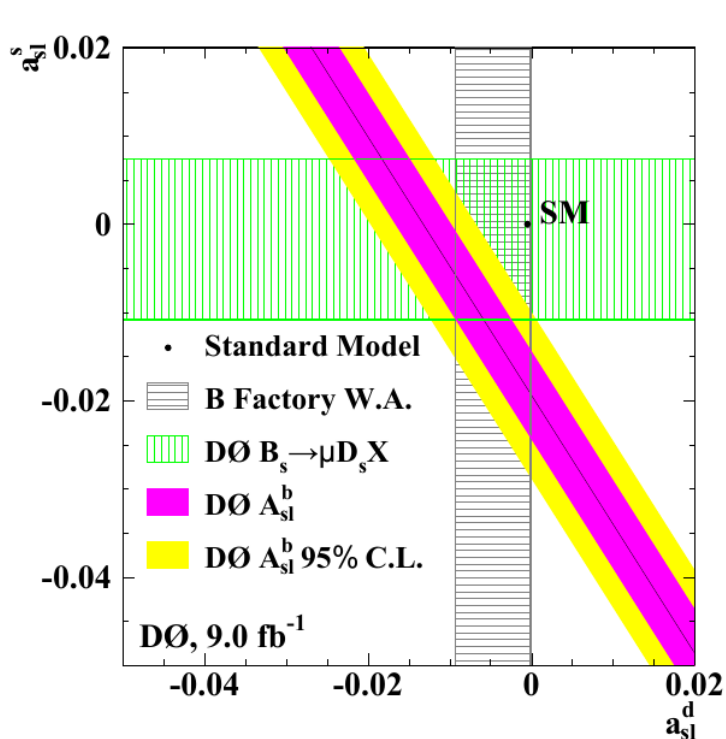
$$a = (+0.688 \pm 0.002) \%$$

- very intricate analysis, large corrections, but also many cross checks

$$A_{sl}^b = (-0.787 \pm 0.172 \pm 0.093) \%$$

## Measured asymmetry 34 times larger than Standard Model prediction

- 3.9  $\sigma$  discrepancy
- tension also with value of  $\phi_s$  measured in  $B_s^0 \rightarrow J/\psi \phi$  and  $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$



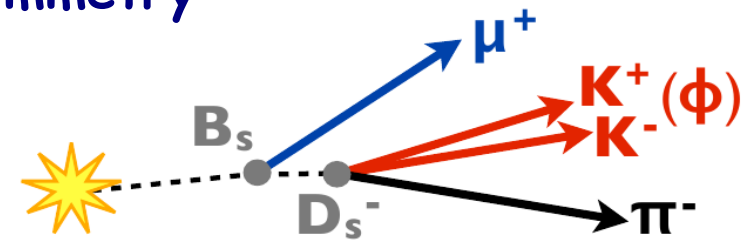


# Semileptonic Asymmetry

## LHC experiments cannot measure like-sign dimuon asymmetry

- large intrinsic charge asymmetry from pp collisions
- but LHCb can directly measure semileptonic asymmetry

$$a_{sl}^s = \frac{\Gamma(B_s^0 \rightarrow D_s^- \mu^+ X) - \Gamma(\bar{B}_s^0 \rightarrow D_s^+ \mu^- X)}{\Gamma(B_s^0 \rightarrow D_s^- \mu^+ X) + \Gamma(\bar{B}_s^0 \rightarrow D_s^+ \mu^- X)}$$



- pp collisions give rise to  $B_s^0 \bar{B}_s^0$  production asymmetry  $a_p \sim 1\%$
- but:  $a_p$  strongly diluted by very rapid  $B_s^0 - \bar{B}_s^0$  oscillations

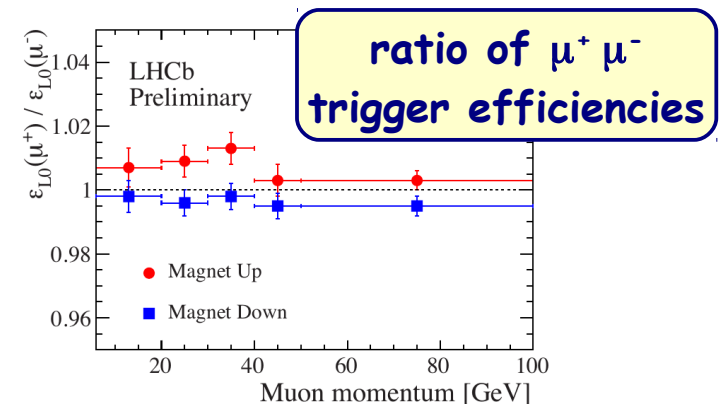
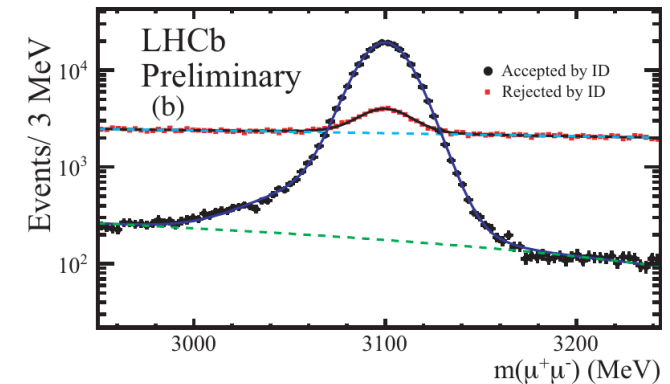
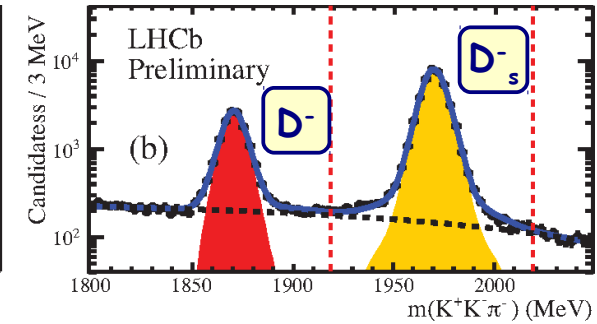
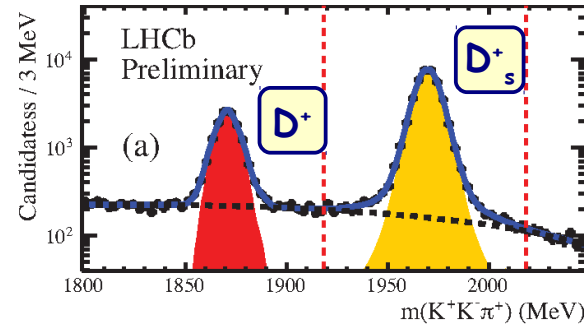
$$A_{\text{raw}} = \frac{N(D_s^- \mu^+) - N(D_s^+ \mu^-)}{N(D_s^- \mu^+) + N(D_s^+ \mu^-)} = \frac{a_{sl}^s}{2} + \left[ a_p - \frac{a_{sl}^s}{2} \right] \times \underbrace{\frac{\int e^{-\Gamma_s t} \cos(\Delta m_s t) \varepsilon(t) dt}{\int e^{-\Gamma_s t} \cosh(\Delta \Gamma_s t/2) \varepsilon(t) dt}}_{= 2 \times 10^{-3} \text{ for LHCb}}$$

(  $\varepsilon(t)$  = decay time acceptance )

## Analysis of $1.0 \text{ fb}^{-1}$ (2011 data set)

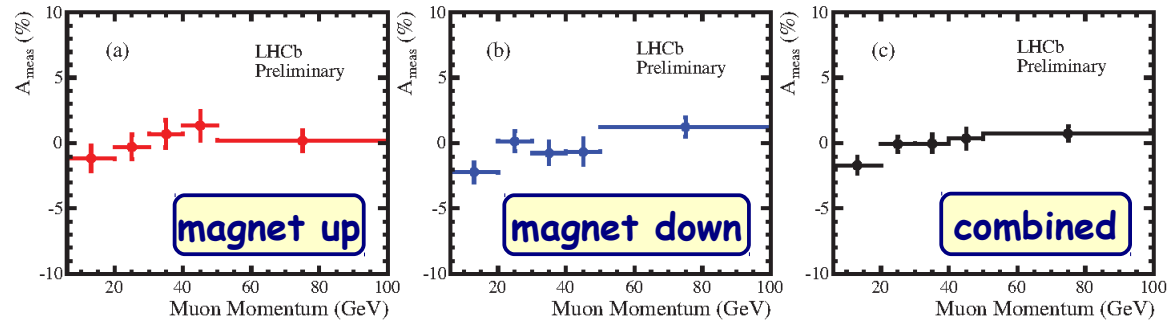
[LHCb-CONF-2012-022]  
preliminary

- clean signals, 193k events, very low backgrounds
- detection efficiencies determined from data using various control channels
- most critical: possible charge asymmetry in muon trigger and muon identification
- studied using large samples of  $J/\psi \rightarrow \mu^+ \mu^-$ 
  - kinematically reconstructed without applying muon identification criteria
  - from events selected by hadron trigger



## Valuable cross check (for many LHCb analyses)

- polarity of LHCb dipole magnet reversed every few weeks
- look at results separately for the two data samples taken with opposite magnet polarity

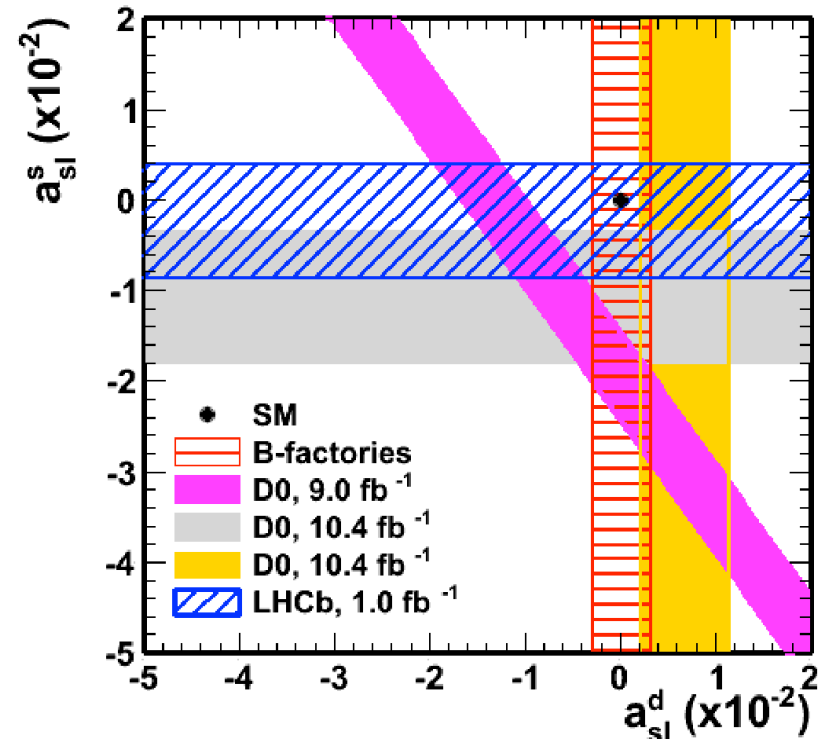


## Result

$$a_{sl}^s = (-0.24 \pm 0.54 \pm 0.33) \%$$

[LHCb-CONF-2012-022] preliminary

- most precise measurement to date
- consistent with Standard Model
- all measurements of  $a_{sl}^s$ ,  $a_{sl}^d$  compatible with each other at  $< 2 \sigma$  level



- **Part I: Introduction**

- what is (quark) flavour physics and why is it so exciting?
- how we got here: brief history of flavour physics in the 20<sup>th</sup> century

- **Part II: Particle-Antiparticle Mixing**

- a little bit of phenomenology (don't worry, I'm an experimentalist ... )
- introduce experimental facilities and techniques

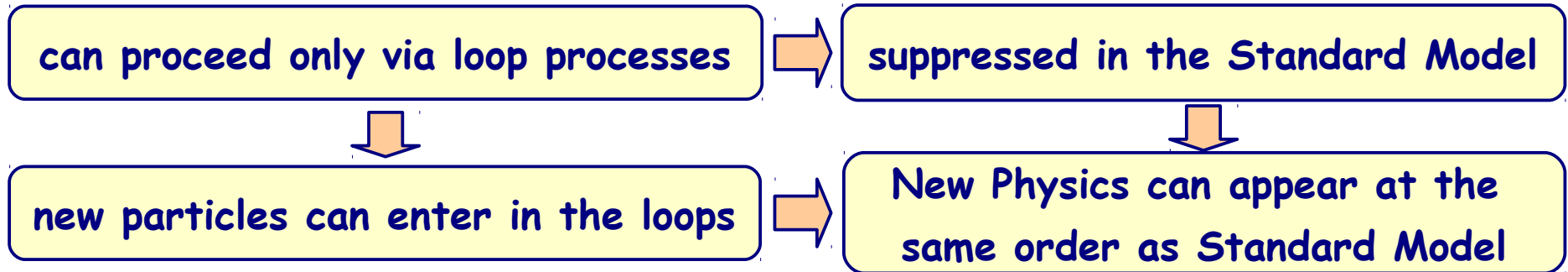
- **Part III: Precision tests of the Standard Model**

- CP violating observables:  $\sin 2\beta$ , CKM angle  $\gamma$ ,  $B_s^0 \bar{B}_s^0$  mixing phase  $\phi_s$
- **rare decays**: search for  $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ , angular observables in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

# Rare Decays

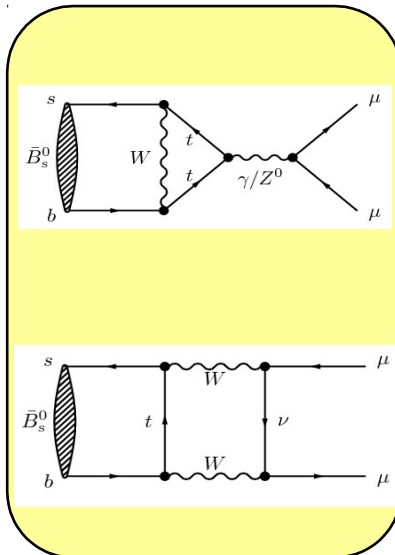
## $b \rightarrow s(d)$ transitions, mediated by Flavour Changing Neutral Currents

- ideal hunting ground for New Physics

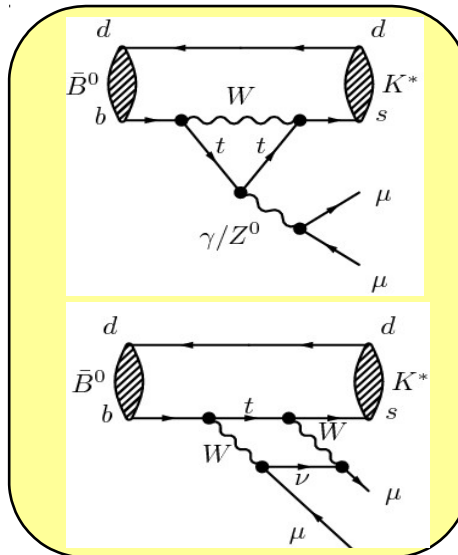


## Most prominent examples

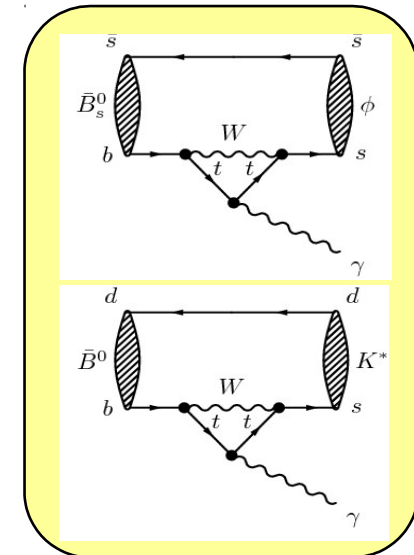
$B^0_{(s)} \rightarrow \mu^+ \mu^-$   
branching fraction



$B^0 \rightarrow K^{0*} \mu^+ \mu^-$   
angular distributions



$B^0 \rightarrow K^{0*} \gamma$  and  $B^0_s \rightarrow \phi \gamma$   
photon polarization



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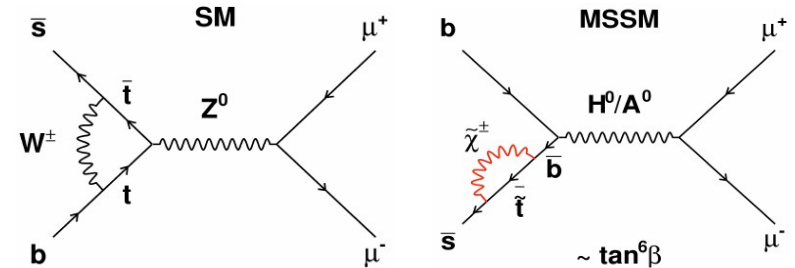
# Rare Decays: $B^0_{(s)} \rightarrow \mu^+ \mu^-$

## $B^0_{(s)} \rightarrow \mu^+ \mu^-$ and $B^0 \rightarrow \mu^+ \mu^-$ very rare in the Standard Model

- GIM suppression and helicity suppression
- predicted branching fractions:

$$\text{BF}(B^0_{(s)} \rightarrow \mu^+ \mu^-) = (3.23 \pm 0.27) \times 10^{-9}$$

$$\text{BF}(B^0 \rightarrow \mu^+ \mu^-) = (1.07 \pm 0.10) \times 10^{-10}$$



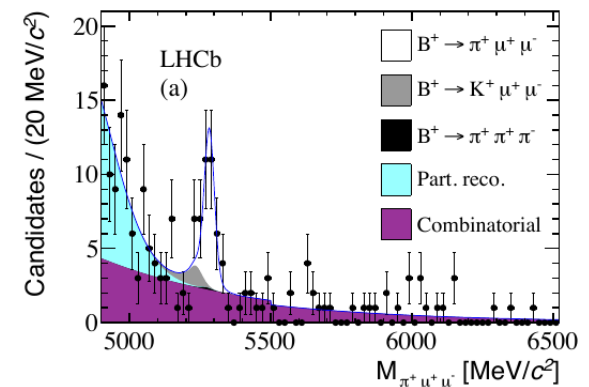
A. Buras et al.,  
[EPJ C72 (2012) 2172]

- sensitive to contributions from scalar and pseudo-scalar sector
- interesting probe for New Physics with extended Higgs sector
- e.g. in MSSM, branching fraction scales approximately as  $\tan^6 \beta / M_A^4$
- compare: rarest B decay observed so far (> 5  $\sigma$  significance)



$$\text{BF}(B^+ \rightarrow \pi^+ \mu^+ \mu^-) = (2.3 \pm 0.6 \pm 0.1) \times 10^{-8}$$

LHCb, [JHEP 1212 (2012) 125]



## Searches at Tevatron and LHC

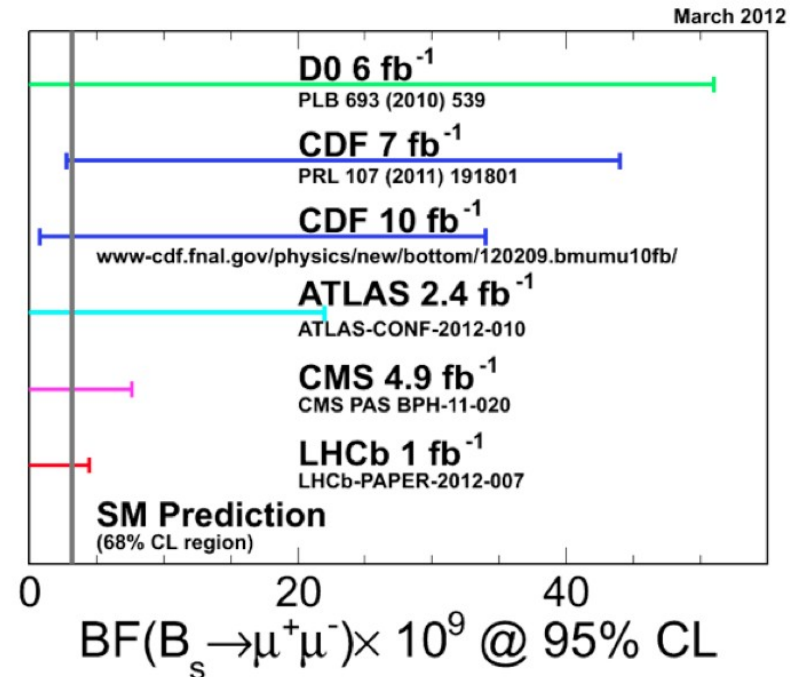
- key features: statistics, mass resolution

	ATLAS	CMS	LHCb
Luminosity	2.4 fb <sup>-1</sup>	4.9 fb <sup>-1</sup>	1.0 fb <sup>-1</sup>
$p_{T,\min}^\mu$	4 GeV	4 GeV	1.5 GeV
Mass window	$\pm 130$ MeV	$\pm 75$ MeV	$\pm 60$ MeV

- LHC combination, June 2012:

$$\text{BF}(B_s^0 \rightarrow \mu^+ \mu^-) < 4.2 \times 10^{-9} \text{ @ 95\% C.L.}$$

[LHCb-CONF-2012-017]



## Subtlety when comparing with Standard Model prediction

- measure time-integrated BF but theoretical prediction evaluated for  $t = 0$
- the two are not equal since  $\Delta\Gamma_s \neq 0$
- “corrected” Standard Model prediction:

$$\text{BF}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.54 \pm 0.30) \times 10^{-9}$$

K. De Bruyn et al., [PRD 86 (2012) 014027]

e.g. BF( $K^0 \rightarrow \pi^+ \pi^-$ ):  
 $\sim 100\%$  for  $t = 0$   
 $\sim 50\%$  time-integrated

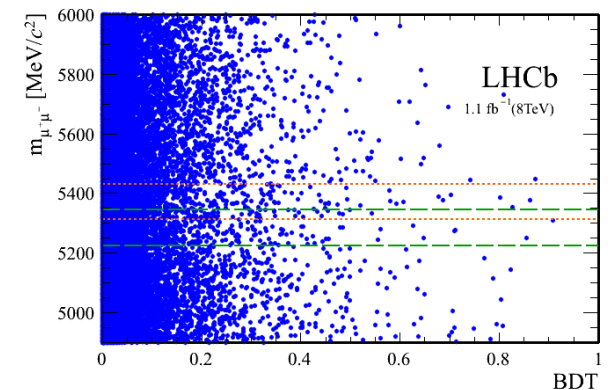
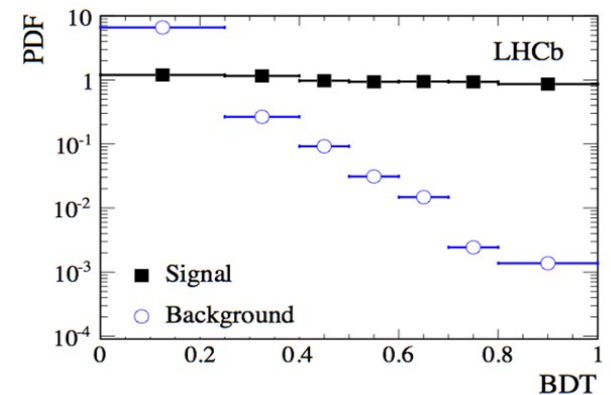
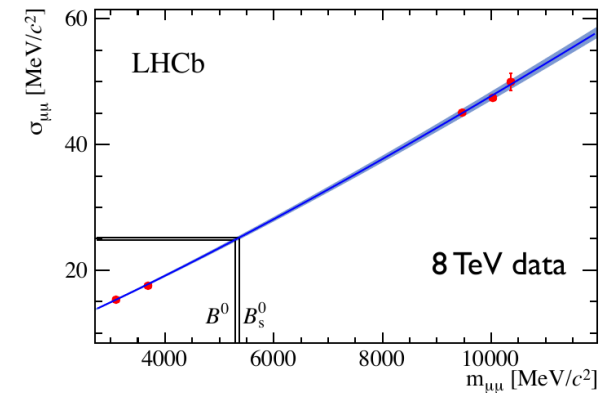


# $B_s^0 \rightarrow \mu^+ \mu^-$ : LHCb

[PRL 110 (2013) 021801]

## LHCb analysis of $2.1 \text{ fb}^{-1}$ (2011 + 50% of 2012 sample)

- signal/background discrimination based on:
- $\mu^+ \mu^-$  invariant mass
  - peak positions calibrated using samples of  $B^0 \rightarrow \pi^+ \pi^-$ ,  $B^0_{(s)} \rightarrow K \pi$ ,  $B^0_{(s)} \rightarrow K^+ K^-$
  - resolution from interpolation between  $J/\psi(ns) \rightarrow \mu^+ \mu^-$  and  $\Upsilon(ns) \rightarrow \mu^+ \mu^-$
- BDT classifier, combining 9 topological variables
  - B decay vertex, impact parameters, ...
  - selected to avoid correlation with mass
  - trained on simulated event samples
  - calibrated on data using of  $B \rightarrow h^+ h^-$  (signal) and invariant mass side bands (background)



# $B^0_{(s)} \rightarrow \mu^+ \mu^-$ : LHCb

## First evidence for $B^0_s \rightarrow \mu^+ \mu^-$

[PRL 110 (2013) 021801]

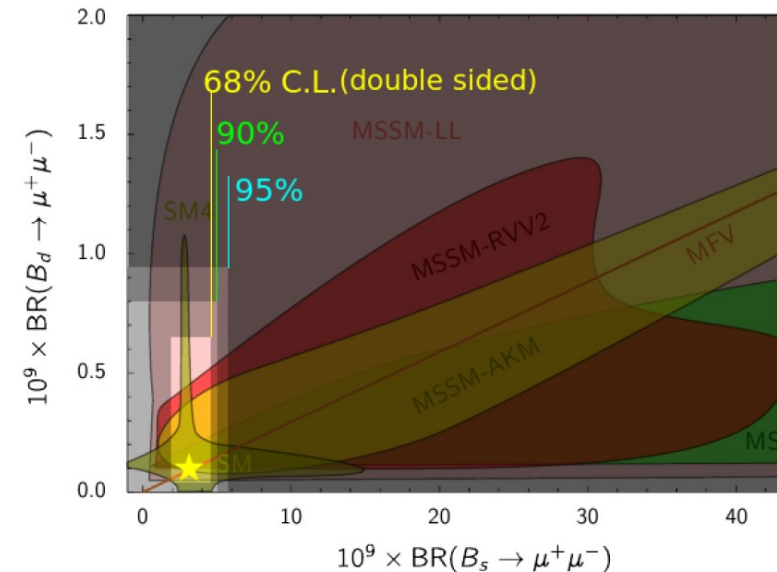
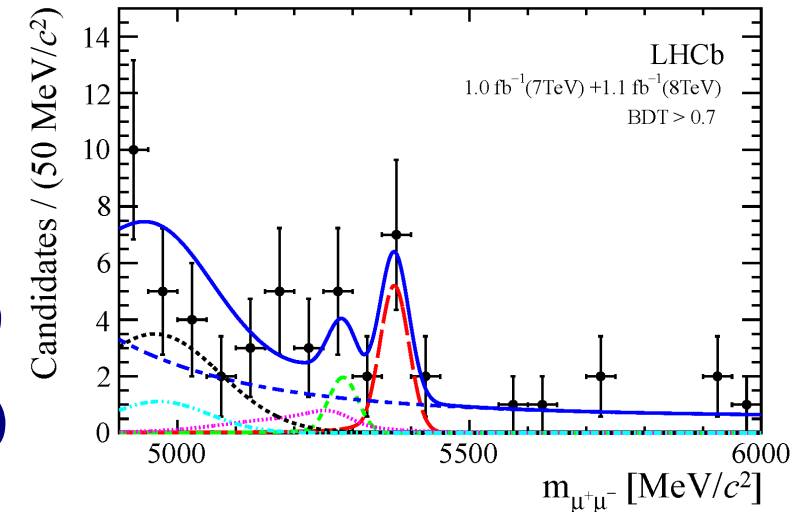
- observe  $3.5 \sigma$  excess over background-only hypothesis (p-value =  $5.3 \times 10^{-4}$ )
- branching fraction normalized to
  - $B^\pm \rightarrow J/\psi K^\pm$  (similar trigger but extra track)
  - $B^0 \rightarrow K^+ \pi^-$  (different trigger, same # tracks)
- normalisation factors agree

$$\text{BF}(B^0_s \rightarrow \mu^+ \mu^-) = (3.2^{+1.4+0.5}_{-1.2-0.3}) \times 10^{-9}$$

- also improved upper limit on  $B^0 \rightarrow \mu^+ \mu^-$

$$\text{BF}(B^0 \rightarrow \mu^+ \mu^-) < 9.4 \times 10^{-10} \text{ @ 95\% C.L.}$$

- results compatible with Standard Model, put stringent constraints on New Physics scenarios



using M. Straub, [arXiv:1205.6094]

- **Part I: Introduction**

- what is (quark) flavour physics and why is it so exciting?
- how we got here: brief history of flavour physics in the 20<sup>th</sup> century

- **Part II: Particle-Antiparticle Mixing**

- a little bit of phenomenology (don't worry, I'm an experimentalist ... )
- introduce experimental facilities and techniques

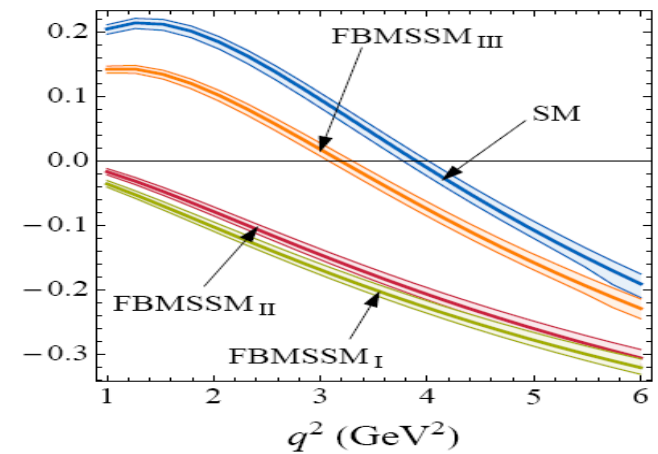
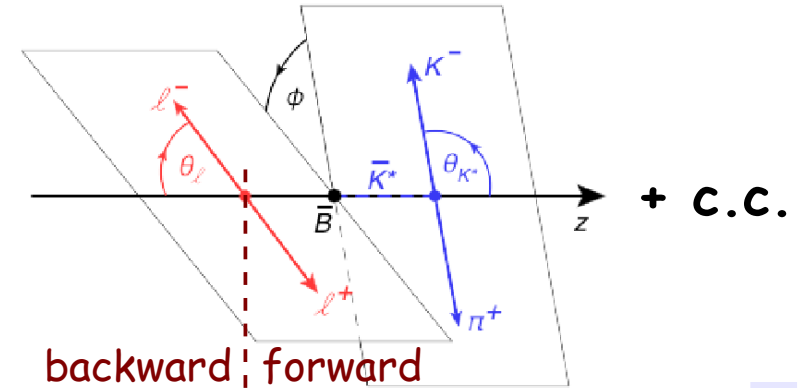
- **Part III: Precision tests of the Standard Model**

- CP violating observables:  $\sin 2\beta$ , CKM angle  $\gamma$ ,  $B_s^0 \bar{B}_s^0$  mixing phase  $\phi_s$
- **rare decays: search for  $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ , angular observables in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$**

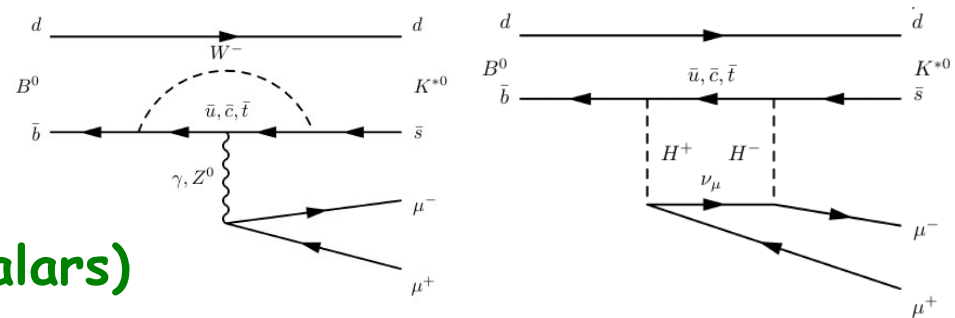
# Rare Decays: $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

## Angular distributions sensitive to contributions from New Physics

- decay can be fully described by three angles ( $\theta_\ell$ ,  $\theta_K$ ,  $\phi$ ) and  $q^2 = m^2(\mu^+\mu^-)$
- differential cross section as a function of these angles gives rise to eight independent observables for which precise predictions can be made as a function of  $q^2$
- prominent example:  $A_{FB}$  = forward-backward asymmetry of the muon in the  $B^0$  rest frame
  - Standard Model predicts zero-crossing of  $A_{FB}$  at a well defined point in  $q^2$
- sensitive to New Physics contributions that affect the helicity structure of the decay (e.g. new scalars, pseudo-scalars)



W. Altmanshofer et al. [JHEP 0901 (2009) 019]



## First measurements at B factories and CDF

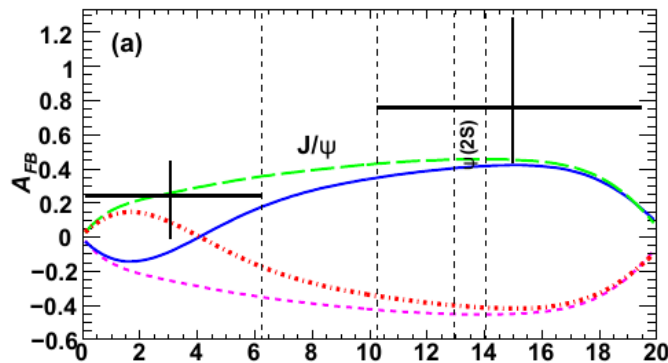
- $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  is a rare decay, but not too rare:  $BF = (1.05^{+0.16}_{-0.13}) \times 10^{-6}$  [PDG]

### Babar:

$384 \times 10^6 \Upsilon(4s) \rightarrow B\bar{B}$  decays

64 signal events

[PRD 79 (2009) 031102]

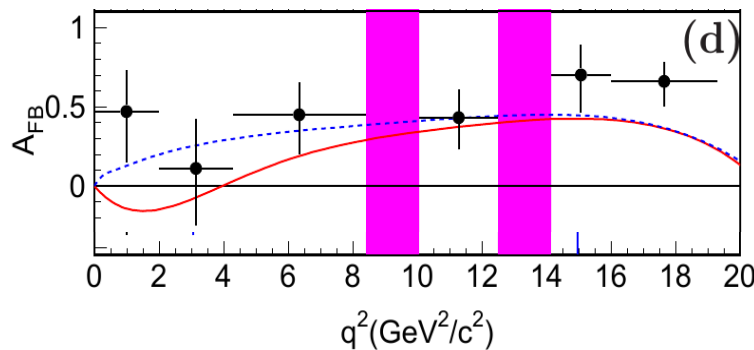


### Belle:

$657 \times 10^6 \Upsilon(4s) \rightarrow B\bar{B}$  decays

244 signal events

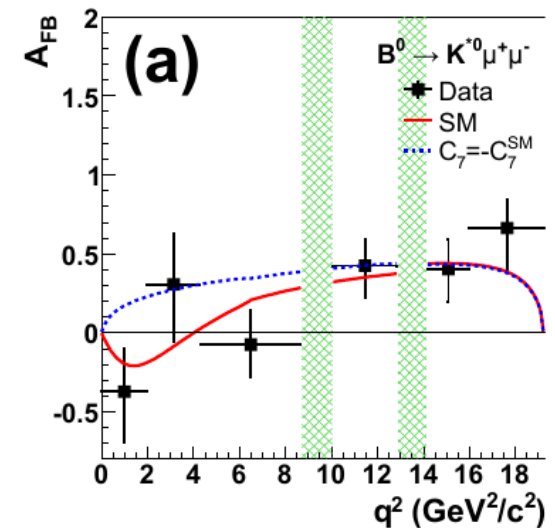
[PRL 103 (2009) 171801]



### CDF: $6.8 \text{ fb}^{-1}$

164 signal events

[PRL 108 (2012) 081807]



- hint for deviation from Standard Model prediction (solid lines) at low  $q^2$ ?
- Belle:  $A_{FB}$  exceeds Standard Model expectation by  $2.7 \sigma$
- but statistics limited, measurement uncertainties still large

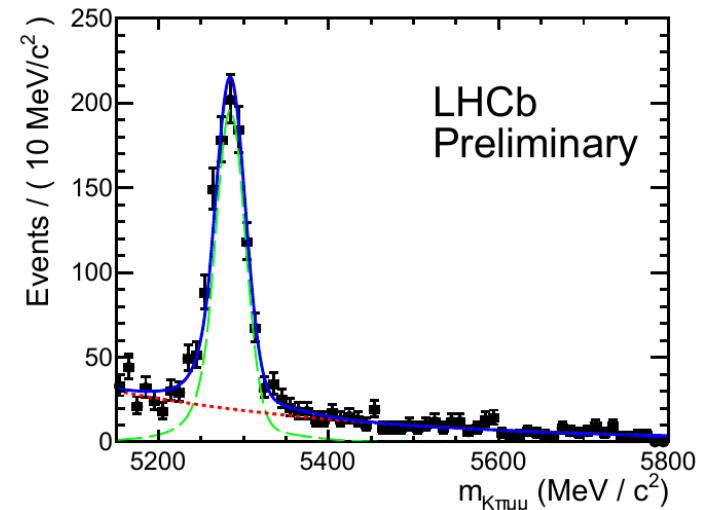
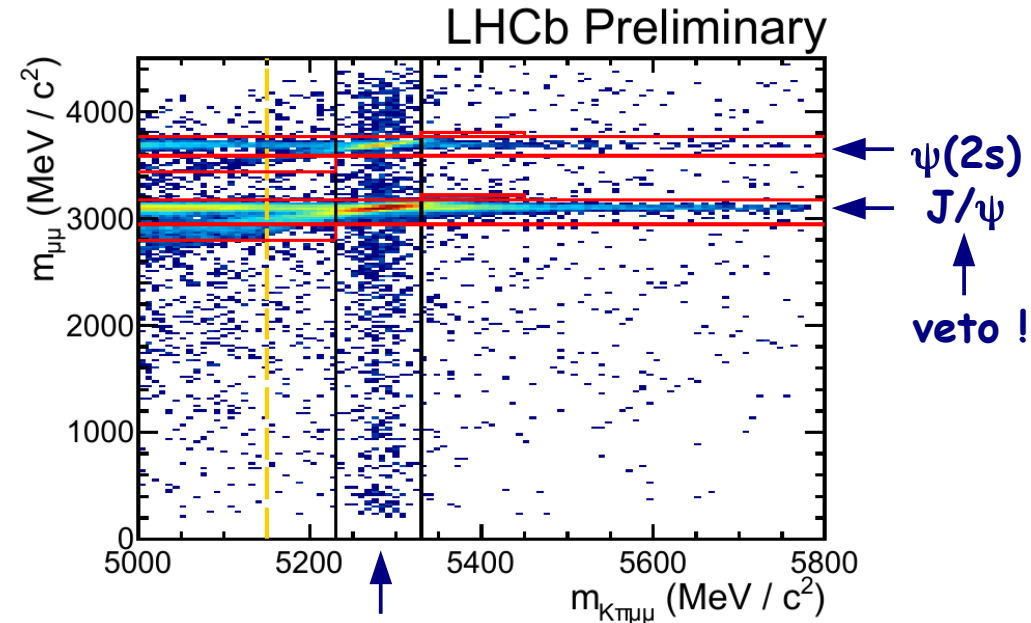
# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ : LHCb

900 signal events from  $1 \text{ fb}^{-1}$  (2011 data set)

[LHCb-CONF-2012-008]  
preliminary

- event selection: BDT using track quality criteria, kinematic and topological event properties,
- have to veto  $\mu^+ \mu^-$  mass windows around  $J/\psi$  and  $\psi(2s)$  to suppress irreducible backgrounds from  $B^0 \rightarrow K^{*0} J/\psi$  and  $B^0 \rightarrow K^{*0} \psi(2s)$
- large sample of  $B^0 \rightarrow K^{*0} J/\psi (\mu^+ \mu^-)$  used to train BTD, also ideal control sample to study acceptance effects on the angular distributions

“every disadvantage has its advantage”  
(Johan Cruijff, footballing philosopher)



## "Folding technique"

- differential cross section as a function of  $(\theta_\ell, \theta_K, \phi, q^2)$

$$\frac{d^4\Gamma}{d \cos \theta_\ell d \cos \theta_K d\phi dq^2} \propto I_1^s \sin^2 \theta_K + I_1^c \cos^2 \theta_K + (I_2^s \sin^2 \theta_K + I_2^c \cos^2 \theta_K) \cos 2\theta_\ell$$

$$+ I_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + I_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi$$

$$+ I_5 \sin 2\theta_K \sin \theta_\ell \cos \phi$$

$$+ (I_6^s \sin^2 \theta_K + I_6^c \cos^2 \theta_K) \cos \theta_\ell + I_7 \sin 2\theta_K \sin \theta_\ell \sin \phi$$

$$+ I_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + I_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi$$

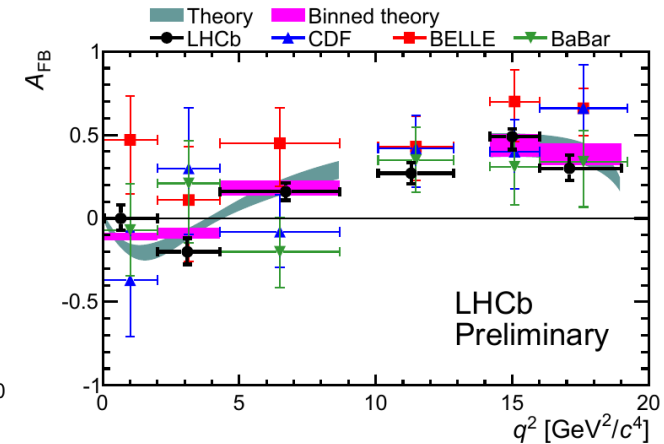
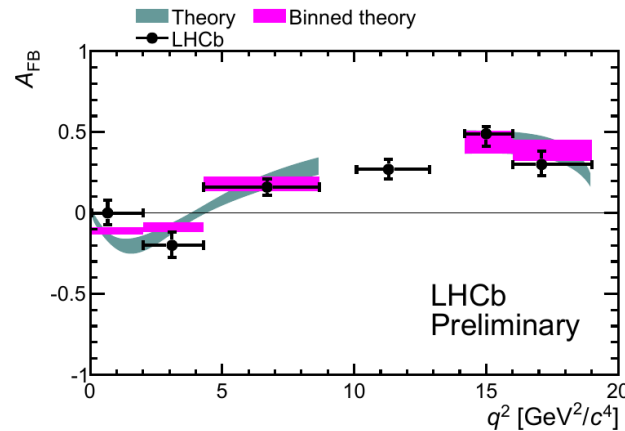
- $I_i = I_i(q^2)$ ; the observables we want to extract are combinations of these  $I_i$
- event sample not (yet) large enough to fit all observables simultaneously
  - reduce number of fit parameters by integrating over some of the angles
  - better: apply "folding technique" exploiting symmetry of sin/cos functions
    - e.g. replacing  $\phi$  by  $\phi + \pi$  for  $\phi < 0$  cancels all terms with  $I_4, I_5, I_7, I_8$
    - four observables remain (one of them  $A_{FB}$ )  $\rightarrow$  fit these simultaneously

# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ : LHCb

## LHCb: results (from $1 \text{ fb}^{-1}$ )

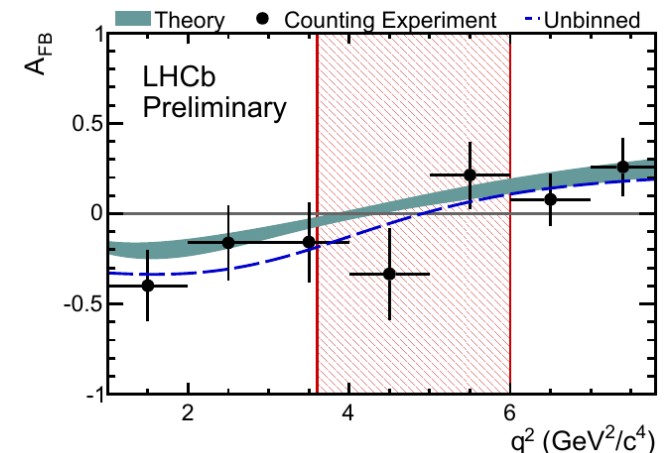
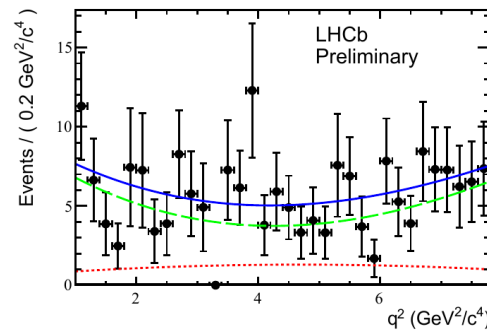
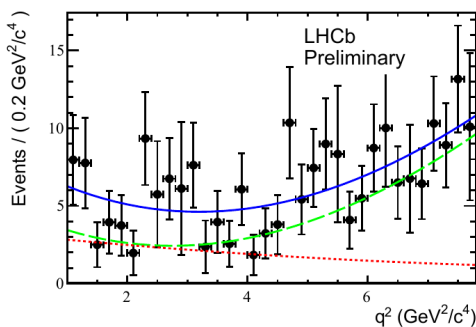
- all observables in good agreement with Standard Model prediction
- also compatible with previous experiments

[LHCb-CONF-2012-008]  
preliminary



## Also: first extraction of the zero crossing point of $A_{FB}(q^2)$

- separately fit event yields for forward-going and backward-going events as a function of  $q^2$ , then calculate the asymmetry
- again, result agrees with Standard Model





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**Short Appendix: Outlook**

- Part III: Precision tests of the Standard Model

- CP violating observables:  $\sin 2\beta$ , CKM angle  $\gamma$ ,  $B_s^0 \bar{B}_s^0$  mixing phase  $\phi_s$
- rare decays: search for  $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ , angular observables in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

- LHC and LHCb are a spectacular success
- and so is the Standard Model
  - ... at least so far
- current precision of measurements still leaves lots of room for sub-dominant contributions from New Physics
- almost all LHCb results are completely dominated by statistical uncertainties
- leading systematic uncertainties will also decrease with increasing statistics

**NEED MORE STATISTICS**

⇒

**THE LHCb UPGRADE !**

2010	0.037 fb <sup>-1</sup> @ 7 TeV
2011	1 fb <sup>-1</sup> @ 7 TeV
2012	2 fb <sup>-1</sup> @ 8 TeV
2013	LHC LS1
2014	
2015	5 fb <sup>-1</sup> @ 13 TeV
2016	
2017	
2018	LHC LS2, LHCb upgrade
2019	
2020	5 fb <sup>-1</sup> per year
2021	
2022	

- goal: reach measurement precision that matches theory uncertainties

[CERN-LHCC-2012-007]

Type	Observable	Current precision	LHCb 2018	Upgrade (50 fb <sup>-1</sup> )	Theory uncertainty
$B_s^0$ mixing	$2\beta_s (B_s^0 \rightarrow J/\psi \phi)$	0.10 [9]	0.025	0.008	$\sim 0.003$
	$2\beta_s (B_s^0 \rightarrow J/\psi f_0(980))$	0.17 [10]	0.045	0.014	$\sim 0.01$
	$A_{fs}(B_s^0)$	$6.4 \times 10^{-3}$ [18]	$0.6 \times 10^{-3}$	$0.2 \times 10^{-3}$	$0.03 \times 10^{-3}$
Gluonic penguin	$2\beta_s^{\text{eff}}(B_s^0 \rightarrow \phi\phi)$	–	0.17	0.03	0.02
	$2\beta_s^{\text{eff}}(B_s^0 \rightarrow K^{*0}\bar{K}^{*0})$	–	0.13	0.02	$< 0.02$
	$2\beta_s^{\text{eff}}(B^0 \rightarrow \phi K_S^0)$	0.17 [18]	0.30	0.05	0.02
Right-handed currents	$2\beta_s^{\text{eff}}(B_s^0 \rightarrow \phi\gamma)$	–	0.09	0.02	$< 0.01$
	$\tau^{\text{eff}}(B_s^0 \rightarrow \phi\gamma)/\tau_{B_s^0}$	–	5 %	1 %	0.2 %
Electroweak penguin	$S_3(B^0 \rightarrow K^{*0}\mu^+\mu^-; 1 < q^2 < 6 \text{ GeV}^2/c^4)$	0.08 [14]	0.025	0.008	0.02
	$s_0 A_{\text{FB}}(B^0 \rightarrow K^{*0}\mu^+\mu^-)$	25 % [14]	6 %	2 %	7 %
	$A_{\text{I}}(K\mu^+\mu^-; 1 < q^2 < 6 \text{ GeV}^2/c^4)$	0.25 [15]	0.08	0.025	$\sim 0.02$
	$\mathcal{B}(B^+ \rightarrow \pi^+\mu^+\mu^-)/\mathcal{B}(B^+ \rightarrow K^+\mu^+\mu^-)$	25 % [16]	8 %	2.5 %	$\sim 10 \%$
Higgs penguin	$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-)$	$1.5 \times 10^{-9}$ [2]	$0.5 \times 10^{-9}$	$0.15 \times 10^{-9}$	$0.3 \times 10^{-9}$
	$\mathcal{B}(B^0 \rightarrow \mu^+\mu^-)/\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-)$	–	$\sim 100 \%$	$\sim 35 \%$	$\sim 5 \%$
Unitarity triangle angles	$\gamma (B \rightarrow D^{(*)}K^{(*)})$	$\sim 10\text{--}12^\circ$ [19, 20]	$4^\circ$	$0.9^\circ$	negligible
	$\gamma (B_s^0 \rightarrow D_s K)$	–	$11^\circ$	$2.0^\circ$	negligible
	$\beta (B^0 \rightarrow J/\psi K_S^0)$	$0.8^\circ$ [18]	$0.6^\circ$	$0.2^\circ$	negligible
Charm	$A_\Gamma$	$2.3 \times 10^{-3}$ [18]	$0.40 \times 10^{-3}$	$0.07 \times 10^{-3}$	–
$CP$ violation	$\Delta A_{CP}$	$2.1 \times 10^{-3}$ [5]	$0.65 \times 10^{-3}$	$0.12 \times 10^{-3}$	–

- two lines of attack
  - increase trigger efficiencies for hadronic final states
    - read out the full detector at the LHC bunch-crossing frequency
  - operate the detector at up to  $\times 5$  higher luminosity
    - new main tracker to cope with increase in particle densities

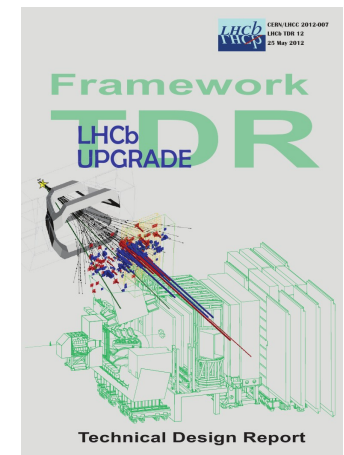
expected increase in rate (compared to 2011):  
 $\times 10$  for channels involving final-state muons  
 $\times 20$  for channels to fully hadronic final states

- details are described in

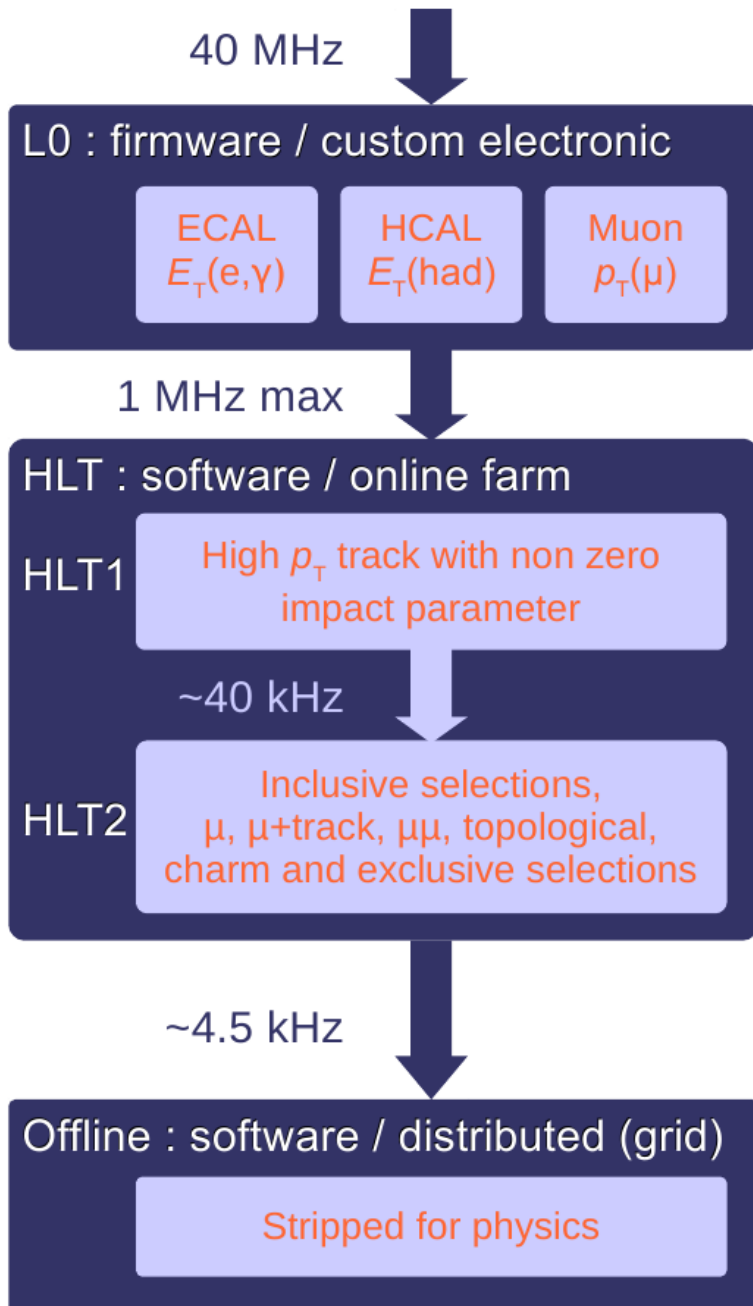
- Letter of Intent [CERN-LHCC-2011-001]

- Framework TDR [CERN-LHCC-2012-007]

- endorsed by the LHCC

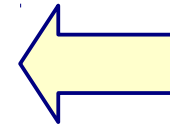
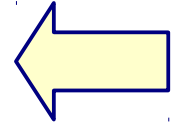


# Reminder: Current LHCb Trigger



## Hardware level (L0):

- maximum output rate 1 MHz
- typical thresholds 2012:
  - $E_T(e/\gamma) > 2.7 \text{ GeV}$
  - $E_T(h) > 3.6 \text{ GeV}$
  - $p_T(\mu) > 1.4 \text{ GeV}$



## Software level (HLT):

~ 30000 tasks in parallel on ~ 1500 nodes

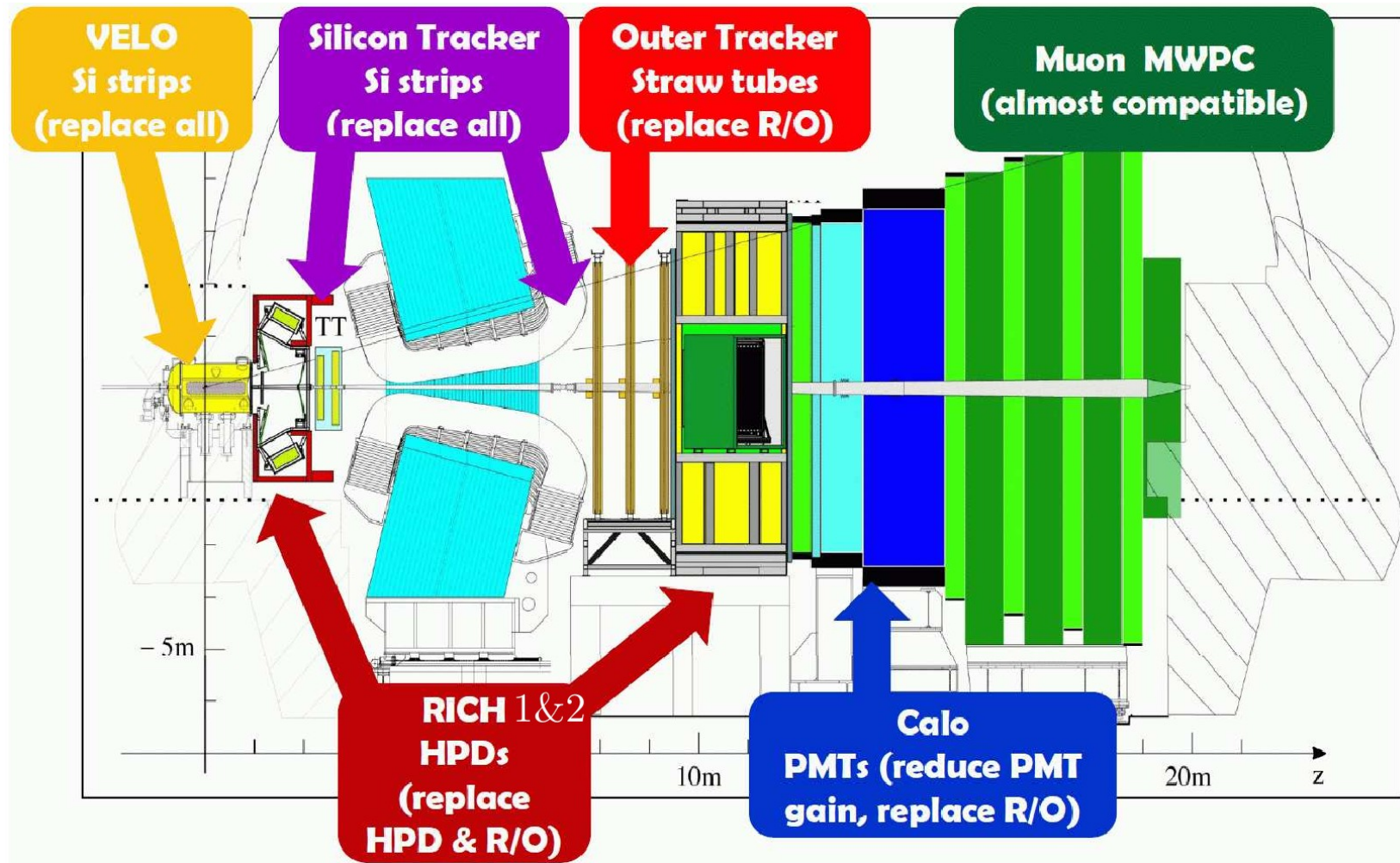
## Combined efficiency (L0+HLT):

- ~ 90 % for di-muon channels
- ~ 30 % for multi-body hadronic final states

## Offline processing:

~  $10^{10}$  events, 700 TB recorded per year

# Upgrade



- 2012/2013: R&D, technology choices, preparation of sub-system TDRs
- 2014: funding, procurements
- 2015-2019: construction and installation